## List of Symbols

| $r$ | generic multi-index for multivariate array, page 3 |
| :---: | :---: |
| $z$ | generic element of $\mathbb{C}^{d}$, page 4 |
| $\|\boldsymbol{r}\|$ | 1-norm of multi-index r, page 7 |
| $\hat{r}$ | unitized vector representing direction determined by $\boldsymbol{r}$, page 7 |
| 1 | vector with all components equal to 1 , page 10 |
| $F$ | generic meromorphic multivariate generating function, page 11 |
| $P$ | numerator of generating function $F$, page 11 |
| $Q$ | denominator of generating function $F$, page 11 |
| critical( $r$ ) | set of critical points in direction $\hat{r}$, page 11 |
| contrib(r) | set of contributing points, page 11 |
| $\Phi_{w}(\boldsymbol{r})$ | formula for the contribution from the point $\boldsymbol{w}$ to the asymptotic series for $a_{r}$, page 12 |
| $\delta_{j}$ | vector of length $d$ with a 1 in its $j$ th coordinate and a 0 elsewhere, page 17 |
| $\mathbb{C}\left[\left[z_{1}, \ldots, z_{d}\right]\right]$ | ring of formal power series in $\boldsymbol{z}=\left(z_{1}, \ldots, z_{d}\right)$ with complex coefficients, page 17 |
| 0 | vector all of whose components equal 0 , page 18 |
| $\partial_{k}$ | partial derivative operator with respect to $k$ th variable, page 18 |
| $\mathbb{C}\left\{z_{1}, \ldots, z_{d}\right\}$ | ring of germs of analytic functions, page 19 |
| $\sqcup$ | disjoint union, page 22 |
| $\mathbb{P}$ | probability measure, page 29 |
| $\mathbb{C}((z))$ | field of formal Laurent series, page 42 |
| Re | real part of a complex number, page 77 |
| Im | imaginary part of a complex number, page 77 |
| $\phi$ | generic phase function of Fourier-Laplace integral, page 89 |
| A | generic amplitude function of Fourier-Laplace integral, page 89 |
| $C(k, \ell)$ | constants defined in terms of Gamma function, appearing in Fourier-Laplace integral formulae, page 90 |


| $C^{M}$ | class of functions whose derivatives to order $M$ are continuous, page 95 |
| :---: | :---: |
| $C^{\infty}$ | class of functions whose derivatives of all orders exist, page 95 |
| $p$ | principal value of $k$ th root, page 98 |
| $\mathcal{I}(\lambda)$ | two-sided Fourier-Laplace integral, page 105 |
| $I_{+}(\lambda)$ | one-sided univariate Fourier-Laplace integral, page 110 |
| Ai | Airy function, page 113 |
| $\mathcal{H}$ | Hessian matrix of second partial derivatives, page 114 |
| $\nabla$ | gradient map, page 114 |
| Relog | coordinatewise log modulus map, page 135 |
| $\mathbb{C}\left[\boldsymbol{z}, \boldsymbol{z}^{-1}\right]$ | ring of Laurent polynomials, page 135 |
| $\mathbb{L}(\boldsymbol{z})$ | space of formal Laurent expressions, page 135 |
| amoeba | polynomial amoeba, page 141 |
| hull | convex hull, page 142 |
| N | Newton polytope, page 143 |
| $v$ | order map, page 143 |
| $\tan _{x}(B)$ | geometric tangent cone to $B$ at $\boldsymbol{x}$, page 150 |
| $\operatorname{normal}_{x}(B)$ | outward normal cone, dual to $\tan _{x}(B)$, page 150 |
| $K^{*}$ | dual cone of $K$, page 150 |
| $\mathcal{V}$ | singular variety of generating function, page 153 |
| $\nabla_{\log }$ | logarithmic gradient, page 159 |
| C | amoeba contour, page 160 |
| deg | order of vanishing of power series, page 162 |
| $\operatorname{algtan}_{x}(f)$ | algebraic tangent cone of $f$ at $\boldsymbol{x}$, page 162 |
| hom | homogeneous part of power series, page 162 |
| $\tilde{Q}$ | square-free part of $Q$, page 182 |
| LT | leading term with respect to monomial order, page 223 |
| $\mathbf{L}(z)$ | logarithmic normal space to the stratum containing $\boldsymbol{z}$, page 229 |
| $\mathcal{G}$ | Gauss map, page 281 |
| $\mathcal{K}$ | Gaussian curvature, page 281 |
| $M(\mathcal{A})$ | matroid of a hyperplane arrangement, page 311 |
| $O_{p}$ | local ring of analytic germs at $\boldsymbol{p}$, page 320 |
| $\Delta$ | standard (embedded) simplex, page 330 |
| t | generic variable for simplex, page 330 |
| $\pi \Delta$ | shadow simplex, page 330 |
| $\mathcal{S}$ | set of critical points for a multiple point Fourier-Laplace integral, page 333 |
| $\mathbf{K}^{\boldsymbol{z}}(A)$ | cone of hyperbolicity for the homogeneous polynomial $A$, page 348 |
| $\mathbf{K}^{\text {A,C }}(\boldsymbol{x})$ | family of cones for a homogeneous polynomial $A$, page 349 |


| $\mathbf{K}^{q, B}(\boldsymbol{z})$ | family of cones when $q$ is log-Laurent polynomial, page 350 |
| :--- | :--- |
| $A^{*}$ | algebraic dual to the homogeneous polynomial $A$, page 369 |
| $n$ | density of standard normal distribution, page 413 |
| $\delta$ | coboundary map, page 475 |
| $\Gamma_{\Psi}$ | augmented lognormal matrix, page 492 |

