

In Fig. 2(b), which is the case of the hyperbola,  
 $\angle ACD$  is supplementary to  $\angle RP_1P_2$ ,  
 and  $\angle BCD = \angle RP_2P_1 = \angle RP_1P_2$ .

Therefore angles  $ACD$  and  $BCD$  are supplementary.

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**Note on Geometric Series.**—The formula for the sum of  $n$  terms of the geometric series

$$a + ar + ar^2 + \dots + ar^{n-1},$$

viz.  $s = \frac{a(r^n - 1)}{r - 1}$ , may be written  $s = \frac{T_{n+1} - T_1}{r - 1}$ ,

where  $T_1$  is the first term and  $T_{n+1}$  the term immediately succeeding the last to be summed. This form is useful for finding the sum of a closed geometric series without first finding the number of terms. Thus

$$\frac{1}{8} + \frac{1}{4} + \frac{1}{2} + \dots + 32 = \frac{64 - 1/8}{2 - 1},$$

and  $a^{-5} + a^{-3} + a^{-1} + \dots + a^{19} = \frac{a^{21} - a^{-5}}{a^2 - 1}$ ,

since the terms of the series which succeed  $32$  and  $a^{19}$  are respectively  $64$  and  $a^{21}$ .

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**Distance of the Horizon.**—The approximate rules given in this note may perhaps be new to some readers.

If an observer be at a height  $h$  above the Earth's surface, the distance of the horizon as seen by him is given by the formula

$$d = \sqrt{2rh},$$

where  $r$  is the radius of the Earth.

If  $h$  is given in feet, then

$$\sqrt{\left(\frac{h}{5280} \times 8000\right)}$$

will give  $d$  in miles.

Now  $\frac{8000}{5280} = \frac{100}{66} = \frac{5}{3}$ , nearly.