

Is There a Relation between Duration and E_{iso} in Gamma-Ray Bursts?

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Abstract. The system of accretion disk and black hole is usually considered as the central engine of Gamma-ray Bursts (GRBs). It is usually thought that the disk in the central engine of GRBs is the advection-dominated accretion disk, which is developed from a massive (mass M_{disk}) torus at radius r_{disk} . We find a positive correlation between the isotropic gamma-ray energy E_{iso} and duration (so-called T_{90}) for GRBs. We interpret this correlation within the advection-dominated accretion disk model, associating E_{iso} and T_{90} with M_{disk} and viscous timescale respectively.

Keywords. Gamma-ray: bursts; accretion, accretion disks; black hole physics

1. Introduction

GRBs are the most luminous events observed at cosmological distances. The physics of GRBs remains as a great puzzle, especially that of the central engine. The burst duration T_{90} is generally regarded as a mark of the activity duration of the central engine. In general, the observed GRBs are classified into two groups by T_{90} divided at 2 s (Kouveliotou *et al.* 1993), i.e., long and soft GRBs *vs* short and hard GRBs, corresponding to two physical types of GRBs produced by deaths of massive stars and mergers of two compact objects, respectively. According to current understanding, whether long or short bursts, the progenitors all form a hyperaccreting black hole. Here we adopt the popular torus-accretion model for GRBs (Popham *et al.* 1999; Narayan *et al.* 2001; Liu *et al.* 2007). The total accretion mass is proportional to the accretion time in the model. Then the total energy radiated E_{iso} may be correlated with the duration T_{90} (see also Gehrels *et al.* 2009).

2. Data and Implication

Data. Data on fluence and T_{90} are obtained from: <http://swift.gsfc.nasa.gov/docs/swift/archive/grbtable/> (Swift data) and <http://heasarc.gsfc.nasa.gov/W3Browse/fermi/fermigtrig.html> (Fermi data) up to September of 2012. GRBs with both short and long duration are included. The left and middle panels of Fig. 1 show the correlation between the fluence and T_{90} . As shown in the plot, the fluence is proportional to $T_{90}^{0.62 \pm 0.02}$ for the *Fermi* data (left) and $T_{90}^{0.56 \pm 0.03}$ for the *Swift* data (middle). We further analyze the sources with known redshift in the *Swift* sample. For these GRBs, we find that $E_{\text{iso}} \propto [T_{90}/(1+z)]^{1.01 \pm 0.15}$, as shown in the right panel of Fig. 1. In addition, the short and long GRBs almost have the same trend in the right panel except GRB 060218, which is a low luminous GRB and may have different progenitor (Gehrels *et al.* 2009).

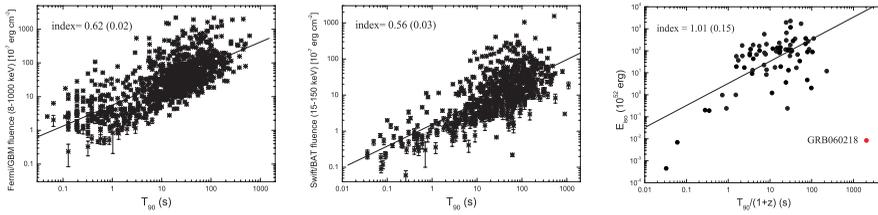


Figure 1. Left and middle panel: Fluence vs T_{90} . Right panel: E_{iso} vs T_{90}

Implication. In order to understand the correlation obtained in the above statistics, we investigate the physical origin within the framework of the GRB-type accretion disk model. Since $H \sim r$ in the advection-dominated accretion disk, we have $t_{\text{vis}} \sim \alpha^{-1} \Omega_K^{-1}$. To simplify, we assume that the accreting mass M_{disk} is deposited at the radius r_{disk} . Then, the timescale of the disk mass M_{disk} falling into the black hole corresponds to the viscous timescale. The equation can be described as (e.g., Narayan *et al.* 2001)

$$t_{\text{vis}} \sim 2.7\alpha^{-1} \left(\frac{M_{\text{BH}}}{M_{\odot}}\right)^{-1/2} \left(\frac{r_{\text{disk}}}{10^9 \text{cm}}\right)^{3/2} \text{ s}, \tag{2.1}$$

$$M_{\text{disk}} \sim 2\pi r_{\text{disk}} \Sigma \Delta r. \tag{2.2}$$

If the r -dependence disk surface density Σ is $\Sigma \propto r^s$ and $\Delta r \propto r$, then we can get

$$M_{\text{disk}} \propto t_{\text{vis}}^{\frac{2(2+s)}{3}} \propto t_{\text{disk}}^{\frac{2(2+s)}{3}}. \tag{2.3}$$

If we assume the T_{90} equals the accretion time and the E_{iso} be proportional to the total mass of the disk, we can derive,

$$E_{\text{iso}} \propto T_{90}^{\frac{2(2+s)}{3}}. \tag{2.4}$$

Comparing the above equation with $E_{\text{iso}} \propto T_{90}$, we get $s \simeq -0.5$.

3. Conclusion and Discussion

We consider that the disk of GRB is an advection-dominated disk in which the mass of the disk M_{disk} is deposited at the radius r_{disk} . The accretion timescale of the disk into black hole corresponds to the viscous timescale. The correlation between E_{iso} and T_{90} obtained in statistics for GRBs can be qualitatively explained in the above model.

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