

Application of the Rayleigh-Ritz variational technique for coronal loop oscillations

Narges Fathalian¹, Hossein Safari² and Sadollah Nasiri^{1,2}

¹Institute for Advanced Studies in Basic Sciences, P. O. Box 45195-1159, Zanjan, Iran

²Department of Physics, Zanjan University, P. O. Box 45195-313, Zanjan, Iran

Abstract. We studied the fast kink modes of a cylindrical model of coronal loops, in coronal conditions, stratified density and low- β plasma. The mode frequencies and profiles are calculated.

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1. Introduction

Several theoretical models have been developed to explore the nature and propagation of waves of coronal loops in 1-D models. Here, a Rayleigh-Ritz variational method developed for the oscillations of 2-D coronal loop model.

2. Overview

The MHD equations in the matrix representation reduces as (see e.g., Sobouti 1981 and Hasan & Sobouti 1987).

$$\mathbf{WZ} = \mathbf{SZE}, \quad (2.1)$$

where \mathbf{E} is a diagonal matrix whose elements are the eigenvalues ω_l and \mathbf{Z} is the matrix of the expansion coefficients. The elements of \mathbf{W} and \mathbf{S} are determined from the equations of motions. We adapt a Rayleigh-Ritz procedure and approximate the linear series in Eq. (2.1) by a finite number of terms, say n . The matrix blocks S_{ls} and $W_{ls}; l, s = 1, 2, 3$ become $n \times n$ matrices.

3. Results

Our numerical results show that: a) for unstratified loop, as expected, ω_n is proportional to its mode number (i.e., $\omega_n \approx n\omega_1$). b) for stratified loops, all the fundamental, first, second, and the third overtone kink ($m = 1$) frequencies increases with increasing stratified density scale height. For typical loop lengths, 100 – 400Mm, the density scale heights fall in the range of 13 – 108Mm. These results are in agreement with Verwichte *et al.* (2004), McEwan *et al.* (2006), and Safari *et al.* (2007). The application of variational method in real model of coronal loop are implementing in our group.

References

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