

## Comparison of Nutation Theories

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**Abstract.** Analyses of residuals between VLBI observations and combinations of nutation series show that the MHB 2000 nonrigid-Earth nutation model applied to the REN 2000 rigid-Earth model results in the best fit, and that amplitudes of any possible periodic terms remaining in the observed corrections to the MHB2000 theory could be expected to be less than 0.1 mas.

### 1. Introduction

The IAU/IUGG Working Group on Nonrigid-Earth Nutation in its report (Dehant 2000) describes both rigid-Earth and non rigid-Earth nutation theories that have been developed in recent years. To evaluate these theories for possible acceptance by the international community it is necessary to compare them with observations. This paper presents the results of the comparison of combinations of rigid and nonrigid-Earth nutation theories to recent high-precision astronomical observations.

### 2. Observations

Observations of corrections to the IAU Precession/Nutation Theory are provided by very long baseline interferometry (VLBI). For the purpose of this comparison the series derived by the National Earth Orientation Service (NEOS) was used. The series of data begins with MJD 44090 (1979) and ends with MJD 51618 (2000). Some VLBI observing sessions that were designed primarily to determine motions of observing sites produced poor results in precession/nutation. The results from these sessions were not used in this comparison.

### 3. Nutation Theories

The theories used in the comparison are (1) MHB2000 (Mathews et al. 2000, see also Mathews 2000) applied to the REN 2000 rigid-Earth theory (Souhay et al. 1999), (2) MHB2000 applied to the SMART97 rigid-Earth theory (Bretagnon et al. 1997, 1998), (3) MHB2000 applied to RDAN97 rigid-Earth theory (Roosbeek and Dehant 1998), (4) SF2000 (Shirai and Fukushima 2000a,b), (5) FG2000 (Getino and Ferrándiz 2000). MHB2000 provides a transfer function to be applied to a rigid-Earth theory of nutation to derive a nonrigid-Earth theory. The FG2000 model uses a global Hamiltonian approach for 106 waves fit to

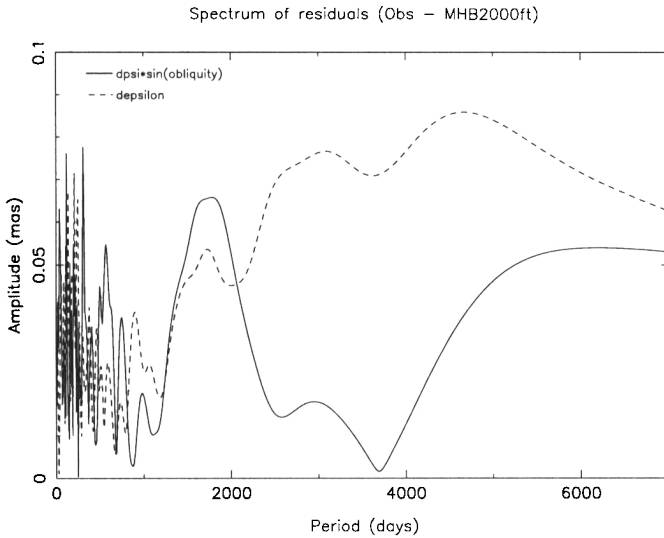


Figure 1.

VLBI data, and the SF2000 is an empirical model, based on a resonance formula fit to VLBI observations.

#### 4. Comparison of Theories with Observations

In comparing theories with observations a time series of residuals was formed by subtracting the theoretical corrections from the observations. Each of these time series was then fit with a straight line to evaluate the rate and bias at the epoch of J2000.0. These values and the rms of each fit is shown in Table 1 for both the obliquity and the longitude of the ascending node of the ecliptic.

#### 5. Discussion

The table shows that the MHB2000 theory applied to the REN 2000 rigid-Earth theory represents a marginal improvement over any of the others. All differences are statistically significant at the 99% level. Figure 1 shows an amplitude spectrum of the residual differences between the observations and the MHB2000 theory applied to REN 2000. Amplitudes of any possible periodic terms appear from this figure to be under 0.1 mas.

#### 6. Conclusion

From this analysis of the residuals between the VLBI observations and the combinations of nutation theories, it appears that the MHB 2000 nonrigid-Earth nutation model applied to the REN 2000 Rigid-Earth model results in the best fit and that amplitudes of any possible periodic terms remaining in the observed corrections to this theory could be expected to be less than 0.1 mas.

Table 1. Comparison of Precession/Nutation Models

Nonrigid Model	Rigid Model	FCN Model	Bias	Error	Rate	$\psi$	Error	WRMS	Bias	Error	Rate	$\epsilon$	Error	WRMS
IERS96		KSV	0.304	0.016	-1.38	0.27	0.470	0.026	0.007	-0.68	0.11	0.193		
MHB2000 (ORB)	SK97		-0.553	0.020	-6.22	0.33	0.575	-0.073	0.008	-1.62	0.13	0.227		
	SK97	KSV	-0.544	0.018	-6.02	0.31	0.530	-0.070	0.007	-1.61	0.12	0.211		
	SK97	MHB2000	-0.545	0.019	-6.09	0.31	0.535	-0.070	0.007	-1.59	0.12	0.205		
MHB2000 (ORB)	RDAN97		-0.569	0.020	-5.79	0.33	0.578	-0.061	0.008	-1.05	0.13	0.227		
	RDAN97	KSV	-0.569	0.019	-5.59	0.31	0.532	-0.058	0.007	-1.03	0.12	0.211		
	RDAN97	MHB2000	-0.569	0.019	-5.66	0.31	0.536	-0.057	0.007	-1.01	0.12	0.205		
MHB2000 (ORB)	BR97		-0.607	0.020	-5.38	0.33	0.577	-0.022	0.008	-1.10	0.13	0.226		
	BR97	KSV	-0.597	0.018	-5.18	0.31	0.532	-0.019	0.007	-1.08	0.12	0.210		
	BR97	MHB2000	-0.598	0.019	-5.26	0.31	0.537	-0.019	0.007	-1.06	0.12	0.204		
Shirai& Fukushima	RDAN97	Shirai& Fukushima	-0.174	0.018	-3.29	0.30	0.525	0.113	0.008	1.16	0.13	0.219		
	RDAN97	KSV	-0.170	0.018	-3.17	0.30	0.516	0.113	0.008	1.18	0.13	0.219		
	RDAN97	MHB2000	-0.172	0.018	-3.24	0.30	0.524	0.114	0.007	1.20	0.12	0.212		
Getino& Ferrándiz		MHB2000	-0.035	0.017	-2.31	0.28	0.477	0.348	0.007	-4.43	0.11	0.195		
MHB2000	SMART		-1.129	0.019	28.72	0.32	0.557	38.721	0.008	-4.67	0.13	0.225		
MHB2000	SMART	MHB2000	-1.120	0.018	28.85	0.30	0.512	38.725	0.007	-4.64	0.12	0.202		
MHB2000 (MIT)	SK97		1.395	0.016	0.12	0.26	0.456	-1.816	0.006	-0.04	0.11	0.183		
MHB2000 (FT)(MIT)	SK97	MHB2000	1.541	0.016	2.34	0.26	0.444	-1.677	0.006	2.13	0.10	0.181		
MHB2000 (USNO)	SK97		1.035	0.016	1.37	0.27	0.472	-0.718	0.006	-0.68	0.11	0.189		
	SK97	MHB2000	1.035	0.016	1.29	0.27	0.464	-0.718	0.006	-0.66	0.10	0.186		

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