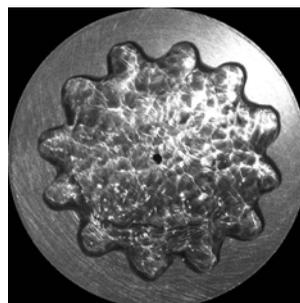


The crackling sound of Leidenfrost stars

P. Brunet[†]

Laboratoire Matière et Systèmes Complexes, UMR CNRS
7057, 75205 Paris CEDEX 13, France



Liquid drops deposited on a hot plate can experience a boiling crisis, when the vapour flux is strong enough to ensure the levitation of the drop and the relative insulation of the liquid from the solid. It is often denoted Leidenfrost effect, after the German Johann Gottlob Leidenfrost, who first reported it in 1756. While many studies have encompassed various applied issues associated with this phenomenon, aiming to control and prevent its appearance, Ma & Burton (*J. Fluid Mech.*, vol. 846, 2018, pp. 263–291) focused on the spontaneous appearance of a standing wave at the free surface, together with temporal oscillations, making the drop adopt the shape of a star. Their far-reaching study presents exhaustive results using six different liquids with a range of different volumes and temperatures, in which they systematically extracted the drop dynamics together with the pressure fluctuations in the vapour cushion below.

Key words: capillary waves, drops and bubbles, waves/free-surface flows

1. Introduction

The repeated fascination of fluid dynamists to study drops in various situations often comes about because this apparently simple system behaves as a model oscillator. The balance between fluid inertia and surface tension that tends to restore the surface of minimal energy, yields $f \simeq (\gamma/\rho R^3)^{1/2}$ as a natural frequency for the oscillations, where γ and ρ are the surface tension and density of the fluid and R is the drop radius. However, liquid–substrate friction often dramatically attenuates the dynamics. Still, there exist situations where friction with the substrate vanishes, making the liquid drop very mobile, for instance when a thin air cushion intercalated in between keeps the drop in levitation.

The Leidenfrost effect (Leidenfrost 1756) provides a situation of very weak friction, and has been the subject of numerous studies with both fundamental and applied scopes (Quéré 2013). In metallurgy, one tries to avoid it, as it is detrimental for a sharp quench in temperature, which is required for the best mechanical properties,

[†] Email address for correspondence: philippe.brunet@univ-paris-diderot.fr

by dramatically limiting heat transfer between the alloy and the surrounding cooling liquid. Conversely, it can be utilised on purpose to move droplets uphill on sloping substrates (Linke *et al.* 2006). In Jules Vernes' book, Michel Strogoff's blindness was prevented thanks to this salutary effect, helped by a few tears, after a red-hot sword blade was put on his eyes. Holter & Glasscock (1952) were the first to report spontaneous oscillations of star-shaped drops, and opportunely published it in a journal of acoustics. Others later investigated these oscillations (Adachi & Takaki 1984) and questioned their origin. A Marangoni effect due to a temperature gradient developing between the centre and the periphery of the drop was proposed (Tokugawa & Takaki 1994). On the other hand, Brunet & Snoeijer (2011) and Bouwhuis *et al.* (2013) reported similar behaviour for a drop sitting on an air cushion blown from below at room temperature, which dismissed the aforementioned mechanism. The star shapes are reminiscent of other situations where drops are driven by external time-periodic fields, e.g. substrate vibrations, acoustic modulation, fluctuating magnetic field (Brunet & Snoeijer 2011), except that in the levitated drops there is no periodic forcing. Hence a purely hydrodynamic instability was invoked (Bouwhuis *et al.* 2013).

Since a perfectly non-wetting drop adopts the shape of a puddle of height $h = 2l_c$, where $l_c = (\gamma/\rho g)^{1/2}$ is the capillary length, when such an instability leads to a time-periodic vertical motion of the drop centre of mass, the effective gravity g_{eff} that the drop feels becomes modulated in time and so do the capillary length and drop height. Because of volume conservation, the drop radius R is also subjected to this modulation. Hence, given the general expression of the drop eigenfrequency f stated above, it becomes clear that drop oscillations are induced by a parametric forcing. But the underlying mechanism of the instability remains ill-understood, as shown by several seemingly contradictory results on the dependence of frequency on drop radius (Bouwhuis *et al.* 2013; Caswell 2014; Ma, Lietor-Santos & Burton 2017).

2. Overview

Ma & Burton (2018) present exhaustive experiments with six different fluids and a large range of temperatures and drop volumes. Thanks to the slight curvature of the substrate, they could keep stable large drops ($R > 4l_c$) that otherwise would have broken under the action of a growing bubble of vapour below (Snoeijer, Brunet & Eggers 2009); hence they observed vibrating drops with wavenumber n from 2 to 13, and R up to 2.4 cm. Furthermore, they measured the pressure underneath the drop, and found that the appearance of the instability goes hand in hand with pressure fluctuations, of typical frequency f_p . Also, they used a smart visualisation technique that evidenced capillary waves not only on top and at the edge of the drop, but also underneath. A sketch of their system is depicted in figure 1. One of their most striking results is the independence of f_p (and so of the frequency of the drop oscillations f_d) and azimuthal wavelength λ_d on the drop radius. They found that f_d is dependent only on l_c , which is dependent only on liquid properties. Figure 2(a) shows an oscillating drop from below, where both the external corrugation and capillary waves below are visible. Figure 2(b) is the corresponding power spectrum that evidences the selection of frequency for these waves. The wavenumber n self-adapts and is found to increase linearly with the radius, $n \sim R$.

These results seem in sharp disagreement with previous ones which showed a significant dependence of f_d on R (Adachi & Takaki 1984; Bouwhuis *et al.* 2013; Caswell 2014). However, the latter studies examined the situation of smaller droplets ($R < 4l_c$), for which Ma & Burton explain the dependence on R with an analytical approach.

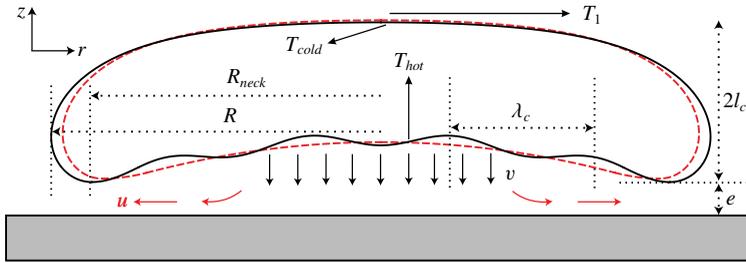


FIGURE 1. The overall sketch of the drop levitating on its own vapour underneath.

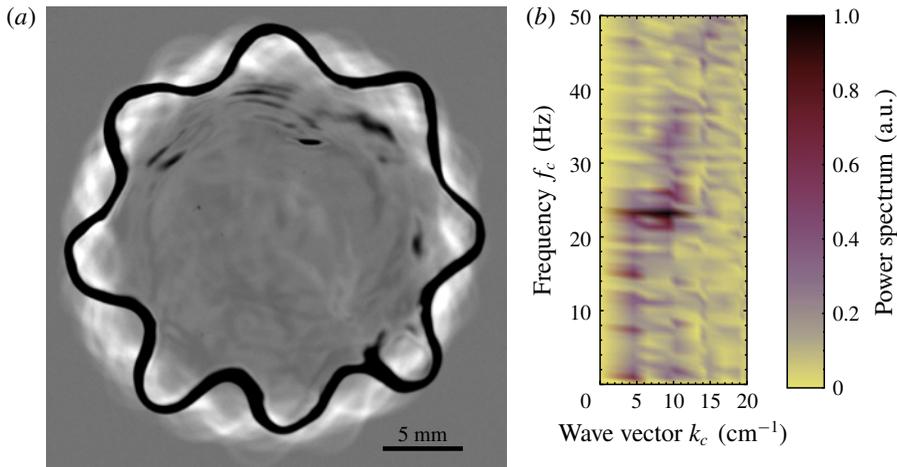


FIGURE 2. (a) A star-shaped drop of acetone levitating on its own vapour, viewed from below, and the radial capillary waves underneath. (b) The corresponding power spectrum in frequency and wavenumber.

Ma & Burton's measurements and analysis of air flow suggest that the selection on f_p (and then on f_d and λ_d) originates from gravity–capillary waves provoked by the shear stress exerted on the vapour–liquid interface, which explains why oscillations appear above a threshold in temperature or in air flow. This analysis also reconciles the different measurements obtained for small drops and large puddles. These waves cannot develop under too small drops, as their wavelength $\lambda_c \simeq 3.03l_c$ would then be larger than R . Instead, the profile underneath takes the shape of a bubble with a 'nip', i.e. a region of minimal air thickness, where most of the viscous stress responsible for lubrication-induced levitation takes place (Snoeijer *et al.* 2009). The radius R remains the only length scale in the radial direction, and the selection of f_p is set by R . Conversely the air layer under large puddles on curved substrates can exhibit several of these minima (see figure 2 in Ma & Burton 2018), with λ_c being the distance between them. Therefore, λ_c becomes the radial length scale selected by the hydrodynamics, which sets the selection of f_p independently of R . It is insightful to revisit previous measurements in light of Ma & Burton's, as one sees more clearly that the power-law decrease of f_d with R holds only for R smaller than $2l_c$ (roughly 5 mm for water) (Adachi & Takaki 1984; Bouwhuis *et al.* 2013), while f_d seems to reach a plateau for larger R .

Overall, with systematic and exhaustive measurements, Ma & Burton unveil the complex hydrodynamical mechanism and frequency selection process that lead to vibrating Leidenfrost star drops. Not only do their measurements with large puddles complete the previous ones, but their analysis explains the selection of frequency over the whole range of drop size.

3. Future

Remaining questions first concern the selection of f_p and how its mechanism should hold under different conditions. For instance, it would be interesting to check how an undulated substrate, with period ranging between l_c and λ_c , could trigger or hinder oscillations and modify the selected f_p . Another possibility would be to address these questions under different conditions, like drops sandwiched in a Hele-Shaw cell (Celestini *et al.* 2014).

Finally, one can wonder whether or not these oscillations could be converted into audible sound waves (f_p higher than 50 Hz), if higher harmonics appear or even if the fundamental has a high enough frequency, as in Celestini *et al.* (2014). Incidentally, the analogy between these drops and some musical instruments is especially striking. Think of a wind instrument with a vibrating reed, such as a clarinet (Wolfe 2018). Depending on how strongly the performer blows, and on the length of the pipe, either the eigenmode of the reed is excited (a so-called ‘burn note’ generally unsuitable in a musical performance) or the selected sound is due to the vibration of the air column in the pipe (Helmholtz resonator), which couples to the reed vibrations and makes a nice and controlled sound. The levitating drops, depending on their size, are also susceptible to excite vibration modes that are either intrinsic to their size or are tuned by the capillary length intrinsic to the liquid.

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