List of Symbols

r	generic multi-index for multivariate array, page 3
z	generic element of \mathbb{C}^d , page 4
r	1-norm of multi-index r , page 7
\hat{r}	unitized vector representing direction determined by r , page 7
1	vector with all components equal to 1, page 10
F	generic meromorphic multivariate generating function, page 11
Р	numerator of generating function F, page 11
Q	denominator of generating function F , page 11
critical(r)	set of critical points in direction \hat{r} , page 11
contrib(r)	set of contributing points, page 11
$\Phi_{\boldsymbol{w}}(\boldsymbol{r})$	formula for the contribution from the point w to the asymp-
	totic series for a_r , page 12
$\boldsymbol{\delta}_{j}$	vector of length d with a 1 in its jth coordinate and a 0
	elsewhere, page 17
$\mathbb{C}[[z_1,\ldots,z_d]]$	ring of formal power series in $z = (z_1, \ldots, z_d)$ with com-
	plex coefficients, page 17
0	vector all of whose components equal 0, page 18
∂_k	partial derivative operator with respect to kth variable, page 18
$\mathbb{C}\{z_1,\ldots,z_d\}$	ring of germs of analytic functions, page 19
Ш	disjoint union, page 22
\mathbb{P}	probability measure, page 29
$\mathbb{C}((z))$	field of formal Laurent series, page 42
Re	real part of a complex number, page 77
Im	imaginary part of a complex number, page 77
ϕ	generic phase function of Fourier-Laplace integral, page 89
Α	generic amplitude function of Fourier–Laplace integral, page 89
$C(k, \ell)$	constants defined in terms of Gamma function, appearing
	in Fourier-Laplace integral formulae, page 90

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C^M	class of functions whose derivatives to order M are contin- uous, page 95
C^{∞}	class of functions whose derivatives of all orders exist, page 95
p	principal value of <i>k</i> th root, page 98
$T(\lambda)$	two-sided Fourier-Laplace integral, page 105
$I_{+}(\lambda)$	one-sided univariate Fourier–Laplace integral, page 110
Ai	Airy function, page 113
H	Hessian matrix of second partial derivatives, page 114
∇	gradient map, page 114
Relog	coordinatewise log modulus map, page 135
$\mathbb{C}[z, z^{-1}]$	ring of Laurent polynomials, page 135
$\mathbb{L}(z)$	space of formal Laurent expressions, page 135
amoeba	polynomial amoeba, page 141
hull	convex hull, page 142
N	Newton polytope, page 143
ν	order map. page 143
$\tan_r(B)$	geometric tangent cone to B at x , page 150
$normal_{r}(B)$	outward normal cone, dual to $\tan_r(B)$, page 150
<i>K</i> *	dual cone of K, page 150
V	singular variety of generating function, page 153
∇_{\log}	logarithmic gradient, page 159
C	amoeba contour, page 160
deg	order of vanishing of power series, page 162
$algtan_r(f)$	algebraic tangent cone of f at x , page 162
hom	homogeneous part of power series, page 162
Õ	square-free part of Q, page 182
LT	leading term with respect to monomial order, page 223
L(z)	logarithmic normal space to the stratum containing z, page 229
G	Gauss map, page 281
K	Gaussian curvature, page 281
$M(\mathcal{A})$	matroid of a hyperplane arrangement, page 311
O_p	local ring of analytic germs at p, page 320
Δ	standard (embedded) simplex, page 330
t	generic variable for simplex, page 330
$\pi\Delta$	shadow simplex, page 330
S	set of critical points for a multiple point Fourier-Laplace
	integral, page 333
$\mathbf{K}^{\boldsymbol{z}}(A)$	cone of hyperbolicity for the homogeneous polynomial A ,
$\mathbf{K}^{A,C}(\mathbf{x})$	family of cones for a homogeneous polynomial A page 240
1X (u)	ranning of cones for a noniogeneous porynomial A, page 349

$\mathbf{K}^{q,B}(\boldsymbol{z})$	family of cones when q is log-Laurent polynomial, page 350
A^*	algebraic dual to the homogeneous polynomial A, page 369
n	density of standard normal distribution, page 413
δ	coboundary map, page 475
Γ_{Ψ}	augmented lognormal matrix, page 492