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# A skew-Hadamard matrix of order 92 Jennifer Wallis 

There is a skew-Hadamard matrix of order 92 .

Previously the smallest order for which a skew-Hadamard matrix was not known was 92 . We construct such a matrix below. The orders < 200 which are now undecided are $100,116,148,156,172,188,196$; see [2], [3]. The existence of any Hadamard matrix of order 92 was unknown until 1962 [1].

We construct a skew-Hadamard matrix of Williamson-type by using the matrix

$$
W=\begin{array}{rrrr}
A & B & C & D \\
-B & A & D & -C \\
-C & -D & A & B \\
-D & C & -B & A .
\end{array}
$$

Then if $A$ is a (1, -1) skew-type cyclic matrix of order 23 (that is $a_{i+1, j+1}=a_{i, j}$ where the subscripts are taken modulo 23), $B, C, D$ are ( $1,-1$ ) anticyclic matrices of order 23 having symmetrical first rows (that is $b_{i, j}=b_{i+1, j-1}, b_{11}=1, b_{1 j}=b_{1,25-j}$ and so on, subscripts modulo 23) and

$$
A A^{T}+B B^{T}+C C^{T}+D D^{T}=92 I_{23}
$$

$W$ is a skew-Hadamard matrix of order 92 .
Suitable first rows for the blocks $A, B, C, D$ are

| $A$ | $:$ | 1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | 1 | -1 | 1 | -1 | 1 | -1 | -1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $B$ | $:$ | 1 | 1 | -1 | -1 | 1 | -1 | -1 | 1 | 1 | 1 | 1 | -1 | -1 | 1 | 1 | 1 | 1 | -1 | -1 | 1 | -1 | -1 | 1 |
| $C$ | $:$ | 1 | 1 | -1 | -1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | -1 | -1 | 1 |
| $D$ | $:$ | 1 | -1 | -1 | -1 | -1 | 1 | -1 | -1 | 1 | -1 | -1 | 1 | 1 | -1 | -1 | 1 | -1 | -1 | 1 | -1 | -1 | -1 | -1 |

If $W=U+I$ is a skew-Hadamard matrix of order 92 where $I$ is the identity matrix then

$$
\begin{array}{cc}
U+I & U+I \\
U-I & -U+I
\end{array}
$$

is a skew-Hadamard matrix of order 184 .

## References

[1] Leonard Baumert, S.W. Golomb and Marshall Hall, Jr, "Discovery of an Hadamard matrix of order 92", Bull. Amer. Math. Soc. 68 (1962), 237-238.
[2] Jennifer Wallis, " $(v, k, \lambda)$ configurations and Hadamard matrices", J. Austral. Math. Soc. 11 (1970), 297-309.
[3] Albert Leon Whiteman, "An infinite family of skew Hadamard matrices", (to appear).

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