

DEPENDENCE OF LINEAR SIZES AND SPECTRAL INDICES OF EXTENDED  
RADIO GALAXIES ON REDSHIFT AND RADIO LUMINOSITY

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1. INTRODUCTION

Apart from the well known evolution in the space density of powerful radio sources, the maximum linear sizes and the spectral indices of extended radio sources could also evolve with epoch and it is important to investigate their epoch-dependence in order to understand the cosmological evolution of radio sources. Evidence for size evolution (in the sense that sources were smaller at earlier epochs) has been presented both from the angular size - redshift relation ( $\theta - z$ ) for quasars and from the angular size - flux density relation ( $\theta - S$ ) for all radio sources. Doubts have sometimes been expressed, however, mainly because it has been difficult to investigate the epoch dependence independent of a possible dependence on radio luminosity. Reasonably reliable estimates of the distances of radio sources have generally been limited to a relatively small range in flux density ( $S$ ), so that high redshift sources are also of high luminosity. An inverse correlation between linear size ( $\ell$ ) and radio luminosity ( $P$ ) is therefore hard to distinguish from a genuine evolution with epoch. A similar situation appears to hold for the spectral indices ( $\alpha$ ) of extended radio sources, which have generally been assumed to get steeper at higher radio luminosities (eg. Laing and Peacock 1980) but a dependence on epoch cannot at present be ruled out (Katgert-Merkelijn et al. 1980).

Recent availability of deep optical identifications and magnitudes together with high resolution mapping of weak radio sources now makes it possible to disentangle the two effects at least in the case of the linear sizes of extended radio galaxies. First attempts in this direction, which confirm the need for size evolution and suggest a direct relation between  $\ell$  and  $P$ , are presented in Sections 2 and 3. Future observations should soon enable this to be done also in the case of the spectral indices. The observed spectral index - flux density relation for sources selected from 408 MHz samples is discussed in Section 4 where we also remark on how the relation can constrain existing models for the evolution of the radio luminosity function which incorporate a correlation between  $\alpha$  and  $P$ , or between  $\alpha$  and  $z$ .

2. EPOCH DEPENDENCE OF LINEAR SIZES

The  $\theta$ - $z$  relation for radio galaxies in a relatively small range of  $P$ , and selected from 3 complete samples at 1.4 GHz has recently been shown (Kapahi 1985) to require evolution in source sizes. An updated version of the relation, based on the 4 samples listed in Table 1, is shown in Fig.1. Note that spectroscopic redshifts are available only for the brightest BDFL sample. The intermediate flux samples are taken from the GB/GB2 samples of radio galaxies defined by Machalski and Condon (1985), who have also estimated the redshifts from photometric data. The weakest flux sample is derived from the Leiden-Berkeley Deep Survey (LBDS; Windhorst 1984) and consists of sources that are either identified with galaxies with an  $F$  mag  $> 22$  or have no optical counterpart ( $F \geq 22.75$ ). Most such sources are expected to be radio galaxies at  $z \geq 0.8$ . All the samples should cover a fairly small range of  $P_{1.4 \text{ GHz}}$  between  $\sim 10^{24.6}$  and  $10^{26} \text{ WHz}^{-1} \text{ ster}^{-1}$  which also places the sources in FR luminosity Class II (fanaroff and Riley 1974).

It is clear from Fig. 1 that the linear sizes of radio galaxies of a constant luminosity depend on epoch. For simplicity, if the evolution is characterised by the relation  $\ell \propto (1+z)^{-n}$ , the parameter  $n$  appears to have a value between 1.5 and 2 depending on the value of  $q_0$  between 0 and 0.5

Evidence for size evolution is provided also by the observed  $\theta$  - $S$

Table 1. Radio galaxy samples at 1.4 GHz

Sample	$S_{1.4}$ (Jy)	range of $z$	$z_{\text{median}}$	no. of sources
BDFL	$\geq 2$	0.075 - 0.20	0.11	36
GB/GB2	$\geq 0.55$	0.15 - 0.40	$\sim 0.28$	25
GB/GB2	$\geq 0.2$	0.25 - 0.60	$\sim 0.45$	35
LBDS	$\geq 0.01$	0.8	$\sim 1$ to 2	43

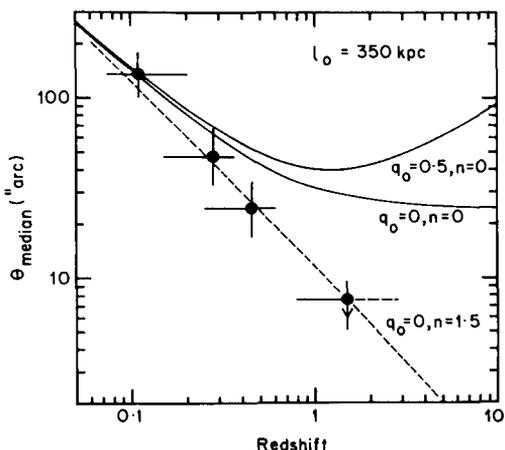


Fig.1. The  $\theta$ - $z$  relation for radio galaxies of constant radio luminosity



Kulkarni & Subrahmanya, in preparation). The predicted  $\theta$ -S relations from the 2.7 GHz parent sample for the 4 models of Peacock and Gull (1981) are shown in Fig. 2. We have also considered other parent samples (BDFL 1.4 GHz survey & 3CR) and evolutionary models (Condon 1984; Subrahmanya and Kapahi 1983). Size evolution was found to be necessary in every case.

### 3. LUMINOSITY DEPENDENCE OF LINEAR SIZES

By comparing the sizes of sources in the samples of Table 1 with those of radio galaxies in the same  $z$  interval in a bright source sample we can also investigate any dependence of  $\ell$  on  $P$ . The BDFL sample ( $S > 2$  Jy) would have been ideal for this purpose but for the fact that deep optical identifications and radio structures are still not available for many sources. We have therefore used the 3CR-LRL sample (Laing et al. 1983). The lower defining frequency of 3CR is unlikely to be serious for our purpose of investigating the sizes of steep-spectrum extended radio galaxies. The possible deficit of SSC and flat-spectrum compact sources (both are predominantly identified with quasars) in the 3CR compared to 1.4 GHz sample can be dealt with by excluding all sources with  $\ell < 30$  kpc from all the samples. The distribution of  $\ell$  in the LBDS (estimated  $z > 0.8$ ) and the 3CR-LRL (measured or estimated  $z > 0.8$ ) radio galaxies are shown in Fig 3. It is clear that the 3CR sources, which are likely to be about 2 orders of magnitude more luminous than the LBDS sources but in approximately the same redshift range, have considerably larger sizes suggesting a direct relation between  $\ell$  and  $P$ , contrary to an inverse relationship which is required to explain the angular size data without invoking size evolution.

The ratio of  $\ell_{med}$  (3CR) in the different  $z$  ranges to the corresponding

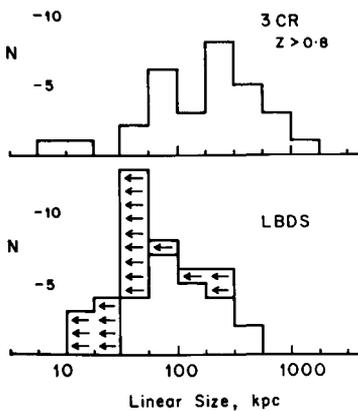


Fig.3. Distributions of  $\ell$  for sources at  $z > 0.8$ .  
 $q_0 = 0.5$ ;  $H_0 = 50 \text{ km s}^{-1} \text{ Mpc}^{-1}$

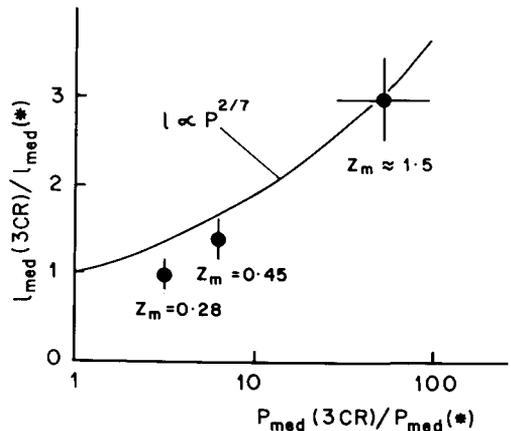


Fig.4. Ratio of  $\ell_{med}$  in the 3CR and 1.4 GHz samples (at constant  $z$ ) against the ratio of corresponding values of  $P_{med}$

values of  $\ell_{\text{med}} (*)$  in the 1.4 GHz samples of Table 1 is shown plotted against the ratios of the corresponding luminosities  $P_{\text{med}} (3\text{CR})/P_{\text{med}} (*)$  in Fig 4. It is interesting to note that the data are consistent with the simplest explanation for linear size evolution in terms of a denser intergalactic medium at earlier epochs. If the density of the IGM surrounding the radio galaxies varies as  $(1+z)^3$ , it is easily shown (to first approximation) by balancing the internal pressure in the hot spots ( $\propto P^{4/7} V^{-4/7}$ , where  $V$  is the Volume) with the ram pressure of the IGM  $\{ \propto (1+z)^3 v^2 \}$  that the average speed of advancement of the hot spot ( $v$ ) is proportional to  $P^{2/7} V^{-2/7} (1+z)^{-1.5}$ . Since  $\ell$  is likely to be proportional to  $v$  and the size of the hot spots is probably not strongly dependent on  $P$  or  $z$ , one may expect  $\ell \propto P^{2/7} (1+z)^{-1.5}$ . This appears to be consistent with the observed  $\ell$ - $z$  relation (at constant  $P$ ) and the  $\ell$ - $P$  relation at constant  $z$ . Although the above treatment is oversimplified the point is that  $\ell$  is indeed expected to be larger for higher luminosity sources.

4. THE SPECTRAL INDEX - FLUX DENSITY RELATION

Because of the statistical correlation between  $\alpha$  and  $P$  (or  $z$ ) the observed distributions of  $\alpha$  at different  $S$  can be useful in constraining evolutionary models of the RLF. This is particularly important at low  $S$  where little redshift information exists. The  $\alpha_{\text{med}}(S)$  relation for complete samples selected at 408 MHz, derived recently by Kapahi and Kulkarni (1986), is shown in Fig 5. The value of  $\alpha_{\text{med}}$  is seen to rise considerably from high to intermediate  $S$ . But between about 1 and 0.1 Jy there appears to be little change in  $\alpha_{\text{med}}$  ( $\sim 0.9$ ) contrary to the earlier results of Steppe and Gopalkrishna (1984) who found a significant flattening of  $\alpha_{\text{med}}$  with decreasing  $S$ . Their results at low  $S$

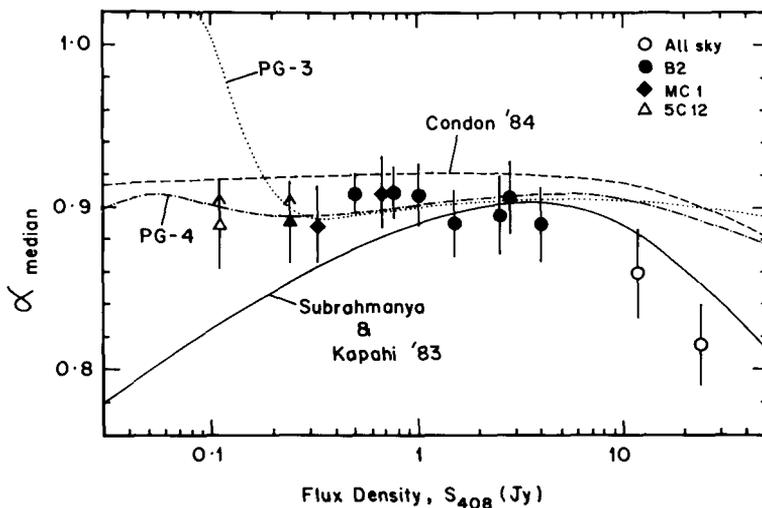


Fig.5. The observed  $\alpha$ - $S$  relation and predictions of evolutionary models of the RLF.

are likely to be affected by selection effects and scaling factors.

The predicted  $\alpha_{\text{med}}(S)$  relations for several models of the evolving RLF are also shown in Fig 5. Surprisingly none of the models (only 2 shown in Fig 5) of Peacock and Gull (1981) or of Condon (1984) fit the observed  $\alpha_{\text{med}}$  at high  $S$  where the models should be tightly constrained by the good redshift information already available. The discrepancy can be traced (Kapahi and Kulkarni 1986) to the low frequency turnover in the spectra of SSC sources which are assumed in the evolutionary models to have  $\alpha$  independent of frequency. This assumption leads to an overestimate in the number of high-luminosity SSC sources in strong source samples at low frequencies, the same effect that results in the predicted values of  $\theta_m$  at the high  $S$  (using a 2.7 GHz parent sample) to be lower than observed (Section 2; and Kapahi, Kulkarni and Subrahmanya, in preparation).

At the low  $S$  end the  $\alpha$ - $S$  relation can indeed provide important constraints to evolutionary models (Fig 5). But the detailed interpretation of the  $\alpha$ - $S$  relation at low  $S$  depends crucially on whether  $\alpha$  correlates with  $P$  or with  $z$ . Observations to determine the spectral indices of the LBDS sample of sources discussed in Sections 2 and 3 could help resolve this question.

#### REFERENCES

- Condon, J.J. 1984, *Astrophys. J.*, 287, 461  
 Downes, A.J.B. 1982, in Extragalactic Radio Sources, eds. Heeschen, D.S. & Wade, C.M., D.Reidel, Holland, p.393  
 Kapahi, V.K. 1985, *M.N.R.A.S.*, 214, 19P  
 Kapahi, V.K. & Kulkarni, V.K. 1986, submitted to *A & A*  
 Kapahi, V.K. & Subrahmanya, C.R. 1982, in Extragalactic Radio Sources, eds. Heeschen D.S. & Wade, C.M., D.Reidel, Holland, p.401  
 Katgert-Merkelij, J.K., Lari, C. & Padrielli, L. 1980, *A & A Suppl.*, 40, 91  
 Laing, R.A. & Peacock, J.A. 1980, *M.N.R.A.S.*, 190, 903  
 Laing, R.A., Riley, J.M. & Longair, M.S. 1983, *M.N.R.A.S.*, 189, 433  
 Machalski, J. & Condon, J.J. 1985, *Astron. J.*, 90, 973  
 Peacock, J.A. & Gull, S.F. 1981, *M.N.R.A.S.*, 196, 611  
 Peacock, J.A. & Wall, J.V. 1981, *M.N.R.A.S.*, 194, 331  
 Steppe, H. & Gopal-Krishna, 1984, *A & A.*, 135, 39  
 Subrahmanya, C.R. & Kapahi, V.K. 1983, in Early Evolution of the Universe and its Present Structure, eds. Abell, G.O & Chincarini, G., D.Reidel, p47  
 Windhorst, R.A. 1984, Ph.D Thesis, University of Leiden