# STELLAR PULSATION: (II) MULTIPLE DISTINCT SHELLS 

YU ZHI-YAO<br>Shanghai Obstrvatory, 80 Nandan Road, Shanghai 200030, China


#### Abstract

We can find the conclusion with our analysis for $\bigvee \mathrm{LA}$ observation of OH maser and $C O$ (2-1) emission line that they are distributed on some different distinct shells in the circumstellar envelope, respectively.


For an expanding spherical envelope the angular radius $R_{0}^{A}$ is given by

$$
\begin{equation*}
R_{0}^{A}=R^{A}(V)\left[1-\frac{\left(V-V_{0}\right)^{2}}{V_{e}^{2}}\right]^{-\frac{1}{2}} \tag{1}
\end{equation*}
$$

where $R^{A}(V)$ is the angular radius at LSR velocity $V, V_{0}$ is systemic radial velocity, $V_{\mathrm{e}}$ is circumstellar expanding velocity (Bowers et al. 1983). Formula (1) is changed as following

$$
\begin{equation*}
\left[R^{A}(V)\right]^{2}=\left[R_{0}^{A}\right]^{2}-\left[\frac{R_{0}^{A}}{V_{e}}\right]^{2}\left(V-V_{0}\right)^{2} \tag{2}
\end{equation*}
$$

We may see from formula (2), a shell has determinate $R_{0}^{A}$ and $V_{\mathrm{e}}$ for each shells, $\left[R^{A}(V)\right]^{2}$ is linear monotonous decrease by degrees function of $\left(V-V_{0}\right)^{2}$. Thus we may divide the envelope into shells according to these regions where the distribution of points, which coordinates are $\left[R^{A}(V)\right]^{2}$, $\left(V-V_{0}\right)^{2}$, is ranged by the orientation of linear monotonous decrease by degrees in $\left[R^{A}(V)\right]^{2}-\left(V-V_{0}\right)^{2}$ map, then do statistic fitting. The error of statistic fitting is least.

The data of VY CMa selected by the paper are from Bowers et al. (1983). We have obtained that VY CMa OH 1612 MHz masers occur on three distinct expanding shells (i.e. shell A, B, and C), their corresponding angular radii $\left[R_{0}^{A}\right]$ and expanding velocities $\left[V_{\mathrm{e}}\right]$ are $2.43,3.08,3.21$ arcsec and 24.0 , $30.4,34.9 \mathrm{~km} \mathrm{~s}^{-1}$, respectively. Given $R_{0}^{A}$, the linear radius $R_{0}$ can be determined if the distance is known. The distributions of VY CMa OH 1612 MHz points are seen from Fig. 1, 2, and 3.

We have also obtained the multiple expanding shells at the analysis and explanation of the CO (2-1) emission line. For an expanding spherical envelope parabola is adaptable (Knapp 1982). Therefore we may obtain

$$
\begin{equation*}
T_{A}^{\star}(V)=T_{A}^{\star}(\text { peak })\left[1-\frac{\left(V-V_{0}\right)^{2}}{V_{\mathrm{e}}^{2}}\right] \tag{3}
\end{equation*}
$$



Fig. 1. The Distribution on Shell A


Fig. 2. The Distribution on Shell B
where $T_{A}^{*}$ (peak) is the antenna temperature of peak. $T_{A}^{\star}(V)$ is the antenna temperature at $V$. We take some points at the $C O(2-1)$ emission line ( 27 points for CIT6). We measure a group of $T_{A}^{*}(V), V$ for each point, farther some groups of $\left(V-V_{0}\right)^{2}, T_{A}^{*}(V)$. We draw $T_{A}^{*}(V)-\left(V-V_{0}\right)^{2}$ map. We find that these points, which coordinates are $T_{A}^{*}(V)$ and $\left(V-V_{0}\right)^{2}$, are distributed at several regions from the $T_{A}^{*}(V)-\left(V-V_{0}\right)^{2} \operatorname{map}$ (three regions for CIT6). At each region the distribution of the points is ranged by the orientation of linear monotonous decrease by degrees. According to formula (3) we may obtain


Fig. 3. The Distribution on Shell C


Fig. 4. The Distribution on Shell D

$$
\begin{equation*}
T_{A}^{*}(V)=T_{A}^{*}(\text { peak })-\frac{T_{A}^{*}(\text { peak })}{V_{\mathrm{e}}^{2}}\left(V-V_{0}\right)^{2} . \tag{4}
\end{equation*}
$$

For a shell which radial distance from stellar center is $r$, and expanding velocity is $V_{\mathrm{e}}, T_{A}^{*}$ (peak) and $V_{\mathrm{e}}$ are determinate. $T_{A}^{*}(V)$ is linear monotonous decrease by degrees function of $\left(V-V_{0}\right)^{2}$. Using $T_{A}^{*}(V)-\left(V-V_{0}\right)^{2}$ map and formula (4) we divide the envelope into shells according to the regions in $T_{A}^{*}(V)-\left(V-V_{0}\right)^{2}$ map where the distribution of points is ranged by the orientation of linear monotonous decrease by degrees.

The observational data are selected from Knapp (1982). We have obtained that CIT6 CO (2-1) molecules also occur on three distinct expanding shells


Fig. 5. The Distribution on Shell E


Fig. 6. The Distribution on Shell F
i.e. shell $\mathrm{D}, \mathrm{E}$, and F ), the corresponding peak antenna temperature $\left[T_{A}^{*}\right.$ (peak)] and expanding velocity $\left[V_{\mathrm{e}}\right]$ are $3.1,3.8,4.5 \mathrm{~K}$ and $12.7,15.2,17.4$ $\mathrm{km} \mathrm{s}^{-1}$, respectively. The distributions of the points of shell $\mathrm{D}, \mathrm{E}$, and F are seen from Fig. 4, 5, and 6, respectively.

## References

Bowers, P. F. et al.: 1983, Astrophysical Journal 274, 733.
Knapp, G. R. et al.: 1982, Astrophysical Journal 252, 616.

