



PROBLEMS FOR SOLUTION

P. 159. Let  $M$  be a metric space,  $M_0$  a compact subset and  $T: M \rightarrow M$  an isometry. Then if  $TM_0 \subset M_0$  or  $TM_0 \supset M_0$  we have  $TM_0 = M_0$ .

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P. 160. Higman [Quart. J. Math. Oxford 10 (1959), 165-178] proves that a group satisfies the identical relation  $[[x, y], [x, y^{-1}]] = 1$  if and only if all its two-generator subgroups are metabelian. Prove that the same conclusion holds for the relation  $[[x, y], [x^{-1}, y^{-1}]] = 1$ .

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P. 161. For any positive integer  $n$  and any  $n$  numbers  $c_1, \dots, c_n$ , let further numbers  $c_{n+1}, c_{n+2}, \dots$  be defined as continued fractions

$$c_{n+1} = 1 - c_n/1 - c_{n-1}/1 - \dots - c_2/1 - c_1,$$

$$c_{n+2} = 1 - c_{n+1}/1 - c_n/1 - \dots - c_3/1 - c_2,$$

and so on. Prove that the sequence  $c_i$  is periodic with period  $n + 3$ ; that is,  $c_{n+4} = c_1, c_{n+5} = c_2$ , and so on.

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SOLUTIONS

P. 149. Find all solutions, other than the trivial solution  $(a, b, c) = (1, 1, c)$  of the simultaneous congruences:

$ab \equiv 1 \pmod c, bc \equiv 1 \pmod a, ca \equiv 1 \pmod b$  where  $a, b, c$  are positive integers with  $a \leq b \leq c$ .

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