

## **Bases of projections in Banach spaces with an appendix on non-standard analysis**

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An increasing net of continuous projections in a Banach space  $X$  is called a basis of projections for  $X$  if it converges strongly to the identity. This notion is more general than that of a Schauder basis or a Schauder decomposition and many results for these concepts are shown to hold in the more general setting. Particular attention is paid to "shrinking" and "boundedly complete" bases of projections and some new results are obtained concerning reflexivity. Existence theorems are obtained for bases of projections and also for Schauder decompositions in non-separable Banach spaces. In the appendix, W.A.J. Luxemburg's characterisation of the pre-near-standard points in the enlargement of a Banach space is generalised to locally convex linear topological spaces.

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Received 17 July 1972. Thesis submitted to the Australian National University, May 1972. Degree approved, August 1972. Supervisor: Dr R.W. Cross.