

## $\ell^p$ -NORMS OF SOME GENERALIZED HAUSDORFF MATRICES: CORRECTIONS

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The proofs of the theorems of [2] rely on the construction of a sequence satisfying certain growth conditions. Specifically, on line 7 of page 503, given an  $\eta$ ,  $0 < \eta < 1$ , one is to choose  $\varepsilon > 0$  so that

$$\sum_{n=N}^{\infty} a_n^p > (1 - \eta) \sum_{n=0}^{\infty} a_n^p, \text{ where } a_n = \frac{\lambda_1 \lambda_2 \cdots \lambda_n}{(\lambda_1 + \omega) \cdots (\lambda_n + \omega)}, \omega = \varepsilon + c/p.$$

Such a choice is possible only if  $\sum_{n=0}^{\infty} a_n^p$  diverges for  $\varepsilon = 0$ . Unfortunately condition (5) does not force the divergence of the series. Some counterexamples are  $\lambda_n = \log(n + 1)$  and  $\lambda_n = n^\delta$ ,  $0 < \delta < 1$ .

In order to repair the proof of Theorem 1 it is necessary to impose an additional growth condition on the  $\lambda_n$ . One sufficient condition is to have  $\lambda_n \geq c \left[ p \left( \exp(1/(n-1)p) - 1 \right) \right]^{-1}$ , where  $c$  is as in (5). Then, using the test of Schlomilch [1, p. 287] the series will converge for all positive  $\varepsilon$  and diverge when  $\varepsilon$  is zero.

In the statements of Theorems 1 and 2 the words *totally monotone* should be replaced by *nonnegative and nondecreasing*.

The author is indebted to Professor David Borwein for kindly pointing out the error.

### REFERENCES

1. K. Knopp, *Theory and applications of infinite series*. Black & Sons, Ltd., London, 1947.
2. B. E. Rhoades,  $\ell^p$ -norms of some generalized Hausdorff matrices, Canadian Math. Bull. 32(1989), 500–504.

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