
Basic Notation

\mathbb{N} : set of all natural numbers.

$\mathbb{N}_0 = \mathbb{N} \cup \{0\}$.

\mathbb{R} : set of all real numbers.

\mathbb{R}^n : n -dimensional Euclidean space.

$\mathbb{R}_+^n : \{(x_i) \in \mathbb{R}^n : x_n > 0\}$.

ω_n : volume of unit ball in \mathbb{R}^n .

Ω : open subset of \mathbb{R}^n with closure $\overline{\Omega}$ and boundary $\partial\Omega$.

$B(X, Y)$: space of all bounded linear maps from a Banach space X to another such space Y .

$K(X, Y)$: subspace of $B(X, Y)$ consisting of all compact linear maps from X to Y .

Embedding: a bounded linear injective map of a Banach space X to another such space Y .

$X \hookrightarrow Y$: the space X is embedded in Y .

$X \hookrightarrow\hookrightarrow Y$: the space X is compactly embedded in Y .

$L_p(\Omega)$: the Lebesgue space of all scalar-valued functions f on Ω such that $\int_{\Omega} |f|^p dx < \infty$ ($1 \leq p < \infty$).

$L_{\infty}(\Omega)$: the Lebesgue space of all scalar-valued functions f on Ω such that $\text{ess sup}_{\Omega} |f(x)| < \infty$.

F : Fourier transform given by $F(f)(\xi) = (2\pi)^{-n/2} \int_{\mathbb{R}^n} f(x)e^{-ix \cdot \xi} dx$.