Advances in Applied Probability

The Editorial Board would like to encourage the submission to the *Advances* of Review Papers summarising and coordinating recent results in any of the fields of Applied Probability. The papers should be approximate y 40-50 printed pages in length.

In addition to these Review Papers, Advances is also designed to be a medium of publication for (1) long research papers in Applied Probability, which may include expository material, (2) expository papers on branches of mathematics of interest to probabilists, (3) papers outlining areas in the biological, physical, social and technological sciences in which probability models can be usefully developed, and finally, (4) papers in Applied Probability presented at conferences which do not publish their proceedings.

In short, the main function of *Advances* is to define areas of recent progress and potential development in Applied Probability. As with the *Journal of Applied Probability*, *Advances* undertakes to publish papers accepted by the Editors within 15 months of their submission.

The Editorial Board consists of E. Sparre Andersen, D. Blackwell, B. Gnedenko, J. Hájek, E. J. Hannan, D. G. Kendall, J. F. C. Kingman, K. Krickeberg, R. M. Loynes, P. A. P. Moran, J. Neveu, K. R. Parthasarathy, R. Pyke, C. A. B. Smith and L. Takács. The Editor-in-Chief is J. Gani, and the Editorial Office of the *Advances* is in the Department of Probability and Statistics, The University, Sheffield, S3 7RH, England.

Volume 4 No. 1 of Advances will contain the following papers:

J. E. Moyal Particle populations and number operators in quantum

theory

E. Lukacs A survey of the theory of characteristic functions

Z. A. Lomnicki Two-terminal series-parallel networks

R. K. Milne and M. Westcott Further results for Gauss-Poisson processes

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M. Brown Low density traffic streams

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Editorial Assistant, Advances in Applied Probability,

Department of Probability and Statistics,

The University, Sheffield, S3 7RH, England.

ANNOUNCEMENT

The Hungarian Academy of Sciences, the International Association for Statistics in the Physical Sciences Section of the International Statistical Institute and the European Region of the Institute of Mathematical Statistics are jointly sponsoring the

BUDAPEST, AUGUST 31-SEPTEMBER 5, 1972

EUROPEAN MEETING OF STATISTICIANS

organized by the Bolyai János Mathematical Society

1. Among the speakers who are invited to give 1 hour addresses are:

Bunke, O.

Dietz, K.

Hajek, J.

Shirvayev, A. N.

Cacoullos, T.

Kingman, J. F. C. Kolmogorov, A. N. Urbanik, K. Vincze, I.

Lindley, D. V.

The following are also among those who have been invited to give 30 minute talks:

Ahlswede, R.

Girault, M.

Neveu, J.

Bühler, W.

Iosifescu, M.

Papangelou, F.

Cox, D. R.

Kendall, D. G.

Spitzer, F.

2. It is tentatively expected that the meeting will proceed as follows:

	Morning	Afternoon	Evening
Thursday, August 31	Scientific program: 1 hour invited talk 1 hour invited talk	Scientific program: 1 hour invited talk ½ hour talk ½ hour talk	Welcome party
Friday, September 1	1 hour invited talk ½ hour talk	Free program	Hungarian dinner with wine tasting
Saturday, September 2	Scientific program	Scientific program	
Sunday, September 3	FULL DAY EXCURSION		
Monday, September 4	Scientific program	Scientific program	Banquet
Tuesday, September 5	Scientific program and closing ceremony		

- 3. There will be a social program for associate members organized under "IBUSZ" Direction; this will include a sightseeing tour of Budapest (half day), a visit to Lake Balaton (full day) and a historical tour (half day). Any additional trip or program desired individually by participants will be arranged by "IBUSZ".
- 4. Reservations will be made in the following hotels (the prices are per person per day, and may be subject to change). US\$

Hotel Intercontinental: single bed room with bathroom double bed room with bathroom 12–14

Hotel Budapest:	single bed room with bathroom double bed room with bathroom	15–16 8–9
Hotel Volga:	single bed room with bathroom double bed room with bathroom three bed room with bathroom	9 5 4
Hotel Sport:	single bed room with bathroom double bed room with bathroom	13–14 7–8
Hotel Szabadság:	single bed room without bathroom	5–6

- 5. Registration fee: US\$ 20.00 per participant; US\$ 10.00 per associate (children free of charge).
- 6. All those wishing to participate in this meeting, should write directly for two copies of the typed registration form. One should be returned by not later than April 10, 1972, to Dr. I. Vincze, Bolyai János Mathematical Society, Budapest V, Szabadságtér 17, Hungary. The other should be sent by the same date to IBUSZ Direction, Congress Department, Mrs. Kövesdy, RCs. 501.015, Budapest V, Felszabadulás tér 5, Hungary, together with a US\$ 20.00 hotel deposit per person.
- 7. Participants are requested to remit the registration fee to the following bank account by not later than April 10, 1972:

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Participants are also reminded to forward a cheque of US\$ 20.00 per person as a hotel deposit simultaneously with their second registration form to "IBUSZ" at the address given above.

On receipt of the registration forms, the Bolyai János Mathematical Society will provide participants with *visa* application forms.

8. Those wishing to present contributed papers should send Dr. I. Vincze a summary not longer than 1-2 typed quarto pages by April 30, 1972. It is hoped to have copies of papers by invited speakers together with these summaries available for members on their arrival at Budapest.

To ensure that your summary will be reproduced directly from your manuscript please follow these instructions:

- a) Summaries should be typed on white quarto sheets in black typescript.
- Symbols and formulae should be inscribed in black ink or typescript only.
- c) The pages of your summary should not be numbered.
- d) The title headings should be centered on the page. The title is to be typed in capital letters. The name of the author and his city of residence should be typed in lower case letters on separate lines.
- 9. Those wishing to be kept informed of details of this Meeting or requiring registration forms should write to

either: Professor J. Gani,

Department of Probability and Statistics, The University, Sheffield S3 7RH, England,

or: Dr. I. Vincze,

Bolyai János Mathematical Society, Budapest V, Szabadsag tér 17, Hungary.

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All enquiries about the *Journal*, as well as other subscriptions and orders for back numbers should be sent to the Editorial Assistant, Miss M. Hitchcock, Department of Probability and Statistics, The University, Sheffield, S3 7RH, England. The price per volume of back numbers is \$19.50, £stg. 8.00, \$A. 17.00 for Volumes 1 to 4, and \$27.00, £stg. 11.25, \$A. 24.20 from Volume 5 onwards. Cheques, money orders, etc. should be made out to *Applied Probability*; cheques on U.S., U.K. and Australian banks will be acceptable.

Notes for Contributors

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Manuscripts should be written in English or French; manuscripts in other languages may be accepted by the Editors, but will appear (subject to the author's agreement) in English or French translation in the *Journal*.

It will be of help to the Editors if the following conventions are adopted:

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Authors will receive only first proofs for correction; charges will be made for excessive alteration to these.

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CONTENTS

Volume 9

Number 1

March 1972

Research Papers	5
-----------------	---

		Research Lupers
NORMAN KAPLAN	1 1	A theorem on compositions of random probability generating functions and applications to branching processes with random en-
		vironments
J. RADCLIFFE	13	An immigration super-critical branching diffusion process
Y. S. YANG	24	On branching processes allowing immigration
JOHN P. MULLOOLY	32	Maximum likelihood estimation for sto-
		chastic rth-order reactions
S. K. SRINIVASAN AND	43	A stochastic model for polymer degradation
K. M. MEHATA		
B. LITTLEWOOD AND	54	Equilibrium distributions of polymers on
J. L. VERRALL		sites which are linearly arrayed
D. A. GRIFFITHS	65	A bivariate birth-death process which approximates to the spread of a disease involving a vector
M. S. BARTLETT	76	Physical nearest-neighbour models and non-
		linear time-series. II. Further discussion of
		approximate solutions and exact equations
JOSEPH TOMKO	87	The rate of convergence in limit theo-
		rems for service systems with finite queue
		capacity
H. EMMONS	103	The optimal admission policy to a multi-
II. Ziviliono	105	server queue with finite horizon
E. K. KYPRIANOU	117	On the quasi-stationary distributions of the
L. K. KIIKIMIOO	11,	GI/M/1 queue
P. J. BROCKWELL	129	A storage model in which the net growth-rate
1. J. BROCKWEEL	12)	is a Markov chain
A. SANTALÓ AND L. YAÑEZ	140	Averages for polygons formed by random
M. BAINIALO AND E. IMNLE	140	lines in Euclidean and hyperbolic planes
J. N. DARROCH AND	158	Exact fluctuation results for Markov-
HEATHER J. WHITFORD	100	dependent coin-tossing
CHRIS P. TSOKOS AND	169	Stochastic asymptotic exponential stability of
M. A. HAMDAN	105	stochastic integral equations
141.711.1111111111111111111111111111111		
		Short Communications
M. F. NEUTS AND	178	The infinite server queue with semi-Markov-
SHUN-ZER CHEN		ian arrivals and negative exponential services
WARD WHITT	185	Complements to heavy traffic limit theorems
		for the $GI/G/1$ queue
JAN M. CHAIKEN AND	192	An extension of Erlang's formulas which
EDWARD IGNALL		distinguishes individual servers
KRISHAN LALL ARYA	198	Study of a network of serial and non-serial
		servers with phase type service and finite
		queueing space
IZZET ŞAHİN AND	202	
OUSSAMA ACHOU		process
JOHN F. REYNOLDS	208	
JOHN F. REYNOLDS	214	Some theorems on the transient covariance
		of Markov chains
R. W. SHORROCK	219	A limit theorem for inter-record times
JÁNOS GALAMBOS	224	Characterization of certain populations by
		independence of order statistics
W. J. HENDRICKS	231	The stationary distribution of an interesting

Markov chain