## THE

## JOURNAL

## OF

# SYMBOLIC LOGIC

#### EDITED BY

Alonzo Church Burton S. Dreben Azriel Lévy Anil Nerode ARTHUR N. PRIOR GERALD E. SACKS

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