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A skew-Hadamard matrix of order 92 Jennifer Wallis

There is a skew-Hadamard matrix of order 92 .

Previously the smallest order for which a skew-Hadamard matrix was not known was 92. We construct such a matrix below. The orders < 200 which are now undecided are 100, 116, 148, 156, 172, 188, 196; see [2], [3]. The existence of any Hadamard matrix of order 92 was unknown until 1962 [1].

We construct a skew-Hadamard matrix of Williamson-type by using the matrix

$$W = A \quad B \quad C \quad D$$
$$-B \quad A \quad D \quad -C$$
$$-C \quad -D \quad A \quad B$$
$$-D \quad C \quad -B \quad A \quad .$$

Then if A is a (1, -1) skew-type cyclic matrix of order 23 (that is $a_{i+1,j+1} = a_{i,j}$ where the subscripts are taken modulo 23), B, C, D are (1, -1) anticyclic matrices of order 23 having symmetrical first rows (that is $b_{i,j} = b_{i+1,j-1}$, $b_{11} = 1$, $b_{1j} = b_{1,25-j}$ and so on, subscripts modulo 23) and

$$AA^{T} + BB^{T} + CC^{T} + DD^{T} = 92I_{23}$$
,

W is a skew-Hadamard matrix of order 92.

Suitable first rows for the blocks A, B, C, D are

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If W = U + I is a skew-Hadamard matrix of order 92 where I is the identity matrix then

is a skew-Hadamard matrix of order 184 .

References

- [1] Leonard Baumert, S.W. Golomb and Marshall Hall, Jr, "Discovery of an Hadamard matrix of order 92", Bull. Amer. Math. Soc. 68 (1962), 237-238.
- [2] Jennifer Wallis, " (v, k, λ) configurations and Hadamard matrices", J. Austral. Math. Soc. 11 (1970), 297-309.
- [3] Albert Leon Whiteman, "An infinite family of skew Hadamard matrices", (to appear).

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