

To the Editor of the *Mathematical Gazette*

DEAR SIR,

I am indebted to Mr. A. Kodym of Prague for pointing out that the expression for π as a continued fraction with unit numerator has been carried to 200 places by P. Pedersen (*Nordisk Matematisk Tidskrift*, Vol. 6, No. 2, 1958). In this paper it is shown that π appears to satisfy two conditions which a random number satisfies. Both the geometrical mean of the first n denominators and the n th root of the denominator of the n th convergent appear to converge (somewhat erratically) to the limiting values of the corresponding quantities for a random number.

I should like to correct the assertion in my previous letter (October 1959, p. 179) that the probability that, for a random number, an denominator is equal to r is $1/r(r+1)$. This is true only of the first denominator. Khintchine (*Compositio Math.* 3, pp. 276–285) has shown that the limit, as n tends to infinity, of the proportion of denominators which are equal to r is $\log[1 + 1/r(r+2)]/\log 2$. If we assume that 200 is a sufficiently large value of n for this to be approximately true, we obtain the following results.

<i>Denominator</i>	<i>Theoretical frequency</i>	<i>Actual frequency</i>
1	83	80
2	34	38
3	19	19
4	12	10
5	8	5
6	6	6
7	5	7
over 7	33	35

Finally, Khintchine (*Compositio Math.* 1, pp. 361–382) has shown that the arithmetic mean of the first n denominators of a random number tends asymptotically to $\log n/\log 2$. For $n = 200$ this value is 7.64. The corresponding value for π is 8.45. This agreement is quite good, since the arithmetic mean is dominated to a much greater extent than the geometric mean, by the large denominators.

Yours etc., E. J. F. PRIMROSE

To the Editor of the *Mathematical Gazette*

DEAR SIR,

Your issue of October 1959 contains two letters on the numerical properties of π . The first letter, by Misses Curphey, Kelley, and Moffat, gives a frequency count of the first 10,000 digits of π which I presume to be those computed by Mr. Felton and published in July 1957 in the *Proceedings of the Oxford Mathematical Conference*