

# Effects of fast rotation on the wind of Luminous Blue Variables

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**Abstract.** While theoretical studies have long suggested a fast-rotating nature of Luminous Blue Variables (LBVs), observational confirmation of fast rotation was not detected until recently. Here I discuss the diagnostics that have allowed us to constrain the rotational velocity of LBVs: broadening of spectral lines and latitude-dependent variations of the wind density structure. While rotational broadening can be directly detected using high-resolution spectroscopy, long-baseline near-infrared interferometry is needed to directly measure the shape of the latitude-dependent photosphere that forms in a fast-rotating star. In addition, complex 2-D radiative transfer models need to be employed if one's goal is to constrain rotational velocities of LBVs. Here I illustrate how the above methods were able to constrain the rotational velocities of the LBVs AG Carinae, HR Carinae, and Eta Carinae.

**Keywords.** stars: rotation, stars: atmospheres, stars: emission-line, techniques: interferometric

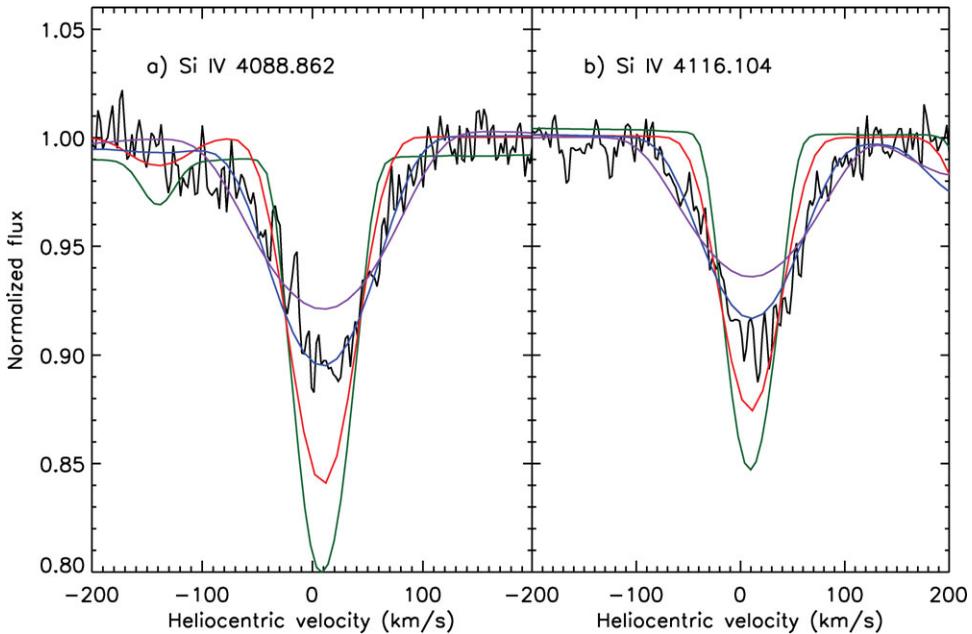
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## 1. Introduction

Tremendous advancement on understanding the evolution of massive stars has been achieved in the last decades (e. g., Maeder & Meynet 1994), in particular after the inclusion of the effects of rotation in evolutionary models (Maeder & Meynet 2000b). These models predict the existence of a short-lived, transitional stage, usually referred to as the Luminous Blue Variable (LBV) phase (Conti 1984), when the star has a high mass-loss rate ( $\dot{M} \sim 10^{-5} - 10^{-3} M_{\odot} \text{ yr}^{-1}$ ). In the current picture of stellar evolution, LBVs are rapidly evolving massive stars in the transitory phase from being an O-type star to becoming a Wolf-Rayet star (Humphreys & Davidson 1994; Meynet & Maeder 2003).

Although the effects of rotation on classical O-type stars have been documented for almost a century, their more active descendants, the Luminous Blue Variables, have eluded direct detection of fast rotation until recently, when the prototype LBV AG Carinae was found to be a fast rotator (Groh *et al.* 2006). Obtaining the rotational velocity ( $v_{\text{rot}}$ ) of LBVs is challenging because of the presence of (a) an optically-thick wind caused by the large mass-loss rate of the star and (b) time variability of the stellar radius due to the S-Dor cycle variability.

The presence of a dense wind causes the formation of an extended photosphere, making the use of a radiative transfer code mandatory to obtain information about the hydrostatic core. Time variability caused by the S-Dor cycles, characterized by changes of up to a factor of 10 in the hydrostatic radius of LBVs, imply variations of  $v_{\text{rot}}$  as a function of time. The issue is that LBVs are apparently closer to the critical rotational velocity for break-up ( $v_{\text{crit}}$ ) only during visual minimum epochs of the S-Dor cycle (Groh *et al.* 2006; Groh *et al.* 2010, in prep.). Unfortunately, LBVs spend most of their time at visual maximum, requiring continuous spectroscopic and photometric monitoring (and a great deal of patience!) to catch the star at the right time and obtain their *maximum* value of  $v_{\text{rot}}$ .



**Figure 1.** Comparison between the Si IV  $\lambda\lambda$  4088–4116 line profiles of HR Car observed on 2009 May 3rd with synthetic model spectra computed with the 2-D code from Busche & Hillier (2005) for different rotational velocities, assuming an inclination angle of  $i = 30^\circ$ :  $0 \text{ km s}^{-1}$  (green),  $75 \text{ km s}^{-1}$  (red),  $150 \text{ km s}^{-1}$  (blue), and  $200 \text{ km s}^{-1}$  (purple). From Groh *et al.* (2009a).

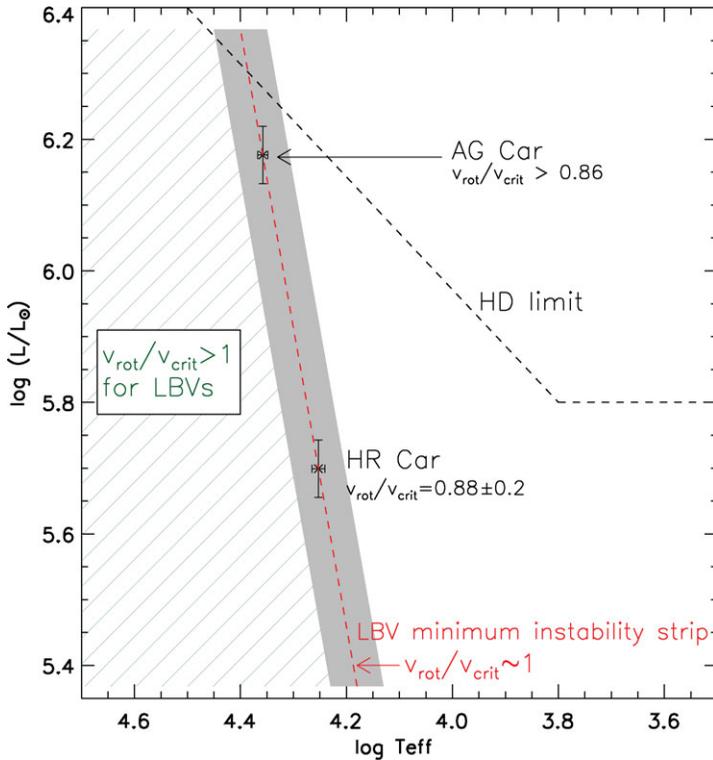
Here I discuss the diagnostics that have allowed us to constrain the rotational velocity of LBVs: broadening of spectral lines and latitude-dependent variations of the wind density structure.

## 2. Rotational broadening in LBVs

As in WR stars, the high mass-loss rate of LBVs also cause a ionization stratification of the wind, and spectral lines from ions of different ionization potentials will form at different distances  $r$  from the star. The most common lines present in the ultraviolet and optical spectra of LBVs, such as  $\text{H}\alpha$  and other Balmer lines, He I, N II, Fe II, and Si III lines, are formed at very large  $r$ . Since the azimuthal velocity component is proportional to  $r^{-1}$ , these lines do not show any evidence of rotational broadening, explaining why this phenomenon went undetected for so long.

Lines from high-ionization species, which are formed closer to the stellar photosphere, need to be observed to detect rotational broadening. Thus, in addition to observing LBVs at the right time, one has to look at the right lines. It turns out that Si IV  $\lambda\lambda$ 4088–4116 lines are the highest ionization lines present in the optical spectrum of most LBVs and, therefore, should be formed closest to the stellar photosphere and are ideal for deriving  $v_{\text{rot}}$  in LBVs.

To obtain realistic values of  $v_{\text{rot}}$ , a 2-D radiative transfer model which takes into account the dynamical effects of rotation on the wind velocity field are required. We used an updated version of the 2-D code from Busche & Hillier (2005) to constrain the rotational velocities of the LBVs AG Carinae (Groh *et al.* 2006) and HR Carinae (Groh *et al.* 2009a). Figure 1 shows the Si IV 4088 line profiles of HR Car observed during visual minimum (2009 May), compared to synthetic model spectra. Assuming an inclination angle of  $i = 30^\circ$ , we derived  $v_{\text{crit}} \simeq 170 \pm 20 \text{ km s}^{-1}$ .



**Figure 2.** HR diagram showing the position of the LBVs AG Car and HR Car during visual minimum (Groh *et al.* 2009a,b). The location of the forbidden region for strong-variable LBVs (green hatched region) and the Humphreys–Davidson limit (black dashed line, Humphreys & Davidson 1994) are shown. From Groh *et al.* (2009a).

How large is  $v_{\text{rot}}$  compared to  $v_{\text{crit}}$  for HR Car? Assuming an admittedly uncertain mass of  $M = 25 M_{\odot}$ , our CMFGEN model of HR Car predicts an Eddington parameter of  $\Gamma \simeq 0.80$ , and we can derive  $v_{\text{rot}}/v_{\text{crit}} \simeq 0.88 \pm 0.2$ . Therefore, similar to AG Car, for which we found  $v_{\text{rot}}/v_{\text{crit}} > 0.86$  (Groh *et al.* 2006), HR Car is also likely rotating very close to, if not at, its critical velocity for break-up at visual minimum.

We have proposed that rotation plays a key role in determining the location of LBVs in the HR diagram during visual minimum. Figure 2 presents the position of AG Car and HR Car in the HR diagram based on their updated stellar parameters (Groh *et al.* 2009a,b). Previous works have recognized that, during visual minimum, LBVs are located in a well-defined region of the HR diagram, the so-called “LBV minimum instability strip” (Wolf 1989; Clark *et al.* 2005). Our results suggest that the LBV minimum instability strip is considerably steeper than previously determined, being characterized by  $\log(L/L_{\odot}) = 4.54 \log(T_{\text{eff}}/\text{K}) - 13.61$  (red dashed line in Fig. 2). More importantly, we suggest that the LBV minimum instability strip corresponds to the region where critical rotation is reached for LBVs with strong S-Dor type variability. When LBVs are evolving towards maximum, the star moves away from the LBV minimum instability strip (to the right in the HR diagram), and  $v_{\text{rot}}/v_{\text{crit}}$  decreases considerably (Groh *et al.* 2006). The region in the HR diagram on the left side of the LBV minimum instability strip would be populated by unstable LBV stars with  $v_{\text{rot}}/v_{\text{crit}} > 1$ , which would make it a “forbidden region” for LBVs. Indeed, no confirmed strong-variable LBV is seen in this region (van Genderen 2001; Clark *et al.* 2005).

### 3. Latitude-dependent variations of the wind density structure

A second way of constraining  $v_{\text{rot}}$  in LBVs is by probing the latitudinal dependence of the wind density structure, which is thought to occur when rotation is significant (e. g., Owocki *et al.* 1996). If a star is surrounded by a reflection nebula with a well-determined 3-D geometry, the latitudinal variation of the wind density can in principle be probed through the reflected stellar spectrum on the nebula. This interesting technique was applied to reflected spectra in the Homunculus nebula around Eta Car, suggesting that the star possesses a faster and denser polar wind (Smith *et al.* 2003). However, such a configuration is unfortunately not seen in many LBVs, and different techniques need to be employed.

Another neat way of probing latitudinal variations of the wind is by *directly* resolving the geometry of the wind photosphere, which is most easily achieved in the K-band using near-infrared long-baseline interferometry. This technique was applied to Eta Car using observations gathered with the VINCI (van Boekel *et al.* 2003) and AMBER (Weigelt *et al.* 2007) instruments on the Very Large Telescope Interferometer from the European Southern Observatory. The interferometric measurements are consistent with an ellipsoidal shape projected on the sky. Both papers analyzed the measurements using simple geometrical models and interpreted their results as evidence for a dense prolate wind generated by fast rotation, as theoretically predicted by Owocki *et al.* (1996, 1998).

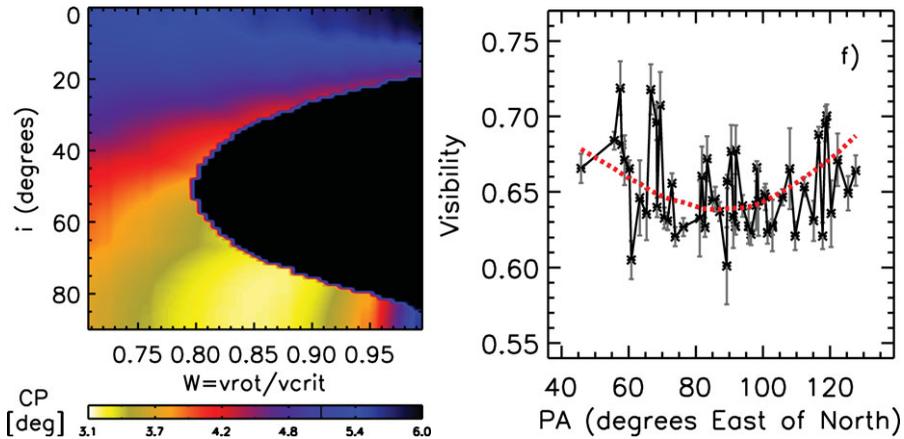
In Groh *et al.* (2010) we analyzed the published K-band continuum interferometric data of Eta Car, with the goal of constraining  $v_{\text{rot}}$  and the spatial orientation of the rotation axis of Eta Car based on the effects of rotation on the wind density structure. This ultimately determines the geometry of the K-band emitting region. We computed 2-D latitude-dependent wind models for the primary star (hereafter  $\eta_A$ ) in Eta Car using an updated version of the 2-D radiative transfer code of Busche & Hillier (2005) and via a methodology similar to that described in Groh *et al.* (2008). The reader is referred to Busche & Hillier (2005), Groh *et al.* (2006, 2008, 2009a, 2010), and Driebe *et al.* (2009) for further details on the code and its applications.

The 2-D code allows for the specification of any arbitrary latitude-dependent variation of the wind density  $\rho$  and  $v_\infty$ . For the latitudinal variation of  $\rho$ , we adopted the predictions from Owocki *et al.* (1998) for gravity-darkened (GD) line-driven prolate winds,

$$\frac{\rho(\theta)}{\rho_0} \propto \sqrt{1 - W^2 \sin^2 \theta}, \quad (3.1)$$

where  $\theta$  is the colatitude angle ( $0^\circ = \text{pole}$ ,  $90^\circ = \text{equator}$ ),  $\rho_0$  is the density at the pole, and  $W$  is the ratio of  $v_{\text{rot}}$  to its critical velocity ( $v_{\text{crit}}$ ). For consistency, we also assumed the Owocki *et al.* (1998) predictions for  $v_\infty(\theta)$ . We assumed the same parameters of  $\eta_A$  derived by Hillier *et al.* (2001): stellar temperature  $T_\star = 35,310$  K (at Rosseland optical depth  $\tau_{\text{Ross}} = 150$ ), effective temperature  $T_{\text{eff}} = 9,210$  K (at  $\tau_{\text{Ross}} = 2/3$ ), luminosity  $L_\star = 5 \times 10^6 L_\odot$ ,  $\dot{M} = 10^{-3} M_\odot \text{yr}^{-1}$ , wind terminal velocity  $v_\infty = 500 \text{ km s}^{-1}$ , a clumping volume-filling factor  $f = 0.1$ , and distance  $d = 2.3$  kpc. The atomic model and abundances are described in Hillier *et al.* (2001).

We calculated a grid of prolate models with the inclination angle  $i$  ranging from  $0^\circ$  to  $90^\circ$  in steps of  $1^\circ$ , and  $W = v_{\text{rot}}/v_{\text{crit}}$  ranging from 0 to 0.99 in steps of 0.01. For a desired position angle (PA) orientation on the sky, the K-band image, visibilities, and closure phases (CP) were computed. Figure 3 shows the reduced  $\chi^2$  values of the fit of the model predictions to the VLTI/VINCI visibilities as a function of  $W$  and  $i$ , for prolate models with PA =  $130^\circ$ . Being conservative, models with CP  $\geq 5^\circ$  are ruled out, since Weigelt *et al.* (2007) measured CP =  $0 \pm 2^\circ$ . Thus, to fit simultaneously the



**Figure 3.** *Left panel:*  $\chi^2$  values of the fit of the VINCI visibilities rejecting models with  $CP \geq 5^\circ$ , as a function of  $W$  and  $i$ , for prolate models with  $PA = 130^\circ$  *Right:* VINCI visibilities for the 24 m baseline as a function of telescope PA (connected black asterisks) compared to one of the best fit models, with  $W = 0.92$ ,  $i = 80^\circ$ , and  $PA = 108^\circ$  (red dotted line). Note that the projected baseline length of the VINCI measurements changes as a function of PA.

VLTI/VINCI visibilities and the VLTI/AMBER CPs,  $W = 0.77\text{--}0.92$  and  $i = 60^\circ\text{--}90^\circ$  are needed (Figure 3). Strikingly, this inclination is significantly higher than that of the Homunculus ( $i_{\text{Hom}} = 41^\circ$ ; Smith 2006), which has been assumed so far to align with the *current* rotation axis of  $\eta_A$ . We find that, based on the available interferometric data, if  $\eta_A$  has a prolate wind, its rotation axis is not necessarily aligned with the Homunculus polar axis.

#### 4. Short Summary and Future Prospects

Constraining the rotational velocity of LBVs is crucial for understanding how mass and angular momentum are lost during this short, unstable evolutionary phase, and how that can possibly affect the fate of a massive star. Here we have discussed the two diagnostics that have allowed us to obtain, for the first time, rotational velocities for the most famous and well-observed LBVs such as AG Car, HR Car, and Eta Car. The two diagnostics are complementary, given that rotational broadening requires observations of high-ionization lines which are usually present in the blue region of the optical spectra. Effects of rotation on the wind structure, on the other hand, can be currently probed in the near-infrared, allowing observations of obscured stars.

The comparison between the value of  $v_{\text{rot}}$  obtained using these diagnostics might allow us to verify whether the LBVs indeed have denser, faster polar winds as theoretically predicted, and to obtain inclination angles. Indeed, we are analyzing a large dataset of interferometric observations of LBVs in the near-infrared for which the determination of the rotational velocity seems promising.

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This paper would not be possible if I had not benefited from a very fruitful collaboration and continuous support from John Hillier. This work is an excellent example of a joint effort by observers and theoreticians that has characterized the massive star field in the last years, and I am more than happy to thank Augusto Damineli, Tom Madura, Stan Owocki, Gerd Weigelt, Rodolfo Barba, Eduardo Fernandez-Lajus, Roberto Gamem,

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## References

- Busche, J. R. & Hillier, D. J. 2005, *AJ*, 129, 454  
 Clark, J. S., Larionov, V. M., & Arkharov, A. 2005, *A&A*, 435, 239  
 Conti, P. S. 1984, in: A. Maeder & A. Renzini (eds.), *Observational Tests of the Stellar Evolution Theory*, IAU Symposium 105, p. 233  
 Driebe, T., Groh, J. H., Hofmann, K.-H., Ohnaka, K. *et al.* 2009, *A&A*, 507, 301  
 Groh, J. H., Damineli, A., Hillier, D. J., Barbá, R. *et al.* 2009a, *ApJ* (Letters), 705, L25  
 Groh, J. H., Hillier, D. J., & Damineli, A. 2006, *ApJ* (Letters), 638, L33  
 Groh, J. H., Hillier, D. J., Damineli, A., Whitelock, P. A. *et al.* 2009b, *ApJ*, 698, 1698  
 Groh, J. H., Madura, T. I., Owocki, S. P., Hillier, D. J. *et al.* 2010, *ApJ* (Letters), 716, L223  
 Groh, J. H., Oliveira, A. S., & Steiner, J. E. 2008, *A&A*, 485, 245  
 Hillier, D. J., Davidson, K., Ishibashi, K., & Gull, T. 2001, *ApJ*, 553, 837  
 Humphreys, R. M. & Davidson, K. 1994, *PASP*, 106, 1025  
 Maeder, A. & Meynet, G. 1994, *A&A*, 287, 803  
 Maeder, A. & Meynet, G. 2000a, *A&A*, 361, 159  
 Maeder, A. & Meynet, G. 2000b, *ARAA*, 38, 143  
 Meynet, G. & Maeder, A. 2003, *A&A*, 404, 975  
 Owocki, S. P., Cranmer, S. R., & Gayley, K. G. 1996, *ApJ* (Letters), 472, L115  
 Owocki, S. P., Cranmer, S. R., & Gayley, K. G. 1998, *Ap&SS*, 260, 149  
 Smith, N. 2006, *ApJ*, 644, 1151  
 Smith, N., Davidson, K., Gull, T. R., Ishibashi, K. *et al.* 2003, *ApJ*, 586, 432  
 van Boekel, R., Kervella, P., Schöller, M., Herbst, T. *et al.* 2003, *A&A*, 410, L37  
 van Genderen, A. M. 2001, *A&A*, 366, 508  
 Weigelt, G., Kraus, S., Driebe, T., Petrov, R. G. *et al.* 2007, *A&A*, 464, 87  
 Wolf, B. 1989, *A&A*, 217, 87

## Discussion

MEYNET: I have a question regarding the HR diagram where the forbidden region is in the left of the LBV minimum instability strip. I would imagine that the star evolves from the blue to red, encounters the instability, suffers strong mass loss which brings the stars to the right because of the optical thickness of the wind.

GROH: The optical thickness of the wind is included in our calculations for the positions of the LBVs in the HR diagram. Apparently, the stars are very close to the Eddington limit modified by rotation at the LBV minimum instability strip, but in the case of AG Car and HR Car we do not see a runaway increase in mass loss, which is actually comparable to other LBVs. That is related to the very important issue of how much rotation increases the mass-loss rate and certainly deserves future studies.

PULS: 1. You referred to the critical velocity for break-up. Since you are dealing with LBVs ( $\Gamma$  close to unity), did you include the effects of the Eddington limit modified by rotation ( $\Omega\Gamma$  limit)? 2. Which kind of models are underlying your analysis?

GROH: First, yes, we include the effects of rotation on the Eddington limit following Maeder & Meynet (2000a). In these analyses we have used an updated version of the 2-D code from Busche & Hillier (2005) using a prescribed latitudinal variation of the wind density as a function of  $v_{\text{rot}}$  as in Owocki *et al.* (1996).