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OF  
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EDITED BY

ALONZO CHURCH    S. C. KLEENE    ALICE A. LAZEROWITZ

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## TABLE OF CONTENTS

A generalization of the concept of $\omega$ -completeness. By LEON HENKIN . . . . .	1
Eulerian syllogistic. By IVO THOMAS . . . . .	15
Sur la structuration du tableau des connectifs interpositionnels binaires. By ROBERT BLANCHÉ . . . . .	17
A theory of restricted quantification I. By THEODORE HAILPERIN . . . . .	19
Two theories with axioms built by means of pleonasms. By ANDRZEJ EHRENFEUCHT . . . . .	36
Decidability and essential undecidability. By HILARY PUTNAM . . . . .	39
Languages in which self reference is possible. By RAYMOND M. SMULLYAN . . . . .	55
Reviews . . . . .	68
Twenty-first annual meeting of the Association for Symbolic Logic. By L. GÁL . . . . .	105
Abstracts of papers . . . . .	105
Elections . . . . .	112
A theory of restricted quantification II. By THEODORE HAILPERIN . . . . .	113
Uniformization of linear arrays. By N. J. FINE and R. HARROP . . . . .	130
On the axioms of order and succession. By KURT BING . . . . .	141
The axiomatization of arithmetic. By HAO WANG . . . . .	145
A criterion for completeness of degrees of unsolvability. By RICHARD FRIEDBERG . . . . .	159
Degrees of unsolvability associated with classes of formalized theories. By SOLOMON FEFERMAN . . . . .	161
New foundations for Lewis modal systems. By E. J. LEMMON . . . . .	176
On the representation of Herbrand functions in algebraically closed fields. By A. H. LIGHTSTONE and A. ROBINSON . . . . .	187
Reviews . . . . .	205
Can the logic of indirect discourse be formalised. By L. JONATHAN COHEN . . . . .	225
Inference by complementary elimination. By BERNARD K. SYMONDS and RODERICK M. CHISHOLM . . . . .	233

TABLE OF CONTENTS

Inferential equivalence and natural deduction. By H. HIŻ . . . . .	237
Independent axiom schemata for von Wright's <i>M</i> . By ALAN ROSS ANDERSON . . . . .	241
Vicious circle principle and the paradoxes. By K. JAAKKO J. HINTIKKA . . . . .	245
Linear reasoning. A new form of the Herbrand-Gentzen theorem. By WILLIAM CRAIG . . . . .	250
Three uses of the Herbrand-Gentzen theorem in relating model theory and proof theory. By WILLIAM CRAIG . . . . .	269
Reviews . . . . .	286
Some results in Church's restricted recursive arithmetic. By JOYCE FRIEDMANN . . . . .	337
A definition of existence in terms of abstraction and disjunction. By FREDERIC B. FITCH . . . . .	343
On logically false evidence statements. By HUGUES LEBLANC . . . . .	345
Reviews . . . . .	350
List of officers and members of the Association for Symbolic Logic	410
Index of reviews . . . . .	422

## ERRATA

### VOLUME 19

Page 39, line 4. The italic *A* should be roman.

### VOLUME 20

Page V. Delete the indicated correction to volume 19, page 38, line 4.

Page 291, line 5. Insert «*against descriptions*» following «*names*».

Page 358, line 9. For «*simplication*», read «*simplification*».

### VOLUME 21

Page 79, line 1. Insert «*the*» before «*synthetic*».

Page 82, line 3. For «*an P-description*», read «*a P-description*».

Page 211, line 3 from below. For 265, read 266.

Page 271, last line of footnote. For  $\epsilon$ , read  $\phi$ .

Page 330, line 14 from below. For «*dont'*», read «*don't*».

Page 384, line 11. For «*propositions*», read «*presuppositions*».

Page 389, line 12. For «*vol. 29*», read «*vol. 28*».

Page 399, line 25. For «*1941*», read «*no. 2 (1941)*».

Page 405, line 8. For *Z*, read *S*.

Page 409, line 15. Replace comma at the end of the line by a period.

Page 409, lines 3 and 4 from below. The letter «*a*» should be deleted in each of the four formulas.

Page 411, line 12, displayed formula. Replace the subscript 1 to  $p$  by a subscript  $i$ .

Page 416, line 4. For «**Bar-Hillil**», read «**Bar-Hillel**».

### VOLUME 22

Page 41, second line of footnote. For «*Harvard*», read «*Holt*».

Page 71, line 3. For «*exsistential*», read «*existential*».

Page 76, line 15. For  $\sigma$ , read  $\sigma'$ .

Page 79, line 24. For «*pp. 112*», read «*112 pp.*».

Page 79, line 19 from below. For «*clod*», read «*closed*».

Page 82, line 14. Insert space after «*only*».

Page 82, line 15. Delete space after ( $\exists x$ ).

Page 99, lines 17 and 18 from below. Read «*Časopis pro pěstování matematiky*, vol. 78 (1953), pp. 373–375».

Page 99, line 12 from below. For «*no. 2*», read «*vol. 2*».

Page 169, footnote 9, line 3. For «*Rassers's*», read *Rosser's*.

## ERRATA

Page 205, line 19 from below. For first «of», read «or».

Page 217, line 13. For  $\mathcal{O}$ , read  $\mathcal{Q}$ .

Page 217, line 25. For «Thorien», read «Theorien».

Page 297, line 27. For «S. 34–67», read «S. 55–67».

Page 300, line 14 from below. For «*Acte*», read «*Actes*».

Page 312, line 20. Insert a left parenthesis before «*Analysis*».

Page 319, line 12 from below. For 1957, read 1956.