

To find k , let the arc diminish and tend to zero, then the ratio chord : arc $\rightarrow 1$, and $OG_1 \rightarrow$ the radius, hence finally

$$OG = \text{radius} \times \frac{\text{chord}}{\text{arc}}.$$

D. M. Y. SOMMERVILLE.

✕ Nomogram for the Solution of the Equation

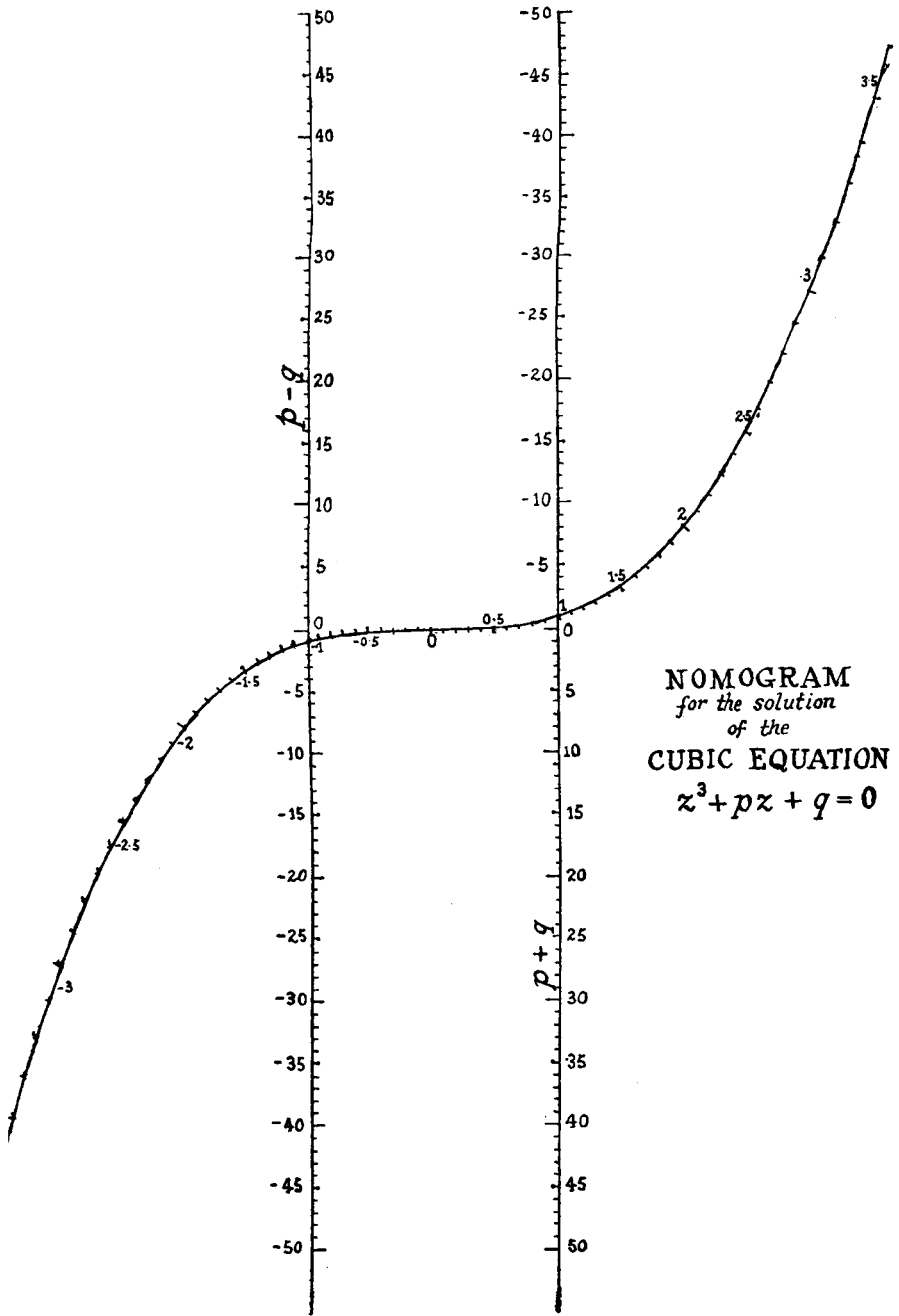
$$z^3 + pz + q = 0.$$

The curve $y = x^3$ is constructed with a scale of 1" horizontally and $\frac{1}{10}$ " vertically. It is graduated with the values of x . Then draw the two lines $x = \pm 1$ and graduate them on the scale of the y -axis, $x = +1$ positive downwards, $x = -1$ positive upwards.

To solve the equation $z^3 + pz + q = 0$, set $p + q$ on the line $x = +1$ and $p - q$ on the line $x = -1$. Join the two points and get the intersections with the curve. The accompanying diagram has only a range between ± 3.5 , but it is easy to divide the roots by 2, 3, or 10. If accurately drawn, it should give two figures of the root with ease, as a rule, and may give three. Sometimes, of course, it may be difficult to separate the roots, e.g. in the equation $z^3 - 13z + 18 = 0$. The line seems to touch about $+2.2$, and the 3rd root is off the paper. Dividing the roots by 2, we get $z^3 - 3.25z + 2.25 = 0$. We see that 1 is a root, another root is -2.08 , and therefore the third root is $+1.08$. Hence the roots of the given equation are 2, 2.16, -4.16 .

I find it convenient to use, instead of a ruler, which hides part of the diagram, a strip of celluloid with a fine line ruled on the lower surface.

D. M. Y. SOMMERVILLE.



NOMOGRAM
for the solution
of the
CUBIC EQUATION
 $z^3 + pz + q = 0$