Index

ε -expansion 62 definition 146	
ϕ^3 theory 36 equations of motion 155, 158	
one-loop calculations 38 mixing under renormalization 149	
Λ parameter of QCD 188 properties 152	
renormalization, example 142	
Adler-Bardeen theorem 338 tensor operators 150	
Altarelli-Parisi equation 370 twist 363	
anomalies 331 Ward identities 160	
Adler-Bardeen theorem 338 see also operator product expansion	on
not in non-singlet axial current 346 continuum limit 8	
one-loop calculation 342 see also renormalization	
triangle 349 coordinate space, renormalization in	59.
anomalously broken symmetries 18, 331 277	,
asymptotic freedom 187 cosmological term, and renormalizat	ion
118	1011
bare parameters counterterm Lagrangian 11, 89	
definition 10 cut-off	
renormalization group calculation 209 dimensional regularization 13, 53,	62
dimensional regularization 217 for infra-red 56	
basic graph 90 lattice 8	
basic Lagrangian 89 Pauli-Villars 12	
definition 11 see also individual entries	
BPH 53	
see also renormalization prescriptions decoupling theorem 222	
BPHZ 53, 133 examples 226	
see also renormalization prescriptions exceptions 223	
broken symmetries 18 manifest decoupling 230	
anomalous 18 proof 233	
dynamically 19 renormalization group 240	
explicitly 18 deep inelastic scattering 354	
spontaneously 18 Altarelli-Parisi equation 370	
not at $d = 2.26$ calculation of Wilson coefficients 3	364
perturbation theory 26, 247 operator product expansion 361	
renormalization 247, 314 partons and operator product exp	ansion
BRS, see gauge theories 369	
W_4 and W_5 357, 371	
canonical momentum field 5 degree of divergence 45	
causality 6 differentiation with respect to param	eters
charge conjugation symmetry, for gauge in Lagrangian 163	
theories 35 dimensional regularization 13, 53, 62	
chiral symmetry 17, 333 axioms 64	
and anomalies 338 definition 67	
commutation relations convergence 68	
canonical equal-time 5 Dirac matrices in 83, 334	
from Green's functions 6 list of integrals 81	
composite operators 138 properties 73	

378 Index

reduced to ordinary integration 67	unbroken, invariance of counterterms
uniqueness 65	245
dimensional transmutation 203	Goldstone bosons, see Nambu-Goldstone
Dirac matrices	bosons
γ_5 at $d \neq 4$ 86, 334	Goldstone model 247
definition in d dimensions 83	Grassmann algebra 27
dynamically broken symmetries 19	Green's functions
	definition 6
equations of motion	equations of motion 13
Green's function 6,13	functional integral 7
momentum space 15	generating functional 7
operator 5	momentum space 15
Euclidean space-time 8.	TT 11
evanescent operators 346	Hamiltonian, field theory 5
explicit symmetry breaking 18	
ftitititi	infra-red behavior, and renormalization
factorization theorems 1, 187	group 187, 191
Faddeev-Popov ghost, see gauge theories	Landau shart 106
Feynman rules	Landau ghost 196
for gauge theories 34	large mass expansion 222
see also perturbation theory	large momentum behavior of Green's functions 185
fixed points 190 forest formula 109	lattice 8
3-loop example 106	
functional integral	leading logarithms 193 non-renormalization group 196
for bosons 6	list of integrals 81
for fermions 27	low-energy behavior 191
Monte-Carlo calculation 13	low-energy behavior 191
Worte-Carlo calculation 15	mass-shell renormalization prescription 48
gauge dependence of counterterms 309,	massive photon, renormalization 324
327	minimal subtraction 56, 135
gauge invariant operators 316	see also renormalization prescriptions
gauge theories 28	Monte-Carlo 13
BRS invariance 32	
charge conjugation symmetry 35	Nambu-Goldstone bosons 21, 252
Faddeev-Popov ghost 30	Noether's theorem 18
Feynman rules 34	non-renormalizability 49
gauge invariance v. gauge independence	in real physics 122
31	non-renormalization of currents 162
gauge-fixing 30	normal products, see composite operators
operator product expansion 321	1 , 1
proof of renormalizability 298	operator product expansion 257
quantization 29	and parton model 369
renormalization 293	and renormalization group 274
renormalization group 319	deep inelastic scattering 361
Slavnov-Taylor identities 32	examples 139, 258
Gell-Mann-Low formula 22	gauge theories 321
General Relativity	in coordinate- and momentum-space 257
as example of gauge theory 17	proof 266
cosmological term and renormalization	to define composite operators 258
118	overlapping divergence 99
generating functional	oversubtraction 130
for Green's functions 7	on 1PR graphs 131
global symmetries	
renormalization 244	partition function, functional integral as 8
spontaneously broken, invariance of	parton model 355, 358, 369
counterterms 247	Pauli-Villars cut-off 12

Index 379

manturbation theory 21	oversubtraction 130
perturbation theory 21 as saddle point expansion 26	oversubtraction 130 prescriptions 52
Feynman rules for gauge theories 34	QED 293, 322
maximum accuracy with asymptotic	with photon mass 323
freedom 189	renormalization group 50, 168
not convergent 24, 189	A parameter 188
perturbative QCD 1	asymptotic freedom 187
Poincaré symmetry 17	change of renormalization prescription
propagator 22	200
short-distance behavior 278	coefficients 180
thermal 280	composite operators 219
	computation of bare parameters 209
QCD	dimensional regularization 217
Λ parameter 188	cut-off procedure, dependence on 206
asymptotic freedom 188	decoupling theorem 240
Feynman rules 34	dimensional transmutation 203
perturbative 1	equation 183
see also gauge theories	examples 50, 172
QED	fixed points 190
gauge dependence of counterterms 327	gauge theories 319
in external field 291	infra-red behavior 187, 191
renormalization 293, 322	Landau ghost 196
renormalization group 329	large momentum behavior 185
Ward identities 326	leading logarithms 193
see also gauge theories	minimal subtraction 56, 181
quantum chromodynamics, see QCD	several couplings 197
quantum electrodynamics, see QED	solution of RG equation 184
quantum field theory	renormalization prescriptions 52
analog of statistical mechanics 8	BPH 53
axioms 6	BPHZ 53, 133
review 4	mass-shell 48
standard properties 6	minimal subtraction 135
standard theories 36	at one loop 56
see also,	spontaneously broken symmetries 253
ϕ^3 theory; QCD; QED	renormalized field 10
quantum mechanics	renormalized mass, and physical mass 51
as field theory at $d = 1.6$	
R_{ξ} -gauge 314	Slavnov-Taylor identities 32
reconstruction theorem 6	spontaneously broken symmetries 18
regulator, see cut-off	absence of IR divergences 252
renormalizability 49, 116	choice of renormalization prescription
renormalization 9, 88	253
and continuum limit 9	renormalization 247
axial current 340	renormalization of current 251
coordinate space 59, 277	super-renormalizability, definition 118
examples 281	supersymmetries 17, 339
examples 38	symmetries 15, 244
for massless theories 59	BRS, see gauge theories
forest formula 109	charge conjugation, see gauge theories
gauge dependence of counterterms 309, 327	gauge 28
	Ward identities 19, 160
gauge invariant operators 316	see also broken symmetries; global
gauge theories 293	symmetries
with symmetry breaking 308, 314	thormodynamia limit of fractional interest
in external field 291 locality of counterterms 97, 125	thermodynamic limit of functional integral
non-zero temperature 286	triangle anomaly 349

twist 363

ultra-violet regulators 12 see also cut-off; dimensional regularization unitary gauge 324, 330

Ward identities 16, 19, 160 axial current 339, 349 **QED 326**

Index

renormalization 246-256 Weinberg's theorem 125 Wick rotation 8, 39 Wightman axioms 6
Wilson expansion, see operator product expansion

Yang-Mills theory, see gauge theories



