Correspondence.

## ON THE ADAPTATION OF ASSURANCE FORMULÆ TO THE ARITHMOMETER OF M. THOMAS.

## To the Editor of the Assurance Magazine.

SIR,-In adapting assurance formulæ to the processes that may be wrought on M. Thomas de Colmar's Arithmometer, the following expressions have occurred to me. They appear to be worthy of record, and I therefore submit them to you.

For simplicity of notation, let

 $l = l_x$  or  $l_{xy}$ , &c., *i.e.*, expressions into which only *lives* enter;

 $d=d_x$  or  $d_{xy}$ , or  $d_x l_{y+\frac{1}{2}}$ , &c., expressions into which deaths enter;  $r = (1+r)l_x$  or  $(1+r)l_{xy}$ , &c., expressions into which the rate of interest enters;

 $a = a_x$  or  $a_{xy}$ , &c., annuities of all kinds;

A=A, or  $A_{x,y}$ , or  $A_{1,y}$ , &c., assurances of all kinds;

also let  $l_1$ ,  $a_1$ ,  $A_1$ , be the same, but advanced one year;

then in all cases 
$$a = \frac{a_1 l_1 + l_1}{r}$$
 . . . . . (1)  
and  $A = \frac{A_1 l_1 + d}{r}$  . . . . . . (2)

Of these equations, the first, in the form  $a = \frac{(1+a_1)l_1}{a_1}$ , is well known; the second is, to me at least, new; and both, for mechanical computation, are very convenient. Being symmetrical they are easy to remember.

The subjoined small table will enable any of your readers, who may be so disposed, to try these methods. I do not propose them as the fittest for working by hand, but I am persuaded that the days of hand work in the actuary's craft are coming to an end. The arithmometer is not an expensive machine, and its speed and certainty are invaluable.

I am, Sir,

Kingstown (near Dublin), 18th March, 1865. Yours very truly, J. HANNYNGTON.

Carlisle Table, 3 per Cent. Difference of Ages, 3 Years.

x.	$d_x$	l <sub>x</sub> .	l <sub>x+3</sub> .	$d_x l_{y+\frac{1}{2}}$ .	<i>l<sub>x y</sub></i> ,	$(1+r)l_{x}$	$(1+r)l_{xr}$	y.	a <sub>z</sub> .	$A_{\frac{1}{x,y}}.$
98	3	14	12.5	79.5	420	14.42	432.60	95	2.3883366	4829954
99	2	11	10	41	253	11.33	260.59	96	$2 \cdot 1308922$	·5116357
100	2	9	8	32	162	9.27	166-86	97	1.6825565	.5699206
101	2	7	6	25	98	7.21	100.94	98	1.2281855	6438465
102	2	5	4	20	55	5.15	56.65	99	0.7710435	.7270884
103	12	3	2	16	27	3.09	27-81	100	0-3236246	7847984
104	17	ĩ	0.5	6	7	1.03	7-21	101	0.0000000	-8321775
104	1 *	1		, v	1	1	1	101	0000000	0021110
$a_{x} = \frac{(1+a_{x+1})l_{x+1}}{(1+r)l_{x}};  \mathbf{A}_{x} = \frac{\mathbf{A}_{x+1}l_{x+1} + d_{x}}{(1+r)l_{x}};  \mathbf{A}_{\frac{1}{x\cdot y}} = \frac{\mathbf{A}_{\frac{1}{(x\cdot y)+1}} + d_{x}l_{y+\frac{1}{2}}}{(1+r)l_{x\cdot y}}.$										
At the highest age $l_{11}$ and $a_{22}$ . At the highest age A <sub>1</sub> vanishes.										
both vanish and at the area next $(x,y)+1$										
and the expression becomes										
below $a_{x+1}$ vanisnes; the initial $d$										
value is, therefore, $\frac{l_{x+1}}{(1+r)l_x}$ , $\frac{a_x l_{y+2}}{(1+r)l_{xy}}$ .										
where $x = 103$ .										