

# THE JOURNAL OF SYMBOLIC LOGIC

## **Edited by**

Enrique Casanovas, *Coordinating Editor*

Matthias Aschenbrenner

Steve Awodey

Veronica Becher

Lev Beklemishev

Michael Benedikt

Damir Dzhafarov

Stephen Jackson

Hiroshi Sakai

Thomas Strahm

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The JOURNAL invites submission of original scholarly work in mathematical logic and its applications.

### Editors

Enrique Casanovas (Coordinating Editor)

Department of Mathematics and Computer Science, University of Barcelona, Gran Via 585,  
08007 Barcelona, Spain

(e.casanovas@ub.edu) ;

Matthias Aschenbrenner

Department of Mathematics, University of California, Los Angeles, Box 951555, Los Angeles,  
CA 90095-1555, USA

(matthias@math.ucla.edu) ;

Steve Awodey

Department of Philosophy, Carnegie Mellon University, 5000 Forbes Avenue, Pittsburgh, PA 15213, USA

(awodey@cmu.edu) ;

Veronica Becher

Departamento de Computación, Facultad de Ciencias Exactas y Naturales, Universidad de Buenos Aires,  
Pabellón I, Ciudad Universitaria C1428EGA, Buenos Aires, Argentina

(vbecher@dc.uba.ar) ;

Lev Beklemishev

Steklov Mathematical Institute of RAS, Gubkina str. 8, 119991 Moscow, Russia

(lbekl@yandex.ru) ;

Michael Benedikt

Department of Computer Science, Oxford University, Wolfson Building, Parks Road, Oxford,  
OX1 3QD, UK

(michael.benedikt@cs.ox.ac.uk) ;

Damir Dzhafarov

Department of Mathematics, University of Connecticut, 341 Mansfield Road U1009, Storrs,  
CT 06269-1009, USA

(damir@math.uconn.edu) ;

Stephen Jackson

Department of Mathematics, University of North Texas, General Academics Building 435,  
1155 Union Circle #311430, Denton, TX 76203-5017, USA

(stephen.jackson@unt.edu) ;

Hiroshi Sakai

Graduate School of System Informatics, Kobe University, 1-1 Rokkodai-cho, Nada-ku, Kobe,  
657-8501, Japan

(hsakai@people.kobe-u.ac.jp) ;

Thomas Strahm

Institut für Informatik, Universität Bern, Neubrückestrasse 10, CH-3012 Bern, Switzerland

(strahm@iam.unibe.ch) .

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