THE

JOURNAL

OF

SYMBOLIC LOGIC

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VOLUME 19

NUMBER 4

DECEMBER 1954

Published quarterly by the Association for Symbolic Logic, Inc.

WITH THE AID OF SUBVENTIONS FROM

EDWARD C. HEGELER TRUST FUND

HARVARD UNIVERSITY
INSTITUTE FOR ADVANCED STUDY

RUTGERS UNIVERSITY
SMITH COLLEGE

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The Journal of Symbolic Locic is the official organ of the Association for Symbolic Logic, Inc., published quarterly, in the months of March, June, September, and December. The Journal is published for the Association by N.V. Erven P. Noordhoff, Publishers, Groningen, The Netherlands. The subscription price is five dollars annually, for current subscriptions. New subscriptions must begin with the first number of the current volume, as determined by the date of receipt of the subscription. Completed volumes are sold at six dollars. Members of the Association of three years standing may purchase back volumes of the Journal at reduced rates for their personal use (except volume 1).

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Attention is called to the fact that the Journal invites submission of (1) original technical papers in the field of symbolic logic, (2) expository papers in this field, (3) philosophical papers which bear upon this field or make use of its methods, and (4) studies in the history of logic in which modern technical developments are taken into account.

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