



# Are Odd Radio Circles phoenixes of powerful radio galaxies?

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# Abstract

Odd Radio Circles (ORCs) are a class of low surface brightness, circular objects approximately one arcminute in diameter. ORCs were recently discovered in the Australian Square Kilometre Array Pathfinder (ASKAP) data and subsequently confirmed with follow-up observations on other instruments, yet their origins remain uncertain. In this paper, we suggest that ORCs could be remnant lobes of powerful radio galaxies, re-energised by the passage of a shock. Using relativistic hydrodynamic simulations with synchrotron emission calculated in post-processing, we show that buoyant evolution of remnant radio lobes is alone too slow to produce the observed ORC morphology. However, the passage of a shock can produce both filled and edge-brightnened ORC-like morphologies for a wide variety of shock and observing orientations. Circular ORCs are predicted to have host galaxies near the geometric centre of the radio emission, consistent with observations of these objects. Significantly offset hosts are possible for elliptical ORCs, potentially causing challenges for accurate host galaxy identification. Observed ORC number counts are broadly consistent with a paradigm in which moderately powerful radio galaxies are their progenitors.

Keywords: Galaxies: active; radio continuum: galaxies; hydrodynamics; galaxies: jets

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# 1. Introduction

Odd Radio Circles (ORCs) are circles of low surface brightness radio continuum emission, first discovered in the Australian Square Kilometre Array Pathfinder (ASKAP) telescope Evolutionary Map of the Universe (EMU) pilot survey data. Eight of these rings or edge-brightened discs have so far been found in the 800-1 088 MHz ASKAP data (Norris et al. 2021c, 2022; Koribalski et al. 2021; Filipović et al. 2022; Gupta et al. 2022). ORCs are characterised by low surface brightness  $(100 - 300 \,\mu\text{Jy beam}^{-1}; \text{ ASKAP rms sensitivity is } \sim 30 \,\mu\text{Jy}$ beam<sup>-1</sup>), edge-brightened rings approximately 60-80 arcsec in diameter. Several ORC detections have been confirmed at both longer wavelengths (325 MHz continuum with the Giant Meterwave Radio Telescope, GMRT) and higher resolution (MeerKAT); and discovered with other instruments (Lochner et al. 2023; Koribalski et al. 2023). The best-studied ORC, dubbed ORC1 (Norris et al. 2021c, 2022) shows a narrow ring of emission unresolved by the ASKAP  $11^{\prime\prime} \times 13^{\prime\prime}$  Full Width at Half Maximum (FWHM) beam; the ring is marginally resolved by MeerKAT's 6" beam (Norris et al. 2022). It shows a remarkably uniform

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spectral index<sup>a</sup>  $\alpha \sim 1.1$  between 800 and 1 400 MHz, with hints of filamentary structure across the ring (Norris et al. 2022).

No electromagnetic counterparts to ORCs have so far been found at other wavelengths. Four 'single ORCs' (ORC1 and ORC4, Norris et al. 2021c; ORC5, Koribalski et al. 2021; SAURON, Lochner et al. 2023) have candidate elliptical host galaxies colocated in projection at the ORC's geometric centre, with photometric redshifts in the range 0.27–0.55; both ORC1 and ORC5 also have galaxies coincident in projection with the ring structure. ORCs 2 and 3, on the other hand, do not appear to have a central candidate host galaxy; however, these two ORCs are in close proximity to each other on the sky and could be part of the same structure (Norris et al. 2021c). Koribalski et al. (2023) have recently reported discovery of a single ORC without a clear central host in MeerKAT data. In addition to single ORCs and ORCs with companion lobes, several ORC candidates have also been found (Gupta et al. 2022).

The origin of ORCs is, at present, a mystery. Several hypotheses have been put forward to explain these, including jet-inflated lobes, black hole mergers (Norris et al. 2022), starburst-driven shocks (Coil et al. 2023), tidal disruption events (Omar 2022), precessing AGN jets (Nolting, Ball, & Nguyen 2023), merger shocks (Dolag et al. 2023), and even supernova remnants (Filipović et al. 2022). Indeed, there may be more than one explanation for this

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<sup>&</sup>lt;sup>a</sup>We adopt the convention  $S_{\nu} \propto \nu^{-\alpha}$  throughout the paper.

morphological class. If ORCs are extragalactic at redshifts suggested by their candidate host galaxies, a very large injection of energy is required to inflate ORCs to their implied sizes of several hundred kiloparsecs. Dolag et al. (2023) recently presented a detailed numerical model suggesting that shock acceleration from galaxy – galaxy mergers can produce radio sizes and morphologies similar to the observed ORCs. Supermassive black holes at galaxy centres are another obvious candidate for providing this large amount of energy. The association of radio galaxy lobes with some ORCs suggests that jets may play a role in this process.

Relativistic jets emanating from Active Galactic Nuclei (AGN) at galaxy centres are a key component in regulating the baryon cycle within and outside galaxies. These jets are found in systems with short cooling times (Mittal et al. 2009), and estimates of their energetics suggest a balance between gas cooling and jet heating (Best et al. 2005; Kaiser & Best 2007; Shabala et al. 2008; Turner & Shabala 2015; Hardcastle et al. 2019; Kondapally et al. 2023). This 'maintenance' mode of AGN feedback keeps circumgalactic and intracluster gas - which would otherwise cool rapidly - hot, and explains the largely quiescent star formation histories of massive ellipticals over the past several Gyr (Croton et al. 2006; Shabala & Alexander 2009a; Fanidakis et al. 2011; Raouf et al. 2017; Weinberger et al. 2017; Thomas et al. 2021). In this 'thermostat' paradigm of jet feedback, the jet duty cycle is in part determined by jet feedback (Kaiser & Best 2007; Pope, Mendel, & Shabala 2012). Observations of radio galaxies with multiple pairs of lobes (so-called Double-Double Radio Galaxies, e.g. Schoenmakers et al. 2000; Steenbrugge, Heywood, & Blundell 2010; Konar & Hardcastle 2013; Mahatma et al. 2018; Jurlin et al. 2020) provide dramatic observational evidence of jet intermittency; Bruni et al. (2019) recently showed that a high fraction of Giant Radio Galaxies may show intermittent jet activity. Recent observations of populations of active, remnant and re-started radio jets (Jurlin et al. 2020) and detailed modelling of their dynamics and synchrotron emission (Shabala et al. 2020) suggest that Chaotic Cold Accretion (Gaspari, Ruszkowski, & Oh 2013; McKinley et al. 2022) is a mechanism which can naturally facilitate intermittent black hole accretion and jet activity. Remnant radio lobes are therefore expected to be ubiquitous, especially in environments with a high jet duty cycle such as cool core clusters. Re-acceleration of cosmic ray electrons within the remnant lobes is thought to be responsible for much diffuse radio emission in clusters, including radio relics and radio haloes (see the Brunetti & Jones 2014 review and references therein). In this paper, we examine whether remnant AGN lobes are plausible progenitors of ORCs.

Churazov et al. (2001, see also Brüggen & Kaiser 2002) modelled the morphological evolution of remnant radio lobes rising buoyantly through a cluster atmosphere. These authors showed that the remnant lobes undergo significant morphological evolution in the buoyant phase: ambient gas is uplifted by the radio lobes through the central channel, and subsequent adiabatic expansion pushes the remnant plasma away from the axis of symmetry; this causes a characteristic 'mushroom' shape, followed eventually by a torus. Viewed close to end-on, such a torus would produce a ring morphology similar to an ORC.

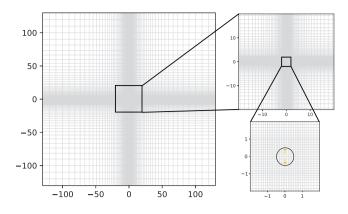
This scenario, however, cannot explain the existence of ORCs: as we show in Section 3.1 (see also Kaiser & Cotter 2002; Godfrey, Morganti, & Brienza 2017; Turner 2018; Hardcastle 2018; Yates, Shabala, & Krause 2018; English, Hardcastle, & Krause 2019; Shabala et al. 2020), once the jets cease to supply energy to the lobes, remnant lobes fade extremely quickly. This situation is exacerbated for extremely large lobes such as those implied by ORCs at non-negligible redshifts, due to the unavoidable inverse Compton losses. As pointed out by O'Neill et al. (2019) and Nolting et al. (2019), the dynamical behaviour of jet-inflated remnant lobes is more complex than that of bubbles in a cluster atmosphere: remnant lobes inflated by powerful jets will spend a considerable amount of time expanding supersonically through the ambient gas (and rapidly fading) before transitioning to the buoyant phase. Hence the remnant lobes will fade below any realistic detection limit much faster than the dynamical time required to transform dynamically into a torus.

Enßlin & Brüggen (2002) showed that passage of a shock through a fossil radio bubble, placed 'by hand' into the simulation, can produce radio emission with a toroidal morphology. This important result can be understood as follows. As the shock propagates through the cluster gas, the post-shock thermal pressure is balanced by the ram pressure (and a small component of thermal pressure) in the pre-shock gas. As the shock first makes contact with the radio bubble, however, the post-shock thermal pressure now exceeds the pre-shock ram pressure (plus thermal pressure) in the underdense bubble, facilitating rapid expansion through the bubble and formation of a torus. O'Neill et al. (2019) and Nolting et al. (2019) extended this pioneering analysis to more realistic, jetinflated remnants, and confirmed that toroidal structures can form in these situations. ZuHone et al. (2021) confirmed that the cosmic ray electrons will form toroidal structures when compressed by a shock in a more realistic cluster merger scenario.

While this is promising, the large sizes of ORCs, if these are extragalactic, pose several challenges to the torus hypothesis. To reach transverse sizes of several hundred kpc, ORCs must be inflated by radio sources with similarly large sizes at switch-off. To remain dynamically stable, such lobes can only be inflated by powerful radio sources, which are relatively rare (see Section 5.5). In this scenario, buoyant bubble models are not applicable, and dynamics of the remnant lobes must be taken into account. This has been done by Nolting et al. (2019), who showed that recently switched off lobes revived by a cluster shock passage can produce toroidal structures  $\sim$ 200 kpc in diameter; however those authors only considered recently switched off lobes, which will be a relatively small subset of all shocked remnants. Dolag et al. (2023) showed that ORC-like structures can be produced by shocks resulting from galaxy mergers, but pointed out that the energetics required to produce the observed radio emission through diffusive shock acceleration (DSA) of thermal electrons are challenging.

In this paper, we explore scenarios under which shock acceleration of remnant radio lobes can produce ORC-like radio morphologies. Our relativistic hydrodynamic simulations follow the full jet duty cycle, from inflation of supersonically expanding lobes by the initially conical, relativistic jets, through the remnant phase of lobe evolution, to shock re-acceleration of the lobe plasma. At all stages, we calculate in post-processing the synthetic radio emission from lobe electrons; this includes re-acceleration at shocks, as well as adiabatic, synchrotron and inverse Compton losses. This approach allows us to self-consistently follow the populations of cosmic ray electrons available for re-acceleration by the shock passage.

We introduce our technical setup and simulations in Section 2. We present our results in Sections 3 and 4. In Section 5, we discuss our main findings, focusing on the importance of progenitor



**Figure 1.** Two-dimensional projection of the simulation grid. Coordinates are in kpc. The central 1 kpc regions in each coordinate have resolution of 0.1 kpc, decreasing to 1.0 kpc at a distance of 10 kpc from the origin, and 10 kpc resolution at distances beyond 100 kpc. The jet injection cone and associated spherical region are also shown.

properties, remnant age, and shock and viewing geometry. We summarise in Section 6.

#### 2. Methods

# 2.1 Numerical hydrodynamics

We use the freely available numerical hydrodynamics code PLUTO<sup>b</sup> version 4.3 (Mignone et al. 2007, 2012) to simulate the evolution of initially relativistic bipolar AGN jets. Our setup follows Yates et al. (2018), Yates-Jones, Shabala, & Krause (2021), and Yates-Jones et al. (2022), and we refer the reader to these papers for technical details. Briefly, we use the relativistic hydrodynamics physics module of PLUTO, along with the hllc Riemann solver, linear reconstruction, second-order Runge–Kutta time-stepping, and a Courant–Friedrichs–Lewy (CFL) number of 0.33.

# 2.1.1 Simulation grid

A challenge in accurately representing large radio sources inflated by relativistic jets is the need to achieve sufficiently high resolution in the jet collimation region while also simulating a large (>1 Mpc<sup>3</sup>) simulation grid. Insufficient resolution at jet collimation scale would result in an underexpanded, heavy jet with large forward ram pressure; such a jet will inflate unrealistically narrow radio lobes. We use a static three-dimensional Cartesian grid, typically 290<sup>3</sup> cells consisting of five uniform and stretched patches symmetric about the origin (see Fig. 1 and Table 1), to achieve this. A central uniform grid patch of 20 cells is defined around the injection region in all three dimensions  $(-1 \rightarrow 1 \text{ kpc},$ a resolution of 0.1 kpc). Either side of this central patch is a geometrically stretched grid of 45 cells, spanning  $1 \rightarrow 100$  kpc; this patch has resolution of 1.0 kpc at 10 kpc from the origin, and 10.0 kpc resolution at 100 kpc. We use a uniform grid of a further 90 cells to maintain this 10 kpc resolution in the outermost regions  $(100 \rightarrow 1\,000 \text{ kpc})$  of the simulation domain. Following Krause et al. (2012), a jet with kinetic power  $Q_i$ , half-opening angle  $\theta_i$  and speed  $v_i$  in an external environment with density  $\rho_x$ , sound speed  $r_x$ , and adiabatic index  $\Gamma_x$  will begin recollimation at a length scale  $L_{1,a} = \left(\frac{\Gamma_x \sin \theta}{\pi(1 - \cos \theta)}\right)^{1/2} \left(\frac{Q_i}{\rho_x v_j}\right)^{1/2} c_x^{-1}$ . For our typical

<sup>b</sup>http://plutocode.ph.unito.it.

parameters (Section 2.1.3), the expected scale of jet recollimation is  $L_{1,a} \sim 5$  kpc, and the jet width of 3 kpc is sufficiently resolved with our 0.5 kpc resolution at this distance.

## 2.1.2 Jet injection

Following Yates-Jones et al. (2021), the bipolar jets are injected as a mass outflow internal boundary condition. We adopt a halfopening angle of  $\theta_j = 15^\circ$ , which produces Fanaroff-Riley type II (Fanaroff & Riley 1974, FR-II) jets with realistic jet widths (Krause et al. 2012; Yates et al. 2018; Yates-Jones et al. 2021). The jet injection region is defined as a sphere with radius 0.5 kpc. The values of density and pressure in cells within this region are overwritten with the corresponding injection zone values; cells at angles  $\theta < \theta_j$  to the *z*-axis within the injection sphere are also assigned a velocity equal to the jet velocity  $v_j = 0.95c$ . The jet density  $\rho_j$ , pressure  $P_j$ , and cross section  $A_j$  at the jet inlet can be related to the (single-) jet kinetic power (Mukherjee et al. 2020; Yates-Jones et al. 2021),

$$Q_{j} = \left[\gamma_{j}(\gamma_{j}-1)c^{2}\rho_{j} + \gamma^{2}\frac{\Gamma_{j}}{\Gamma_{j}-1}P_{j}\right]\nu_{j}A_{j}$$
(1)

where  $\gamma_j = \left[1 - (\nu_j/c)^2\right]^{-1/2}$  is the bulk jet Lorentz factor and  $\Gamma_j$  is the jet adiabatic index. We inject pressure-matched jets, that is,  $P_j$ equals the ambient pressure at the jet inlet. The requirement that the jets are cold ( $\chi \equiv \frac{\Gamma_j}{\Gamma_j - 1} \frac{\rho_j c^2}{P_j} = 100$ ) allows the jet density at injection to be calculated. Although  $\Gamma_j = 5/3$  (corresponding to cold jets) initially, we use the Taub–Mathews equation of state (Taub 1948; Mathews 1971; Mignone & McKinney 2007) to account for any shock-heating of the jet material; the reader is referred to Yates-Jones et al. (2021) for further details of the jet injection setup.

#### 2.1.3 Environment

For all simulations, we adopt an environment representative of clusters. We adopt an isothermal beta profile for the density and pressure,  $\rho_x(r) = \rho_0 \left[1 + \left(\frac{r}{r_0}\right)^2\right]^{-3\beta}$ , with temperature  $T = 3.6 \times 10^7$  K (corresponding to a sound speed  $c_s = 910$  km s<sup>-1</sup>), central density  $\rho_0 = 5 \times 10^{-23}$  kg m<sup>-3</sup>, core radius  $r_0 = 30$  kpc, and exponent  $\beta = 0.38$ . These values are consistent with observed low-redshift clusters (Vikhlinin et al. 2006) and cosmological simulations (Cui et al. 2018; Yates-Jones et al. 2023), with the possible exception of a smaller scaling radius  $r_0$ ; as most of the evolution presented in this paper occurs on scales of several hundred kpc, our environments are representative of clusters on the scales of interest.

This choice of a cluster environment is consistent with observations of both ORCs and their putative progenitors, powerful radio galaxies. Probable host galaxies for ORC1, ORC4, and ORC5 are all massive, red ellipticals with slowly accreting black holes (Koribalski et al. 2023; Rupke et al. 2023). When hosting powerful FR-II radio sources, such galaxies are preferentially found in clusters (Hardcastle & Croston 2020). While ORC environments are not well constrained at present, ORC1 is likely to be in an overdensity and likely hosts of ORCs 4 and 5 have close companion galaxies (Norris, Crawford, & Macgregor 2021a), similar to hosts of powerful radio galaxies (Krause et al. 2019).

We note that our analysis below is not strongly affected by the choice of environment. Edge-brightened FR-II radio galaxies such as those simulated in this work are even more prevalent in less

Table 1. Simulations. t<sub>shock</sub> refers to the approximate age of the system at which the shock front reaches the remnant lobe.

Simulation code	Type of simulation	Single jet power (W)	t <sub>on</sub> (Myr)	Domain (kpc <sup>3</sup> )	Grid cells $(N_x \times N_y \times N_z)$	Resolution (kpc) at 100, 1 000 kpc
Simulation code	Type of	Single jet power	t <sub>on</sub>	Shock angle	Shock speed	t <sub>shock</sub>
	simulation	(W)	(Myr)	(degrees)	$(\mathrm{km}~\mathrm{s}^{-1})$	(Myr)
Q38-t50-s90	normal shock	10 <sup>38</sup>	50	90	3 000	280
Q38-t50-s70	70 deg oblique shock	10 <sup>38</sup>	50	70	3 000	280
Q38-t50-s45	45 deg oblique shock	10 <sup>38</sup>	50	45	3 000	280
Q38-t50-s20	20 deg oblique shock	10 <sup>38</sup>	50	20	3 000	280

dense environments such as galaxy groups (Hardcastle & Croston 2020), hence lobe dynamics would not be qualitatively impacted. For fixed jet power, the time to inflate radio lobes to a given size (and thus the total number of radiating leptons) scales with density as  $\rho^{-1/3}$  (Kaiser & Alexander 1997; Shabala & Godfrey 2013; Turner & Shabala 2023), hence the luminosities presented in Section 3 are robust for a realistic range of environments.

## 2.2 Radio emission

Strong internal shocks such as jet recollimation shocks and hotspots are the sites of particle acceleration in radio galaxy jets (Meisenheimer et al. 1989; Orienti, Murgia, & Dallacasa 2010; McKean et al. 2016), and strong external shocks have been argued to re-accelerate relic non-thermal plasma (Finoguenov et al. 2010; Iapichino & Brüggen 2012; Stroe et al. 2014).

We follow the method of Yates-Jones et al. (2022), which employs the Lagrangian passive tracer particle module of PLUTO 4.3 (Vaidya et al. 2018). The details of our implementation are given in Appendix 2. Briefly, each Lagrangian particle in the PLUTO simulations represents an ensemble of electrons; our simulations track the re-acceleration history due to shocks of each such ensemble, and we calculate in post-processing the energy losses due to adiabatic expansion, inverse Compton upscattering of Cosmic Microwave Background (CMB) photons, and synchrotron emission.

The radio emissivity is calculated as follows. Starting with the Lorentz factor required for the given electron ensemble to radiate at the observed frequency, we iterate backwards in time to infer the (higher) Lorentz factor at the time when this ensemble was last accelerated. This injection Lorentz factor depends on the local magnetic field strength (for synchrotron losses) and the CMB energy density (for inverse Compton CMB losses). Electron populations which have suffered severe losses (e.g. in regions of high magnetic field strength and/or accelerated sufficiently long ago) will require very high injection Lorentz factors; such electrons are in the power-law tail of the DSA energy distribution and will therefore contribute little to the integrated emissivity.

Several model parameters affect the predicted synchrotron emissivity; the majority of these are robustly constrained by observations of radio galaxies and remnants.

The power-law slope of the DSA electron energy distribution in the active phase is set to s = 2.2, corresponding to a synchrotron spectral index of  $\alpha_{inj} = 0.6$  characteristic of radio galaxy lobes; we note that the exact value of this parameter is not important to the results presented in this paper.

The greatest source of uncertainty in our analysis is the lowenergy cutoff for the radiating particles. We set this parameter to  $\gamma_{\min} = 500$ , consistent with observations of hotspots (Carilli et al. 1991; Stawarz et al. 2007; Godfrey et al. 2009; McKean et al. 2016) and lobe evolutionary tracks (Turner et al. 2018a; Turner, Shabala, & Krause 2018b; Yates-Jones et al. 2022) in powerful radio sources similar to those simulated here. No radio relics have been observed to show a low-energy cutoff; however the much lower (by about three orders of magnitude compared to hotspots; Godfrey et al. 2009) magnetic fields in remnants mean such a turnover would only be detectable at frequencies below 100 MHz even for high  $\gamma_{min}$  values. We therefore adopt a fiducial value of  $\gamma_{\min} = 500$  in our analysis, but caution that the uncertainty in this parameter introduces a large uncertainty in the normalisation of calculated emissivities, as for spectra steeper than s = 2 the majority of electrons will have Lorentz factors just above  $\gamma_{\min}$ .

Because the simulations presented in this paper are purely hydrodynamic, we need to assume a mapping between the lobe magnetic field strength and a hydrodynamic quantity. We follow an established approach (Kaiser, Dennett-Thorpe, & Alexander 1997; Turner & Shabala 2015; Hardcastle 2018) to relate the lobe magnetic field strength to pressure; this approach yields inferred lobe magnetic field strengths which are consistent with independent X-ray measurements (Turner et al. 2018b; Ineson et al. 2017). Similarly, our assumed remnant magnetic field strengths are consistent with observations; details are provided in Appendix 2. While the lack of magnetic fields in our simulations means that we are unable to track the small-scale details in emergent radio structures, the success of hydrodynamic approaches in modelling radio galaxy lobes validates our overall analysis.

The final important parameter is the total number of radiating particles. Because we simulate the full duty cycle of jet activity, we track this quantity throughout the active phase as jet material is supplied to the lobes and then ensure that it is conserved in the remnant phase of lobe evolution.

For each simulation snapshot, surface brightness is calculated by integrating emissivity through the entire simulation volume along a given line of sight. These synthetic surface brightness maps are convolved with a two-dimensional Gaussian beam with 6 arcsec Full Width at Half Maximum. Redshift dependence is explicitly included in post-processing through changes to the restframe frequency (and hence Lorentz factor) of emission for a given observing frequency, strength of the CMB photon energy density field, resolution, and observed flux density of simulated sources.

# 2.3 Simulations

The suite of simulations used in this work is presented in Table 1. The main simulations use relativistic ( $v_j = 0.95c$ ) jets with kinetic power  $10^{38}$  W per jet, powered for 50 Myr; these parameters are characteristic of moderate power FR-II radio galaxies (Rawlings & Saunders 1991; Kino & Kawakatu 2005; Godfrey & Shabala 2013; Turner et al. 2018b; Hardcastle & Croston 2020; Turner & Shabala 2023). Our technical setup follows Yates-Jones et al. (2021): the jets are injected conically at a height of 0.5 kpc and initial radius 0.1 kpc, with a half-opening angle of 15 degrees; such jets are likely to retain their FR-II morphology following collimation (Alexander 2006; Krause et al. 2012). We refer the reader to Yates-Jones et al. (2021) for technical details.

All our jets inflate radio galaxies several 100 kpc in size at switch-off. We follow the remnant phase of evolution and find (Section 3) that the synchrotron emission in this phase fades rapidly. The second suite of simulations therefore explores reacceleration of cosmic ray electrons by the passage of a planeparallel shock, creating a 'phoenix' phase of radio emission. We explore four shock orientations: a normal shock (i.e. a planeparallel shock perpendicular to the jet axis), and three shocks inclined at 20, 45, and 70 degrees to the normal. The microphysics of DSA is complex, with shock strength, orientation, and the fraction of energy imparted to the electrons all potentially playing a role in determining particle acceleration efficiency (e.g. Böss et al. 2023). We follow the approach of Kang (2020) and assume a power-law energy distribution for remnant electrons revived by shocks, with the normalisation set by the total number of electrons injected during the active jet phase (see Appendix 2). As shown by Kang (2020), both a power-law energy distribution and only a weak dependence of emissivity on the shock Mach number are found in semi-analytic DSA models for shocks with Mach number exceeding three, as in our simulations. In this aspect, our re-acceleration model is less dependent on unknown physics, and hence simpler, than the paradigm involving in situ shock acceleration of thermal electrons. In addition to a much weaker dependence on shock parameters (Kang 2020), our fossil electron model also avoids the so-called pre-acceleration problem, in which low-energy electrons cannot repeatedly cross the shock to undergo repeated acceleration due to their small gyroradii (see e.g. Malkov & Drury 2001; van Weeren et al. 2016; Kang, Ryu, & Ha 2019 for details, and Caprioli & Spitkovsky 2014; Ryu, Kang, & Ha 2019 for possible solutions).

Each active jet simulation required approximately 200k CPU hours on the University of Tasmania's *kunanyi* HPC cluster; remnant and shock simulations are significantly cheaper.

# 3. Results

Our choice of simulation parameters, specifically the low jet density, high speed, and narrow jet opening angle, ensure that all jets considered in this work inflate lobes with characteristic edgebrightened FR-II morphology (see e.g. review by Turner & Shabala 2023). The narrowness of injected jets means that they have sufficient forward thrust to propel the terminal shock past the jet recollimation shock. Because the jets are light, the collimation is done by the cocoon inflated via backflow from the jet termination shock, rather than by the external medium; this produces narrow jets (Komissarov & Falle 1998; Krause 2005; Alexander 2006; Krause et al. 2012), consistent with observations of FR-II radio galaxies. Fig. 2 shows the evolution of moderate power (10<sup>38</sup> W) relativistic ( $v_j = 0.95c$ ) jets in the Q38-t50 simulation. Rows show relevant variables: density, jet tracer, jet particles, and synchrotron emissivity at 1 000 and 200 MHz. At 50 Myr (left column), a 550 kpc radio galaxy with clear FR-II morphology is seen, including edge-brightened lobes and narrow jets. If ORCs are radio galaxies viewed close to end-on, they must be seen in the remnant phase to avoid emission from the jet head region, which would produce extended bright emission near the geometric centre of the ORCs; we note that this argument does not depend on the morphology (FR-I or FR-II) of the ORC progenitor.<sup>c</sup> Columns in Fig. 2 show the dynamical and radiative evolution of the remnant lobes, starting at the jet switch-off time of 50 Myr.

# 3.1 Rapid fading of remnant lobes

A key tenet of this paper is that, in the absence of particle reacceleration, the dynamical evolution of remnant radio lobes required to give the observed ORC morphology is much slower than the rate at which the lobe synchrotron emission fades. We now present numerical and analytical results in support of this argument.

As the remnant lobes evolve, the channel formerly occupied by the jet is excavated (top two rows of Fig. 2), and the lobes slowly transition to a toroidal morphology as predicted by Churazov et al. (2001). However, this transition is slower than both the decay of the strong bow shock ahead of the lobes, clearly seen in the density maps even at 150 Myr; and the rapid fading in surface brightness (bottom two rows). These results are consistent with recent literature (Hardcastle 2018; Shabala et al. 2020) and can be understood as follows.

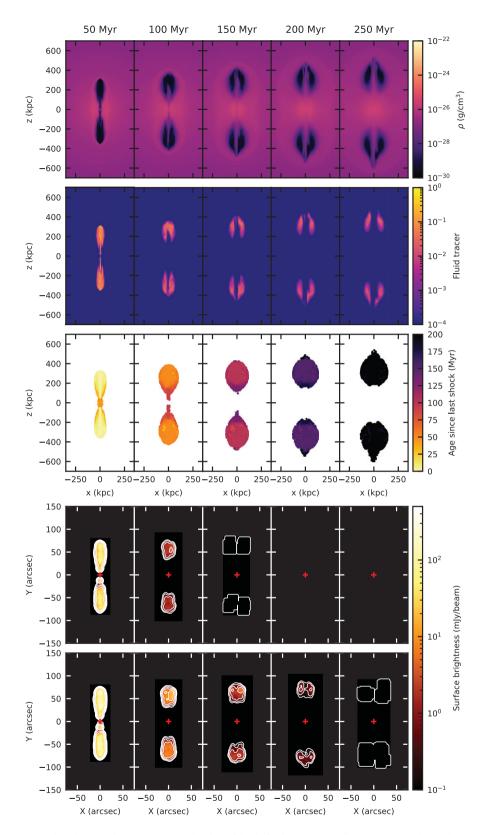
# 3.1.1 Fading timescale

The typical remnant fading time is  $t_{\text{fade}} \approx -\frac{\gamma}{d\gamma/dt}$ , where  $\gamma$  is the characteristic Lorentz factor emitting at observing frequency  $\nu$ . The radiative loss rate term in the denominator is  $\frac{d\gamma}{dt} = -\frac{4}{3}\frac{\sigma_T}{m_e}\gamma^2(u_B + u_{\text{CMB}})$ , where  $u_B$  is the lobe magnetic field energy density and  $u_{\text{CMB}} = 4.17 \times 10^{-14}(1 + z)^4$  J m<sup>-3</sup> is the energy density of CMB photons. This expression is a lower limit on the loss rate, since it ignores any adiabatic expansion which can be important to lobe evolution, particularly in the active phase (Kaiser et al. 1997; Turner & Shabala 2015; Shabala & Godfrey 2013; Hardcastle 2018). The fading timescale is therefore

$$t_{\text{fade}} \le \frac{3}{4} \frac{m_e c}{\sigma_T} \gamma^{-1} (u_B + u_{\text{CMB}})^{-1}$$
(2)

At low redshift, the magnetic field energy density dominates Equation (2), with typical field strengths at several  $\mu$ G level (Hardcastle et al. 2016; Ineson et al. 2017; Turner et al. 2018a). An estimate for the lobe field strength of  $B \gtrsim (2\mu_0\eta_{eq}\eta_{op}p_x)^{1/2} = 8.7 \times 10^{-10} (\eta_{eq}\eta_{op})^{1/2}$  Tesla is obtained from the constraint that FR-II lobes do not suffer significant entrainment (Croston & Hardcastle 2014; Ineson et al. 2017), and thus the lobe pressure should be approximately comparable to the thermal pressure in the external gas,  $p_x \gtrsim 3 \times 10^{-13}$  Pa in our simulated environments. The factor  $\eta_{eq} \equiv u_B/p$  (Hardcastle et al. 2016; Ineson et al. 2017; Turner et al. 2018b) is the ratio of magnetic field energy density

<sup>&</sup>lt;sup>c</sup>While edge-brightened lobes inflated by cosmic ray proton-dominated jets may appear as circles when viewed end-on (Lin & Yang 2024), for the majority of orientations such models predict edge-brightened structures which are inconsistent with observations of the radio galaxy population.



**Figure 2.** Hydrodynamic quantities and synthetic synchrotron emission in the plane of the sky for the Q38-t50 simulation at z = 0.3. Columns show snapshots every 50 Myr; the left panels correspond to the switch-off time of 50 Myr; subsequent panels show remnant evolution. Top row: mid-plane density. Second row: mid-plane jet tracer. Third row: particle age since last shock; youngest particles are plotted on top. Fourth row: integrated surface brightness at 1 GHz, viewed in the plane of the sky and convolved with a 6 arcsecond beam FWHM. Contours are at 0.1, 0.3, 1, 3, and 10 mJy beam<sup>-1</sup>. Bottom row: surface brightness at 200 MHz, convolved to the same beam. 1 arcsec = 4.5 kpc at the simulated redshift z = 0.3, hence all plots are shown on the same spatial scales. Remnant lobes fade rapidly after the jet switches off.

to pressure in the lobes; and  $\eta_{op} \equiv p_l/p_x \approx 1 - 3$  (Croston et al. 2005; Ineson et al. 2017; Hardcastle & Croston 2020) is the overpressure factor of the lobes with respect to the surrounding gas. In our simulations we adopt  $\eta_{eq} = 0.03$ , corresponding to lobe magnetic fields of  $\sim 10 \ \mu G$  at the time the powerful jets switch-off, and fading to a few  $\mu$ G level in the remnant phase, consistent with observations (Croston, Ineson, & Hardcastle 2018; Knuettel, O'Sullivan, Curiel, & Emonts 2019). Hence the factor  $(\eta_{eq}\eta_{op})^{1/2}$  is of order unity.

The minimum Lorentz factor of electrons required to produce emission at a frequency  $\nu$  is  $\gamma = \left(\frac{\nu}{\nu_L}\right)^{1/2}$  where  $\nu_L = \frac{eB}{2\pi m_e}$  is the Larmor frequency (in SI units). Using typical scalings above,  $\gamma = 6.4 \times 10^3 \left(\frac{\nu}{1 \text{ GHz}}\right)^{1/2} \left(\frac{u_B}{3 \times 10^{-13} \text{ Pa}}\right)^{-1/4}$  and the fading timescale is  $t_{\text{fade}} \leq 51 \text{ Myr} \left(\frac{\gamma}{6.4 \times 10^3}\right)^{-1} \left(\frac{u_B + u_{\text{CMB}}}{3 \times 10^{-13} \text{ Pa}}\right)^{-1}$ .

# 3.1.2 Dynamical timescale of buoyant bubbles

The minimum timescale associated with the transformation of a remnant lobe to a torus (and hence an ORC when viewed close to head-on) is the time for cocoon expansion to slow down to subsonic velocities, plus the time for the morphological transformation. We now show that this timescale is significantly longer than the remnant fading timescale.

If ORC progenitors are large radio lobes, these must be inflated by moderate-to-high power jets for the following reasons. First, inflation of large (several hundreds of kpc) lobes in a reasonable (hundreds of Myr; Alexander & Leahy 1987; Harwood et al. 2013; Hardcastle et al. 2019) time requires a substantial supersonic lobe expansion phase, which can only be provided by jets with high kinetic power (Begelman & Cioffi 1989; Kaiser & Alexander 1997; Hardcastle & Krause 2013; Turner & Shabala 2023); such a supersonic phase is also necessary for the lobes to not become substantially entrained by the external gas. Second, populations studies suggest that lower power sources are typically short-lived (Hardcastle et al. 2019) and hence unlikely to produce very large sources.

The integrated radio luminosity of large sources declines with source size due to a combination of synchrotron, adiabatic and inverse Compton losses; in order to be visible (even when compressed into ring-like structures) these sources must therefore be powered by a large mass flux along the jet. This is an important consideration, because as pointed out by Nolting et al. (2019) the timescale for the transition to the buoyant rising bubble phase can be significant. We now show that, for parameters typical of powerful radio sources, this is substantially longer than the bubble fading time.

For source of size  $D_s$  at switch-off time  $t_s$ , the remnant grows as (Kaiser & Cotter 2002)

$$D(t) = D_s \left(\frac{t}{t_s}\right)^{2/(2-\beta+3\gamma_c)}$$
(3)

where the external medium density profile is  $\rho_x(r) = \rho_0 \left(\frac{r}{r_0}\right)^{-\beta}$ , and  $\gamma_C = 4/3$  for a relativistic cocoon. For our simulated cluster

environment,  $\beta \approx 1$  at radii well beyond  $r_0 \approx 30$  kpc, and hence  $D(t) = D_s \left(\frac{t}{t_s}\right)^{2/5}$ . Hence the transition to subsonic expansion happens at time  $t_b = t_s \left(\frac{\dot{D}_s}{c_s}\right)^{5/3}$ . For the Q38-t50 simulation (Fig. 2), the observed cocoon size at switch-off  $t_s = 50$  Myr is  $D_s \approx 320$  kpc, and the bow

shock expansion speed at switch-off is  $\dot{D}_{s} \approx 1.5 \times 10^{6}$  km s<sup>-1</sup>. This yields an expected  $t_h \approx 120$  Myr, consistent with the mildly supersonic forward velocities observed in the 100 Myr snapshot, and subsonic velocities in the 150 Myr snapshot in Fig. 2.

In the active phase, the relationship between single jet kinetic power Q, source age t, and size D is given by (e.g. Kaiser & Alexander 1997):

$$D(t) \propto \left(\frac{Qt^3}{\rho_0 r_0^5}\right)^{3/(5-\beta)} \approx \left(\frac{Qt^3}{\rho_0 r_0^5}\right)^{3/4}$$
(4)

For a given environment, we therefore have  $D(t) \propto (Qt^3)^{3/4}$  and  $\dot{D} \propto Q^{3/4} t^{5/4}$  in the active phase.

Equations (3) and (4) now predict the dependence of the buyoancy timescale on jet parameters,  $t_b \propto Q^{5/4} \hat{t}_s^{37/12}$ . More powerful, longer-lived jets will take longer to reach the buoyant phase. For example, with reference to the Q38-t50 simulation, we expect a more powerful ( $Q = 10^{40}$  W), shorter-lived ( $t_{on} = 10$  Myr) jet to enter the buoyant phase 2.2 times later, at around 260 Myr.

These timescales  $t_b$  are all much longer than the fading timescale of the bubbles calculated in Section 3.1.1. Fig. 2 confirms that remnants fade well before the development of toroidal structures characteristic of old remnants.

## 3.2 Transient features in powerful backflows

In principle, it may be possible for an ORC to form if the timescale  $t_{\rm evac} \sim \frac{r_{\rm ORC}}{M_c}$  associated with the evacuation of a cavity is shorter than the fading timescale. Here,  $M_x$  is the Mach number of the flow with respect to the ambient medium,  $c_s \sim 900 \text{ km s}^{-1}$  is the ambient sound speed, and  $r_{\rm ORC} \approx 200~{\rm kpc}$  is the characteristic radius of the ORC (e.g. ORC1, Norris et al. 2022). External Mach numbers  $M_x > 4$ , corresponding to flow velocities in excess of 0.01care required for this dynamical timescale to be shorter than  $t_{fade}$ (Equation (2)).

Detailed analysis of simulations in this paper, however, shows that while fast (>15000 km s<sup>-1</sup>) backflow from strongly overpressured hotspots in recently switched-off sources can indeed temporarily evacuate central cavities, these structures are exceptionally transient and not necessarily ring-like in morphology; furthermore, the emission is very patchy and fades rapidly over several Myr. These characteristics are at odds with observations of ORCs 1, 4, 5, and 6 which show narrow, smooth rings of emission (Norris et al. 2021c, 2022; Koribalski et al. 2021).

## 4. Revived remnant lobes

Discussion in Section 3.1 shows that, for toroidal remnants to be visible, the synchrotron-emitting electrons must be re-accelerated. We consider this scenario next.

The large sizes (hundreds of kpc; Fig. 2) of remnant lobes inflated by typical ( $Q \sim 10^{38}$  W) FR-II jets are comparable to cluster virial radii, and these remnants will be subject to cluster 'weather'. Recently, Rajpurohit et al. (2020, 2021); Domínguez-Fernández et al. (2021) and Wittor et al. (2021) have presented evidence for re-acceleration of fossil remnants by weak cluster shocks, for which there is ample observational evidence (Planck Collaboration et al. 2013; Chon et al. 2019). In particular, Domínguez-Fernández et al. (2021) showed that the interaction of a cluster shock wave with a uniform Mach number with the ICM will naturally produce a range of Mach numbers, which in turn can

produce radio spectra steeper ( $\alpha \sim 1.1$ ) than expected in singleshock DSA models, and remarkably similar to ORC1 (Norris et al. 2022). Russell et al. (2022) show these shocks are typically narrow and quasi-planar on scales of hundreds of kiloparsecs. In this section, we calculate the morphology of radio emission from remnant plasma reaccelerated by such weak shocks.

# 4.1 Shock re-acceleration in a hydrodynamic simulation

We initialise plane-parallel shocks in our simulations by setting the post-shock pressure and density as given by the hydrodynamic Rankine–Hugoniot conditions,

$$p' = p\left(\frac{2\Gamma_x M^2 - (\Gamma_x - 1)}{\Gamma_X + 1}\right) = \frac{5M^2 - 1}{4}p$$
  

$$\rho' = \rho\left(\frac{(\Gamma_x + 1)M^2}{(\Gamma_X - 1)M^2 + 2}\right) = \frac{4M^2}{M^2 + 3}\rho$$
(5)

Here, *p* and  $\rho$  refer to the unshocked ambient medium, and *P*' and  $\rho'$  to the shocked quantities. For a fiducial shock travelling at 3 000 km s<sup>-1</sup> (Table 1), corresponding to a Mach number of M = 3.3 (see Section 4.2), we get a factor of 13.3 increase in pressure, and a factor of 3.1 increase in density, in the post-shock material.

These quantities, together with the relevant shock velocity, are implemented as a user-defined boundary condition in PLUTO at all post-shock locations. The initial location of the shock front is such that the shock first reaches the lobe at approximately 400 Myr.

## 4.2 Shocks normal to the jet axis

We first investigate the effects of a plane-parallel shock oriented perpendicular to the jet axis; for jets propagating in the *z*-direction, our shock therefore lies in the *x-y* plane. We adopt a shock speed of 3 000 km s<sup>-1</sup>, corresponding to a Mach number number of 3.3 representative of cluster shocks (e.g. Vazza et al. 2016,Wittor et al. 2021, and references therein). Fig. 3 shows that such shocks are efficient at both compressing and 'lighting up' particular sections of the remnant torus. For most observing orientations, the radio emission will appears either as a relic (for viewing angles  $\leq 30^{\circ}$ ), or as a circular ring (for viewing angles  $\geq 45^{\circ}$ ). We provide a more detailed gallery of possible phoenix morphologies for both normal and non-normal shocks in Appendix 1.

Fig. 4 shows the radial surface brightness distribution for different viewing angles. Even viewing geometries significantly offset from 90° (i.e. not end-on) produce close to circular rings, as evidenced by a relative lack of broadening of the interquartile range at a given radius.

Importantly, for viewing angles other than 90°, the ORC host galaxy will not be at the centre of the ring. For example, shockcompressed lobes viewed at a 60° angle will have the host (located at the origin in our simulation) *within* the ring. Some ORCs, such as ORC1, indeed have galaxies within the ring structure in addition to a galaxy at the centre of the ring (Norris et al. 2022). However, the probability of the shock normal aligning perfectly with the jet axis is low, and hence below we consider phoenix morphologies for non-normal shocks.

We examine the circularity of phoenix emission and its relation to host galaxy location in more detail in Section 5.2.

## 4.3 Time dependence

Fig. 3 shows that ORC surface brightness and morphology, particularly the extent of diffuse emission, depends on the exact location of the shock. We quantify this effect in Figs. 5 and 6, which show that the observable features of the swept-up ring depend sensitively on shock location. At early times (350 Myr), the shock sweeps out a relatively narrow, edge-brightened ring. As the shock progresses, the synchrotron morphology evolves to a wider, brighter, and centrally filled ring (at 400 Myr), before fading to another edge-brightened ring at late times (450 Myr).

#### 4.4 Non-normal shocks

We now examine the morphologies created by passage of a nonnormal shock.

Fig. 7 shows the evolution of a plane-parallel shock inclined at 20 degrees to the normal, at several viewing angles; Fig. 8 shows a shock at 45 degrees to the normal; and Fig. 9 a shock at 70 degrees to the normal (i.e. a quasi-parallel shock). A comparison of characteristic radio phoenix morphologies is shown in Fig. 10.

More complex shock geometries produce a qualitatively similar, but more nuanced picture: toroidal radio structures (seen as circular emission when viewed close to edge-on) still form at late times for shocks closer to normal than parallel (Figs. 7 and 8), when the shock has interacted with the full lobe cross section. At earlier times, however, arc-like structures 'light up' only the side of the lobe which has interacted with the shock; these arcs undergo significant evolution, in both morphology and surface brightness, as the shock progresses. Even for end-on observing geometries, non-normal shocks also produce less symmetric structures; this asymmetry increases at large viewing angles, and for larger shock angles. For the largest shock angles, such as the quasi-parallel shocks in Fig. 9, no observable ellipses or circles are produced as circular symmetry is destroyed by the shock passage.

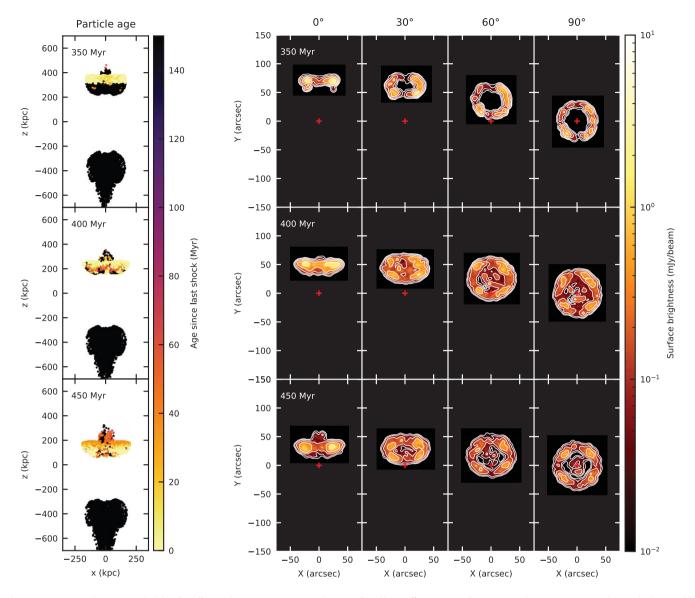
#### 5. Discussion

#### 5.1 Implications of the model

The results presented in Section 4 show that remnant radio lobes revived by a shock passage may provide a plausible explanation for the ORC phenomenon. Diffuse and edge-brightened rings are seen for a wide range of shock geometries, viewing angles and shock ages.

A diversity of ORC geometries is possible, with younger shocks creating smaller, brighter, more filled (i.e. less edge-brightened) quasi-circular structures. For a given shock angle, elliptical ORCs will be more rare than expected from simple projection arguments, because of the relatively rapid transition – with viewing angle – from mushroom cap to quasi-circular geometry. A testable prediction of our model is that, for non-normal shocks, viewing angles sufficiently away from the line of sight should produce both more elliptical and more asymmetric (i.e. one side of the ring wider than the other) ORCs. Depending on surface brightness sensitivity, such structures may be seen as one-sided arcs (e.g. Fig. 7).

Because our simulations do not include magnetic fields, we cannot make robust predictions for spatially resolved spectra in simulated ORCs. To first order, when the shock first encounters the lobe the newly shocked relic electrons attain a (Mach numberdependent) spectral index reflecting their energy distribution; this spectrum gradually steepens as the electrons age on timescales



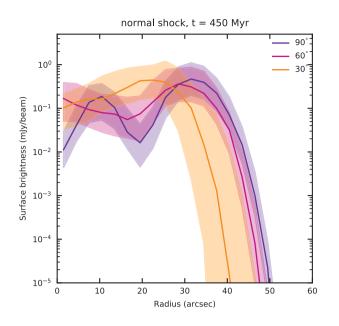
**Figure 3.** Re-energised remnant radio lobes for different observing geometries. Lobes are inflated by a 10<sup>38</sup> W jet, active for 50 Myr in a cluster environment; then evolve buoyantly until they are impacted by a plane-parallel normal shock, travelling at 3 000 km s<sup>-1</sup> in the negative *z*-direction. Rows represent three different times since the onset of the shock. Columns from left to right are: (1) time since last shock for simulated lobe particles, as viewed in the plane of the sky; and projected radio surface brightness at 1.0 GHz at viewing angles of (2) 0 degrees (i.e. in the plane of the sky); (3) 30 degrees; (4) 60 degrees; and (4) 90 degrees (i.e. 'down the barrel' of the switched off jet). Contours are at 0.01, 0.03, 0.1, 0.3, and 1 mJy beam<sup>-1</sup>, and synthetic radio emission is convolved to a 6 arcsec FWHM beam. Circular, or quasi-circular rings of emission are clearly seen for angles inclined by 45 degrees or more to the line of sight. Ellipses are rare because of the fast (in terms of viewing angle) transition between ring and 'linear relic' morphologies. The host galaxy is at the centre of the image in all cases.

comparable to the shock crossing time (cf. Equation (2)). In principle, non-normal shock and viewing geometries may produce spectral gradients across the phoenix structure; details will depend on the detailed interaction between shock and remnant dynamics, and the structure of the lobe magnetic field which may become increasingly complex in the transition to the phoenix phase.

# 5.2 Single ORCs

Rings of radio emission can be produced by quasi-normal shocks for a relatively broad range of viewing angles close to the line of sight. Because the jet axis and shock orientation are expected to be independent of each other, shock normal orientations exactly aligned with the jet axis such as in Fig. 3 are unlikely. The probability of jet-shock angle orientation in the range  $(\theta, \theta + d\theta)$  is proportional to  $(1 - \cos \theta) d\theta$ , hence shocks aligned to within 10° of the jet axis (as in Fig. 3) are 7.8 times less likely than shocks misaligned by 20° (as in Fig. 7), and 16 times less likely than shocks misaligned by 45° (as in Fig. 8). Quasi-parallel shocks (e.g. Fig. 9) are more likely still, but these do not produce circular or elliptical post-shock emission. Therefore, the shocks most likely to produce ORC-like structures are quasi-normal ones such as those in Fig. 7.

This has important implications for the likely location of the ORC host galaxies. For normal shocks, hosts can be significantly offset from the ORC geometric centre while still retaining circular structure when viewed away from the line of sight; for example,



**Figure 4.** Circularity of rings for different viewing angles, following passage of a normal shock. Lines show median surface brightness at 1 GHz, shaded region shows interquartile range for three viewing angles in Fig. 3. Quasi-circular rings are seen for 90 and 60 degree viewing angles. Departure from circularity (as given by the broadening of the interquartile range at a given radius) is observed for the 30 degree viewing angle.

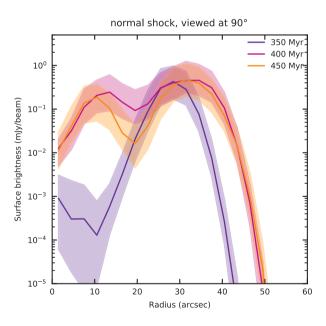


Figure 5. Circularity of rings for different remnant ages. All snapshots are viewed headon. Depending on how much lobe material has been swept up, both filled and edgebrightened rings can be produced.

in the 60° viewing angle in Fig. 4 the ORC host galaxy would be located inside the radio ring.

We quantify this effect in Fig. 11. For each normal and quasinormal shock snapshot presented in Figs. 3 and 7, we calculate the centre of emission, and semi-major and semi-minor axes lengths  $r_{maj}$  and  $r_{min}$ . The resultant offset of the centre of the radio emission from the host galaxy (located at the origin in our simulations), and the ratio  $r_{\rm maj}/r_{\rm min}$ , are plotted in Fig. 11. While there is significant variability with shock angle and time of observation, some clear trends emerge. The host galaxy can be significantly offset from the centre of the radio emission, however this requires viewing angles some way away from the line of sight. For non-normal shocks – which are more common – such viewing angles also correspond to more elliptical structures, that is, higher  $r_{\rm maj}/r_{\rm min}$  ratios at viewing angles further away from 90° in Fig. 11. A requirement for the radio emission to be close to circular requires viewing angles close to the line of sight, and hence more central host galaxies.

In Fig. 12 we calculate the probability distribution of host galaxy locations for a range of  $r_{\rm maj}/r_{\rm min}$  values, integrated over all viewing angles. For the most circular ORCs, the majority of host galaxies will be near the centre ( $\leq 0.3r_{\rm maj}$ ) of the radio emission; this trend is stronger for non-normal shocks (right panel), which are more common.

These results provide a potential explanation for observations of ORCs 1, 4, and 5, where host galaxies are associated with the ORC geometric centre at high confidence (Norris et al. 2022). The observed ORCs all have candidate host galaxies within 10 per cent of the ring radius, which is more central than the predictions in Fig. 12. We note that DSA will be more effective at accelerating the cosmic ray electrons in quasi-normal shocks (Böss et al. 2023), due to the expected topology of the magnetic field swept out by the lobes during the active phase (Hardcastle & Krause 2014; Nolting et al. 2019); this will further enhance the observability of quasi-normal shocks. A more detailed exploration of simulated ORC ellipticities for a range of shock and viewing geometries, and larger samples of observed ORCs with host galaxies, are required to examine this further. A testable prediction of our model is that host location will move away from the ORC geometric centre with increased ellipticity. Less circular and edge-brightened ORC candidates (e.g. Gupta et al. 2022) may be off-centre radio phoenixes.

# 5.3 ORCs with lobes

ORCs associated with radio lobes (e.g. ORCs 2 and 3, Norris et al. 2021c) are more challenging to explain in this model. A shock interacting with a lobe still emitting detectable synchrotron radiation will only produce strongly edge-brightened emission when viewed in projection after it has traversed the whole lobe – before this time, the parts of the lobe closer to the host galaxy will still yield detectable radio emission near the ORC geometric centre. Because the lobes fade rapidly (Section 3.1.1), this scenario requires a fast shock reaching the remnant shortly after the jet switches off, then traversing it rapidly while the counterlobe is still visible, as proposed by Nolting et al. (2019).

Figs. 7, 8, and 9 suggest another plausible scenario. If the two remnant lobes are not anti-parallel, a single shock passing through both lobes will produce structures which look different in projection. An ORC plus lobe morphology will be seen at certain viewing angles if the axis of symmetry for one of the lobes but not the other is close to the shock normal. Wide Angle Tailed (WATs) radio sources are common in clusters (O'Dea & Baum 2023), and Mpcscale cluster shocks (e.g. Russell et al. 2022) can shock both lobes; hence this scenario is plausible. We note that in both ORCs known to be associated with a radio lobe (Norris et al. 2021c; P. Macgregor

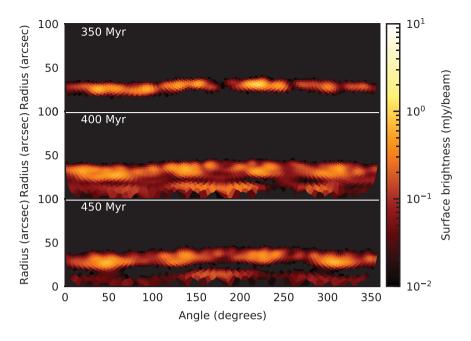


Figure 6. Polar projection of radio phoenix emission at 1.0 GHz, at the same snapshots as in Fig. 5. These are directly comparable to observations presented in Figure 4 of Filipović et al. (2022).

et al., in preparation), the two sets of radio structures are not colinear, consistent with our hypothesis. Alternative mechanisms such as precessing jets (Nolting et al. 2023) are also possible: jet precession has been reported in powerful radio galaxies (Krause et al. 2019), and ring-like structures attributed to jet precession have been observed in 3C 310 (Kraft et al. 2012) and (Rawes, Birkinshaw, & Worrall 2018) albeit on much smaller scales.

# 5.4 Detectability of ORCs

Source age, shock orientation, and viewing geometry all play a role in setting the observed morphology of the resulting radio phoenix. While detailed analysis of simulated source morphology is beyond the scope of this paper, we now provide estimates of the expected ORC fractions.

For quasi-normal shocks such as those shown in Figs. A1 and A2, circular structures appear at viewing angles  $\geq 60^{\circ}$ , ellipses for viewing angles  $30^{\circ}-60^{\circ}$ , and unstructured morphologies for viewing angles closer to side-on than approximately  $30^{\circ}$ . The probability of each range in viewing angle is proportional to the subtended solid angle  $\Delta\Omega = 2\pi \Delta$  (sin<sup>2</sup>  $\theta$ ). The surface brightness is similar for the different viewing angles. Hence approximately 13 per cent of remnants revived in quasi-parallel shocks are expected to be seen as circles, 37 per cent as ellipses, and half as neither.

The fraction of ORCs among all shock-revived remnants will be much lower. Circular and elliptical structures are not visible for quasi-parallel shocks, such as shown in Fig. 9. For intermediate shock angles (Fig. 8), even when ellipsoidal structures are produced there can be significant brightness asymmetry between different sides of the radio phoenix. Taking 30° as the largest off-normal angle that can produce detectable ellipsoidal structures, only 3 per cent of radio phoenixes are expected to be either ORCs or ellipses. The real fraction is likely to be even lower due to asymmetries in realistic remnant environments and cluster weather.

## 5.5 Expected ORC densities

We can test the plausibility of the ORCs as radio galaxy phoenixes hypothesis, by estimating the expected sky density of these objects.

The expected number of ORCs in a solid angle  $\Omega$  on the sky is given by

$$N_{\rm ORC} = \int_0^{z_{\rm max}} dz \,\Omega D_L(z)^2 \left(\frac{dD_L(z)}{dz}\right) \Phi_{\rm RG} f_{\rm shock} f_{\rm orient} f_{\rm life} \qquad (6)$$

where  $D_L$  is the luminosity distance,  $\Phi_{\rm RG}$  is the volume density of ORC progenitors, assumed to be powerful radio galaxies;  $f_{\rm shock}$  is the fraction of radio galaxy remnants revived by a shock;  $f_{\rm orient}$  is the fraction of sources with favourable orientation; and  $f_{\rm life} = t_{\rm visible}/t_{\rm active}$  is the ratio between the time for which the remnant is visible and the age of the jet which produced the remnant. The limit of the integral,  $z_{\rm max}$ , corresponds to the maximum redshift to which a typical ORC can be observed and depends on ORC morphology (including shell thickness) as well as survey surface brightness limits.

We can now make a (very approximate) estimate for the expected number of ORC1-like sources in the EMU Pilot Survey. Below, we adopt the following survey parameters (see Norris et al. 2021b): surface brightness sensitivity at 1 GHz of  $\Sigma_{\rm min} =$  90  $\mu$ Jy beam<sup>-1</sup> (corresponding to approximately  $3\sigma$ ),  $\Omega =$  0.26 sr (corresponding to 270 sq. deg.), and beam FWHM of 12 degrees.

Relevant parameters for the best-studied Odd Radio Circle, ORC1, are: ASKAP surface brightness  $\Sigma_{ORC} = 0.13$  mJy beam<sup>-1</sup>,  $z_{ORC} = 0.55$  (Norris et al. 2021c), and ring width of 40 kpc (corresponding to ORC1 being marginally resolved with MeerKAT; Norris et al. 2022). For the assumed sensitivity, the maximum observable redshift of ORC1 is  $z_{max} \sim 0.6$ .

For representative scaling parameters we adopt  $\Phi = 10^{-7}$  Mpc<sup>-3</sup>, representative of the number density of powerful radio

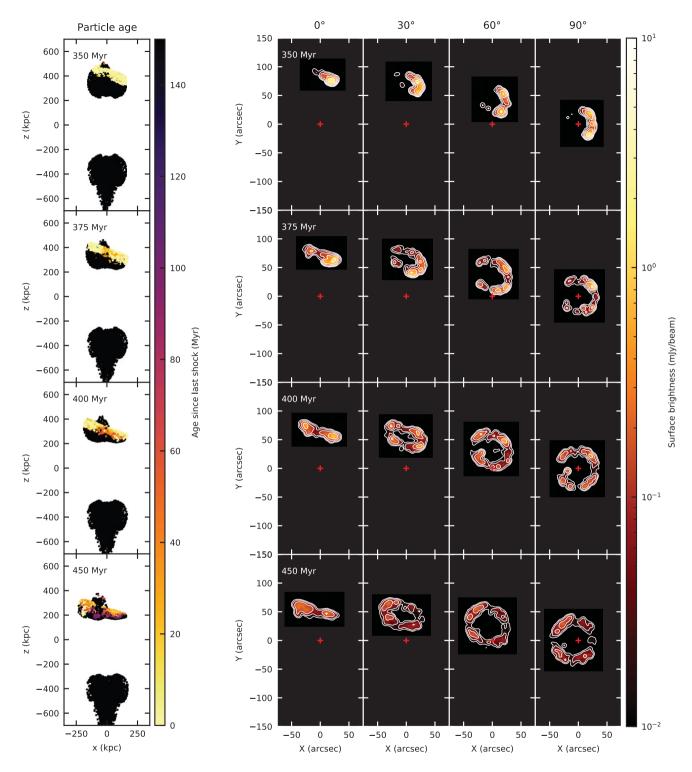


Figure 7. As Fig. 3, but for a shock angled at 20 degrees to the normal. Arcs or rings will be seen depending on whether the shock has re-energised the full lobe cross section.

galaxies in the local Universe (Hardcastle et al. 2019), a substantial fraction of which are associated with clusters (Croston et al. 2019). From results in this work, we estimate  $f_{\text{orient}} \sim 0.01$ , that is, 1 per cent of visible remnants produce ring-like structures. The largest uncertainty comes from the term  $f_{\text{life}}f_{\text{shock}}$ . We adopt  $0.05 \leq f_{\text{shock}} \leq 0.65$ , where the upper limit is set by the observed cluster merging rate (Cassano et al. 2016) and the lower limit by the fraction of prominent bow shocks in clusters in cosmological simulations (Łokas 2023); we note that the association between mergers and powerful radio galaxies (Ramos Almeida et al. 2012; Krause et al. 2019) may increase  $f_{\text{shock}}$ . Fig. 9 shows that shocked remnants are visible after 150 Myr for an initial jet active phase of

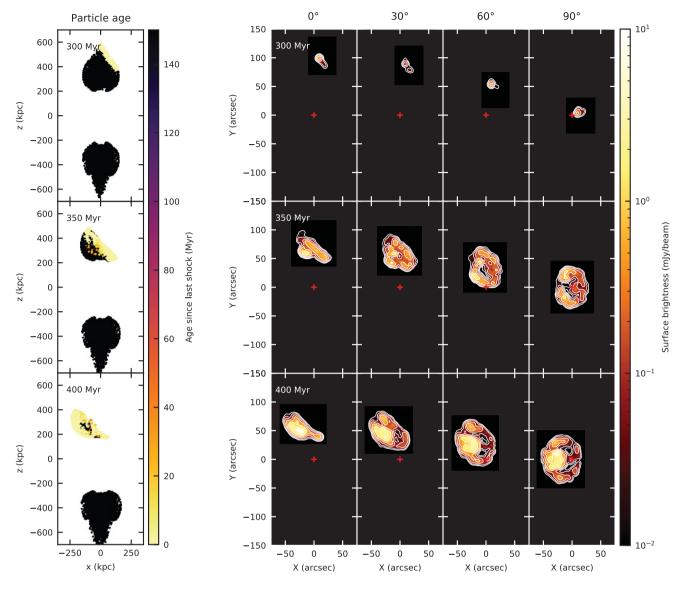


Figure 8. As Fig. 3, but for a shock angled at 45 degrees to the normal.

50 Myr, setting  $f_{\text{life}} \ge 3$ . We therefore estimate  $f_{\text{life}}f_{\text{shock}} \sim 1$ , noting the large uncertainties on this parameter.

An order-of-magnitude estimate for the expected number of ORCs in the EMU Pilot Survey field is then  $N_{\rm ORC} = 1.5 \left(\frac{\Phi_{\rm RG}}{10^{-7} \, {\rm Mpc}^{-3}}\right) f_{\rm shock} f_{\rm life} \left(\frac{f_{\rm orient}}{0.01}\right)$ . Although these numbers appear plausible and are broadly consistent with the handful of ORCs discovered so far by the EMU survey, they should of course be interpreted as order-of-magnitude estimates only due to large uncertainties in several parameters.

# 5.6 Future outlook

While capable of accurately following the dynamics of the full radio jet life cycle, and making robust global predictions for synchrotron radio emission, our hydrodynamic simulations do not capture the complex processes responsible for turbulent reacceleration of remnant plasma. Instead, we adopt a simplified approach of a single-shock threshold (Appendix 2.2) and assign a single power-law in electron energy to particles assumed to be accelerated at such shocks. More sophisticated treatments of particle re-acceleration, including full MHD and capturing of the turbulent cascade, have recently been presented by Domínguez-Fernández et al. (2021) and Wittor et al. (2020, 2021). Their findings validate our approach: Domínguez-Fernández et al. (2021) show that magnetic fields are not significantly compressed by weak (Mach 2, i.e. similar to those adopted in this paper) shocks; while Wittor et al. (2020) showed that re-acceleration of remnant plasma by sustained turbulence can lead to uniform spectral indices similar to those observed in ORC1 (Norris et al. 2022). We note that, to re-accelerate a *non-thermal* pool of electrons, as assumed in our model, shocks weaker than the canonical threshold Mach number of  $\sqrt{5}$  are sufficient (Vink & Yamazaki 2014).

Our approach of calculating radio emission in post-processing necessitates some assumptions. As discussed in Section 2.2, the most important is the low-energy cutoff for radiating particles,

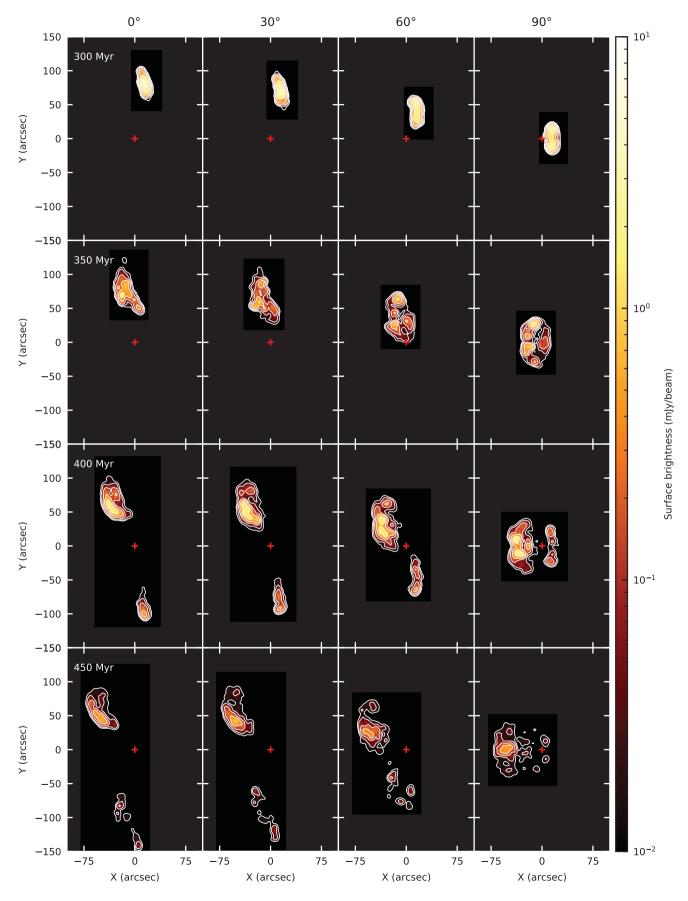
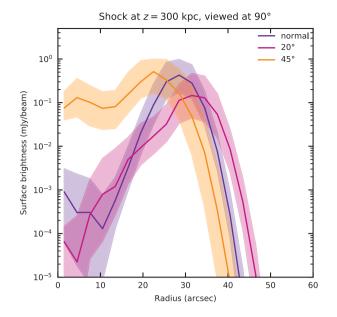


Figure 9. As Fig. 3, but for a shock angled at 70 degrees to the normal, that is, a quasi-parallel shock. No clear rings or ellipses are seen.



**Figure 10.** Circularity of rings for different shock orientations. Snapshots are selected so that the shock mid-point is at coordinate  $z \sim 300$  kpc; this corresponds to the 350 Myr snapshot for the normal shock, 400 Myr snapshot for the quasi-normal 20 degree shock; and 350 Myr snapshot for the 45 degree shock. Quasi-circular rings can be produced even by non-normal shocks.

which is directly proportional to the normalisation of the radio emission (cf. Equation (A7)). Our purely hydrodynamic simulations neglect the role of magnetic fields; while not dynamically important in the momentum-dominated phase of lobe evolution (e.g. Hardcastle & Krause 2014; English et al. 2019), magnetic field structure will affect the spatial distribution and and spectra of the radio emission. The sweeping up of magnetic field lines can also provide additional stability (along with gas viscosity) to remnant bubbles (Kaiser et al. 2005; Shabala & Alexander 2009b). On the other hand, our simulations may overestimate bubble stability by not having sufficient resolution to capture instabilities at the bubble surface and not including complex gas and shock dynamics (e.g. Dolag et al. 2023) in our idealised environments.

Our idealised assumption of plane-parallel shock geometry would be improved by instead considering radio lobe evolution in dynamical, cosmological MHD simulations (e.g. Kang & Ryu 2015; Vazza et al. 2016, 2019, 2021; Hodgson et al. 2021; Dolag et al. 2023). A crucial point to note, however, is that modelling the revived remnant dynamics requires an accurate description of the full jet lifecycle, because the dynamics of the remnant bubbles are sensitive to parameters describing the earlier, active phase of the jet-inflated lobes (see Section 3.1.2). The current generation of cosmological simulations do not model relativistic jets as observed in powerful FR-II radio sources – the putative ORC progenitors. New, hybrid codes involving both relativistic jets and cosmological initial conditions (e.g. CosmoDRAGoN, Yates-Jones et al. 2023) will be required for this work.

Shock interactions with the remnant plasma may produce detectable X-ray emission. Dolag et al. (2023) considered this issue in some detail for their shocked CGM model and concluded that this is plausible, but large uncertainties in environment properties make accurate predictions challenging. We defer a detailed investigation of this to future work.

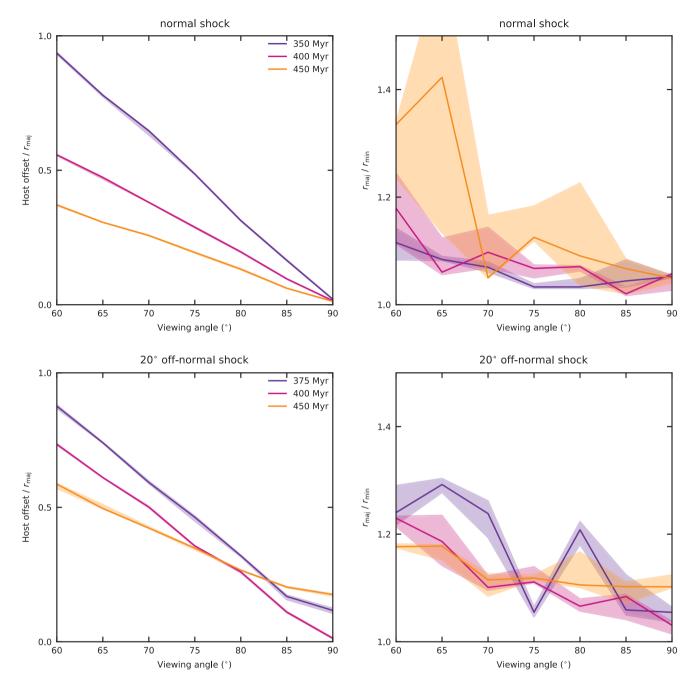
Our simulations predict that only 1 per cent of shock-lobe encounters will result in circular radio emission and 2 per cent in elliptical structures. Because of the interest in ORCs, considerable efforts have been made to find new ones. However, the elliptical and other structures produced in these encounters also have a great deal to teach us about radio galaxy physics and the presence of shocks in the environment. Observational samples of a broad range of structures, some of which are illustrated in this paper, are required to explore these aspects. Compiling such samples may be challenging because the host galaxies can be significantly offset from the radio emission; nevertheless they are likely to be worth the effort.

#### 6. Conclusions

We have run hydrodynamic simulations of powerful, relativistic jets in cluster environments and calculated synchrotron radio emission in post-processing, to test whether quasi-circular structures resembling ORCs can be produced by radio lobes. Our main findings are as follows.

- Large (>100) kpc remnant lobes fade below the detection limit faster than their morphology evolves into a toroidal shape. Hence old remnants cannot form ORCs.
- Strong backflow from powerful jets can, for a short time, evacuate a cavity near the jet head. Such structures, however, are too transient and diffuse to be consistent with the observed ORCs.
- Passage of a moderate Mach number shock sweeps up and re-accelerates remnant lobe plasma, creating ORC-like structures for a range of shock and observing geometries.
- The majority of shock lobe interactions will not form either circular or elliptical structures.
- Circular structures can be produced by the passage of a quasi-normal shock (angle between shock normal and the jet axis  $\leq 20^{\circ}$ ), and viewing angle within approximately  $30^{\circ}$  of the jet axis.
- The width, surface brightness, and ellipticity of the shockinduced radio phoenix depends on shock age and angle, and observing orientation. Asymmetric structures, including arcs, are predicted for off-axis shocks, and shocks which have only interacted with part of a lobe.
- Circular ORCs with a geometric centre which is significantly offset from the host galaxy location require the shock normal to be closely aligned with the jet axis and hence are rare. The more likely off-axis shocks produce circular structures with the host galaxy near the geometric centre, consistent with observations of known ORCs. Ellipsoidal radio structures are predicted to have host galaxies which are offset from the centre of the ellipse.
- ORCs with lobes, such as ORCs 2 and 3 (Norris et al. 2021c), can be produced by shock passage through the lobes of a WAT radio source.

In our radio phoenix model, ORCs can only be produced if the remnant radio lobes remain intact before the shock passage revives the non-thermal emission. Botteon et al. (2023) recently showed that radio lobes will be shredded by gas sloshing in clusters on a timescale of approximately 500 Myr, corresponding to



**Figure 11.** Host offset from the geometric centre of emission (left panel) and circularity (defined as the ratio of semi-major to semi-minor axes of the synthetic radio emission, right panel) observed at a range of viewing angles. Solid lines denote medians for a range of simulated sensitivities ( $0.5-2 \mu Jy$  beam<sup>-1</sup> for a 6 arcsec beam), and shaded regions show the interquartile range. Top row: normal shock. Bottom row: quasi-normal (20 degree offset) shock. Offset of the host galaxy from the ORC geometric centre increases with viewing angle away from the line of sight, while circularity decreases. For the quasi-normal shock, only observing geometries close to line of sight can produce highly circular structures.

several sound-crossing times. This timescale is longer than the duration of the remnant phase in all our simulations – which focus on powerful radio sources – and hence our proposed mechanism is plausible; however this requirement becomes increasingly challenging for lower power jets in dynamic environments.

The radio phoenix model combines two well-established features of the cosmological structure formation paradigm: largescale shocks and radio galaxy lobes. Our simulations show that ORC-like structures can be produced when these shocks interact with remnant lobes. Dolag et al. (2023) recently showed that direct shock acceleration of thermal electrons on halo outskirts may also be able to produce similar ring-like structures. Both hypotheses are plausible; the prediction of a relationship between host galaxy offset and ORC ellipticity in our phoenix model may help distinguish between these two scenarios. To definitively answer whether or not a large number of ORCs are indeed radio galaxy phoenixes

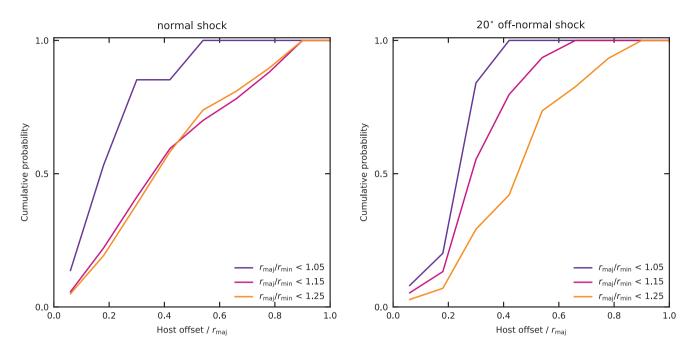


Figure 12. Cumulative probability of the location of the host galaxy for a range of ellipticities. Left panel: normal shock; right panel: quasi-normal shock. The most circular structures  $(r_{mai}/r_{min} \approx 1)$  will have host galaxies close to the geometric centre of the ORC.

will require large, detailed samples of observed ORCs, together with ever more sophisticated magnetohydrodynamic simulations of remnant jets in realistic, dynamic environments.

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#### Data Availability. Not applicable.

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#### Appendix A. Simulated radio emission

Radio phoenix geometries are shown below for a normal shock, quasi-normal shock at 20°, and a shock at 45° to the normal, for several snapshots. These plots complement those in the main body of the paper by showing a larger number of viewing geometries.

# Appendix B. Calculation of synchrotron emission

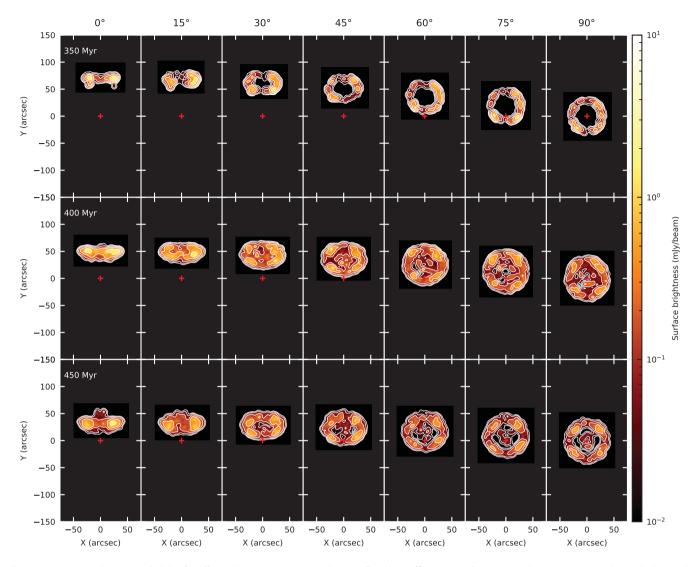
## Appendix B.1. Particle acceleration at shocks

We use the Lagrangian passive tracer particle module of PLUTO 4.3 (Vaidya et al. 2018), and detect shocks following the flagging scheme described by Mignone et al. (Appendix B 2012). A zone is flagged as shocked if the divergence of the velocity is negative,  $\nabla \cdot \mathbf{v} < 0$ , and the local pressure gradient exceeds a threshold  $\epsilon_p = p_2/p_1 - 1$ , where the subscripts "1" and "2" refer to pre- and post-shock quantities, respectively. The relationship between shock threshold, Mach number, slope of the power-law distribution of Diffusive Shock Accelerated electrons (Blandford & Ostriker 1978; Drury 1983), and the injection spectral index, is:

$$\epsilon_p = \frac{p_2}{p_1} - 1 = \frac{5(\mathcal{M}^2 - 1)}{4}$$

$$s = \frac{2(\mathcal{M}^2 + 1)}{\mathcal{M}^2 - 1} = \frac{5 + 2\epsilon_p}{\epsilon_p}$$

$$\alpha_{inj} = \frac{s - 1}{2} = \frac{5 + \epsilon_p}{2\epsilon_p}$$
(A1)



**Figure A1.** Re-energised remnant radio lobes for different observing geometries. Lobes are inflated by a 10<sup>38</sup> W jet, active for 50 Myr in a cluster environment; then evolve buoyantly until they are impacted by a plane-parallel normal shock, travelling at 3 000 km s<sup>-1</sup> in the negative *z*-direction. 450 Myr snapshot is shown at different viewing angles. This plot is for the same simulation as Fig. 3, but for a larger number of observing geometries.

Here, *s* the power-law index of energy injection  $N(E) \propto E^{-s}$ , and  $\alpha_{inj}$  the injection spectral index for the DSA electrons. For a strong shock ( $\mathcal{M} \gg 1$ ), we recover the canonical result of s = 2,  $\alpha_{inj} = 0.5$ .

In our simulations, we follow the method of Yates-Jones et al. (2022) to track three pressure discontinuities linearly separated in log-space,  $\epsilon_p = [0.5, 1.6, 5]$ . These correspond to Mach numbers  $\mathcal{M} = [1.1, 1.5, 2.2]$ , energy injection indices s = [12, 5.2, 3], and spectral indices at injection  $\alpha_{inj} = [5.5, 2.1, 1]$ .

In the active jet phase, very strong shocks are found at jet recollimation shocks, and especially hotspots. We set  $s_{active} = 2.2$ , corresponding to an injection spectral index  $\alpha_{inj,active} = 0.6$  typically observed in radio galaxies; we note that the exact value of this parameter is not important for the results presented in this paper.

### Appendix B.2. Synchrotron emissivity

Synchrotron emissivity is calculated following the approach described in Yates-Jones et al. (2022); here we recap key aspects

of our approach, and refer the interested reader to that paper for full details.

Electrons are assumed to radiate at the the critical frequency

$$\nu_c = \gamma^2 \nu_L \tag{A2}$$

where  $\nu_L$  is the Larmor frequency (e.g. Longair 2011). The magnetic field strength therefore sets the Lorentz factor of electrons radiating at the observed frequency  $\nu$ . The rate at which relativistic electrons are injected into the cocoon is set by the jet kinetic power. These electrons are accelerated at strong shocks; DSA theory predicts a power-law distribution in the energy, and hence Lorentz factor, of electrons at the time of acceleration, with number density

$$n(\gamma) \, d\gamma = n_0 \gamma^{-s} \, d\gamma \tag{A3}$$

The electron energy density subsequently evolves with time due to a combination of adiabatic, synchrotron and Inverse Compton losses; and any re-acceleration at subsequent shocks as described in Section Appendix 2.1.

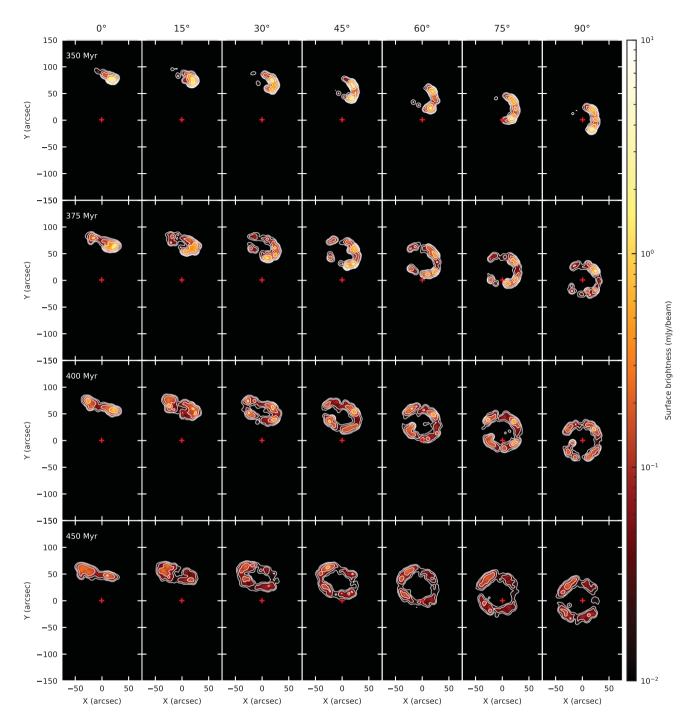


Figure A2. Same as Fig. A1 but for a shock at 20 degrees to the normal.

Each Lagrangian particle in the PLUTO simulations represents an ensemble of electrons. For each PLUTO particle, the time of last shock  $t_{acc}$  is updated at each simulation snapshot, that is, every 0.1 Myr (Section 2). This time of last electron acceleration is tracked separately for each shock threshold; in our analysis below we focus on  $\epsilon_p = 5$ . Starting with the Lorentz factor required for the electron to radiate at the observed frequency (Equation (A2)), we iterate backwards in time to infer the (higher) Lorentz factor  $\gamma_{acc}$ at injection time  $t_{acc}$  using the recursion relation (see Equation 2 of Yates-Jones et al. 2022),

$$\gamma_n = \frac{\gamma_{n-1} t_n^{a_p(t_{n-1},t_n)/3\Gamma_{\rm C}}}{t_{n-1}^{a_p(t_{n-1},t_n)/3\Gamma_{\rm C}} - a_2(t_{n-1},t_n)\gamma_{n-1}}$$
(A4)

where  $a_p(t_{n-1}, t_n) = \log (p_n/p_{n-1})/\log (t_n/t_{n-1})$  describes the instantaneous pressure evolution, and the radiative loss term  $a_2(t_{n-1}, t_n)$  depends on the local magnetic field strength (for synchrotron losses) and the CMB energy density (for Inverse Compton CMB losses). Electron populations which have suffered severe losses (e.g. in regions of high magnetic field strength and/or

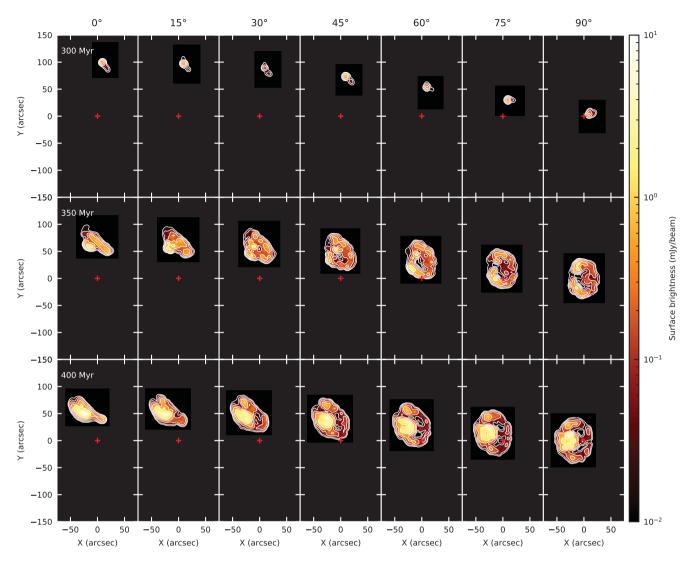


Figure A3. Same as Fig. A1 but for a shock at 45 degrees to the normal.

accelerated sufficiently long ago) will require very high injection Lorentz factors; such electrons are in the power-law tail of the DSA energy distribution, and will therefore contribute little to the integrated emissivity.

Two further quantities are required to describe the synchrotron emissivity. Simulations presented in this paper are purely hydrodynamic; we therefore need to assume a mapping between the lobe magnetic field strength and a hydrodynamic quantity. Following an established approach (Kaiser et al. 1997; Turner & Shabala 2015; Hardcastle 2018), we write

$$p = (\Gamma_{\rm C} - 1)(u_e + u_B + u_T) \tag{A5}$$

where  $u_e$  is the energy density in non-thermal (radiating) particles,  $u_B = B^2/2\mu_0$  the magnetic field energy density, and  $u_T$  the thermal pressure in the cocoon. For FR-II jets considered in this work, constraints from X-ray and radio observations (Croston et al. 2018) suggest that there are very few, if any, thermal particles in the cocoon; we therefore set  $u_T = 0$ . We adopt  $\eta \equiv u_B/p = 0.03$ , which yields lobe magnetic fields at the  $\sim$  10  $\mu G$  level, consistent with observations (Ineson et al. 2017).

In the paradigm examined in this paper, revived lobe emission represents synchrotron radiation from re-accelerated radio galaxy lobes. These are the 'radio-gischt' of Ensslin et al. (1998), Hoeft & Brüggen (2007), Iapichino & Brüggen (2012), in which the seed cosmic ray electrons are provided by the now-switched-off jet – as opposed to compressed fossil plasma which results in 'radio ghosts' (Enßlin & Gopal-Krishna 2001; Enßlin & Brüggen 2002; Kempner et al. 2004). Revived lobes have typical spectral indices  $\alpha \sim 1$ , consistent with our  $\epsilon = 5$  (s = 3) threshold, and we adopt this value here. We take  $\eta = 0.002$  for the remnant lobes, which yields magnetic fields at the several  $\mu$ G level, consistent with observations (Nakazawa et al. 2009; Finoguenov et al. 2010; Stroe et al. 2014). We note that  $\eta$  parametrises important MHD effects not captured in our hydrodynamic simulations, including dynamical amplification of magnetic fields.

The total emissivity at observed frequency  $\nu$  is calculated by combining adiabatic and radiative losses (details in Yates-Jones

et al. 2022). The number density normalisation factor  $n_0$  in Equation (A3) sets the normaliation of emissivity; it is constrained by the total energy injected by the pair of jets, each with kinetic power  $Q_{iet}$ ,

$$2Q_{j}t_{active} = \int_{V} u_{e} dV \qquad (A6)$$

$$= \int_{V} dV n_{0}m_{e}c^{2} \int_{\gamma_{\min}}^{\gamma_{\max}} (\gamma - 1)\gamma^{-s} d\gamma$$

$$\approx \int_{V} dV n_{0}m_{e}c^{2} \left(\frac{\gamma_{\min}^{-(s-1)}}{s-1}\right) \left[\left(\frac{s-1}{s-2}\right)\gamma_{\min} - 1\right]$$

where we have assumed electron-positron composition characteristic of FR-II jets (Hardcastle 2018), and  $\gamma_{min}$  and  $\gamma_{max}$  are the Lorentz factors corresponding to low and high energy cutoffs. The integral is insensitive to the choice of  $\gamma_{max}$  for typical values of s >2 and we make the usual assumption  $\gamma_{max} \rightarrow \infty$  (Kaiser et al. 1997; Turner & Shabala 2015), yielding the last approximate equality.

The final parameter required to calculate emissivity is the low-energy cutoff for the radiating particles,  $\gamma_{min}$ . Calculated

emissivities depend sensitively on this parameter: for spectra steeper than s = 2, the majority of electrons will have Lorentz factors just above  $\gamma_{min}$ . Observations of hotspots in powerful radio sources, similar to those simulated here, show  $\gamma_{min} \sim 500$  (e.g. in Cygnus A, Carilli et al. 1991; Stawarz et al. 2007; McKean et al. 2016 or slightly higher Godfrey et al. 2009). We adopt  $\gamma_{min} = 500$  for our radio galaxy modelling, noting that this value produces size-luminosity tracks consistent with observations of real radio sources (Turner et al. 2018a,b; Yates-Jones et al. 2022).

# Appendix B.3. Conservation of particle number density

Because we simulate the full duty cycle of jet activity, we are able to constrain the total number of emitting particles  $N_{\text{rad}}$ , evaluated at the time when the jet switches off.

The total number of radiating particles is

$$N_{\rm rad} = \frac{2Q_{\rm jet}t_{\rm active}(s-2)}{m_e c^2 \gamma_{\rm min}} \tag{A7}$$

We ensure that this quantity is conserved in the remnant phase of lobe evolution.