

SHAPE ANALYSIS OF CUMULATIVE PROBABILITY DENSITY FUNCTION OF RADIOCARBON DATES SET IN THE STUDY OF CLIMATE CHANGE IN THE LATE GLACIAL AND HOLOCENE

Danuta J Michczyńska¹ • Anna Pazdur

Radiocarbon Laboratory, Institute of Physics, Silesian University of Technology, Krzywoustego 2, 44-100 Gliwice, Poland.

ABSTRACT. We report on a statistical analysis of a large set of radiocarbon dates for reconstruction of paleoclimate. Probability density functions were constructed by summing the probability distributions of individual ¹⁴C dates. Our analysis was based on 2 assumptions: 1) The amount of organic matter in sediments depends on paleogeographical conditions; 2) The number of ¹⁴C-dated samples is proportional to the amount of organic matter deposited in sediments in the examined time intervals. We quantified how many dates are required to give statistically reliable results. As an example, 785 peat dates from Poland were selected. The dates encompassed the Holocene and Late Glacial period. All dates came from the Gliwice Radiocarbon Laboratory. Results were compared with other paleoenvironmental records. Detailed analysis of the frequency distributions showed that preferential sampling plays an important part in the shape determination. The general rule to take samples from locations where visible changes of sedimentation are apparent (e.g. from the top and the bottom of the peat layer) results in narrow peaks in the probability density function near the limits of the Holocene subdivision.

INTRODUCTION

Since the 1970s, analyses of frequency distributions of radiocarbon-dated samples over restricted timescales have been carried out for several selected geographic regions. Geyh and Streif (1970) used 330 ¹⁴C dates of sediments from lagoons and tidal flats in the Netherlands, Niedersachsen, and Schleswig-Holstein to investigate sea-level variations on a regional scale. The basic assumption of their study was that ¹⁴C dates could be expected only for periods in which intensive peat formation occurred. In 1980, Geyh presented a Holocene North Sea sea-level history based on a set of 641 ¹⁴C dates. In the same article, the limitations of the statistical evaluation of ¹⁴C dates using histograms were discussed. Pazdur and Pazdur (1986b) analyzed the frequency distribution of ¹⁴C dates between arbitrarily chosen limits of 10 and 15 kyr BP. They used all the ¹⁴C dates made before 1985 in the Gliwice Radiocarbon Laboratory for the territory of Poland to construct a cumulative histogram. The authors found prominent maxima corresponding to the interstadials of Bölling and Alleröd, and the minima of the Older and Younger Dryas. Also, the beginning of the Holocene was marked by a sharp increase in the frequency of ¹⁴C dates. In turn, Goździk and Pazdur (1987) analyzed the frequency of ¹⁴C dates from the territory of Poland in the time interval from 12 to 45 kyr BP based on a set of 193 samples. Although, in the authors' opinion, a significantly larger set of ¹⁴C dates was necessary to draw detailed conclusions, the frequency distribution revealed good agreement with conclusions drawn from geological, paleobotanical, and geomorphological evidence and they suggested the dates would be useful in reconstruction of paleoclimate. Pazdur et al. (1995) presented the age distribution of speleothems from the Kraków-Wieluń Upland, southern Poland. The principal period of speleothem deposition fell within the Holocene; in particular, the maximum peak of the probability density approximately fitted the climatic optimum of the Holocene (i.e. Atlantic period). The older dates ranged from 48 to 20 kyr. These boundaries coincided almost exactly with the Interplenivistulian climatostratigraphic unit. ¹⁴C dating, which was primarily used simply to determine the age of sediment-containing samples, became an important source of information on the development of some geologic processes in the past. It should be stressed that the analysis of the frequency distribution of results from other dating methods has also been used in paleoclimate study.

¹Corresponding author. Email: djm@radiocarbon.gliwice.pl.

Herman (2000) presented an attempt to utilize the U/Th dates of speleothems as a source of paleoclimatic data. She also presented a detailed review of earlier studies concerning the analysis of growth frequency curves of cave speleothems. The speleothem deposition intensity is influenced by the changing climate, which is reflected in a clustering of dating results in certain time intervals. An example of a frequency distribution of 456 results of TL dating of loess samples was discussed by Singhvi et al. (2001) and Bluszcz and Michczyński (1999).

We report on a statistical analysis of a large set of ^{14}C dates for the reconstruction of the paleoenvironment. Our analysis was based on 2 assumptions:

1. The amount of organic matter in sediments depends on paleogeographical conditions.
2. The number of ^{14}C -dated samples is proportional to the amount of organic matter deposited in sediments in studied time intervals.

When the criteria for including ^{14}C dates in an analyzed set are chosen suitably (Geyh 1980; Goździk and Pazdur 1987; Stolk et al. 1994), fluctuations in the constructed cumulative distribution reflect changes of the investigated geologic phenomenon. The cumulative probability density function (CPDF) is created by superposition of individual Gaussian distributions for each ^{14}C date. Analysis of the shape of the CPDF may allow periods with favorable conditions for sedimentation (peaks of CPDF) or unfavorable conditions (gaps of CPDF) to be determined. But the key question is whether peaks and gaps are the result of environmental changes in the past or statistical and sampling fluctuations. In other words: How does one test accurately if the analyzed CPDF is significantly different from the uniform CPDF? How many dates are required to give reliable results? Geyh discussed such problems for histograms (Geyh 1980) and distinguished 3 kinds of histograms according to the value of the parameter s describing statistical fluctuations:

- Reliable histograms, $s \leq 20\%$
- Common histograms, $50\% < s < 20\%$
- Unreliable histograms, $s \geq 50\%$

In his article, the studied time interval is divided in a number of classes. The number of dates belonging to a certain class l is a random variable. If the number of ^{14}C dates in the studied time interval is large, then this variable can be described by Poisson statistics. In such situations, the statistical fluctuation s , which can be expressed as the ratio of the expected value and dispersion, is easy to calculate.

METHODS

In the case of CPDFs, the situation is a little more complicated. To estimate the range of statistical fluctuation for CPDFs, we carried out a Monte Carlo experiment for different values (N) of the number of ^{14}C dates in the sets ($N = 50, 100, 200, 500, 1000,$ and 2000), and for different values of the mean uncertainties $\Delta T = 50, 70, 100, 120, 150,$ and 200 yr. We assumed that the N ^{14}C dates are uniformly distributed in the time range of 0–14 kyr. For simplification, we assumed that all dates have the same uncertainty. Using the Monte Carlo method, we generated 10,000 CPDFs for each pair of N and ΔT values. On the basis of the 10,000 CPDFs, we estimated the fluctuation range as 95% confidence intervals. The results obtained for $\Delta T = 120$ yr and different N values and for $N = 500$ dates and different uncertainty values are presented in Figure 1. To compare our results with evaluations for histograms, the parameter s_f which describes statistical fluctuations, was calculated. The results are presented in Figure 2. In comparison with histograms, CPDF is characterized by lower statistical fluctuations, e.g., we need 1530 dates with a mean uncertainty of 115 yr for the time range 0–14 kyr

BP to give reliable (according to the criteria proposed by M Geyh) results for histograms, but we would need about 785 dates for the CPDF. The minimum number of dates for the case $\Delta T = 120$ yr is equal to 125 and for $\Delta T = 115$ yr is equal to 200 dates.

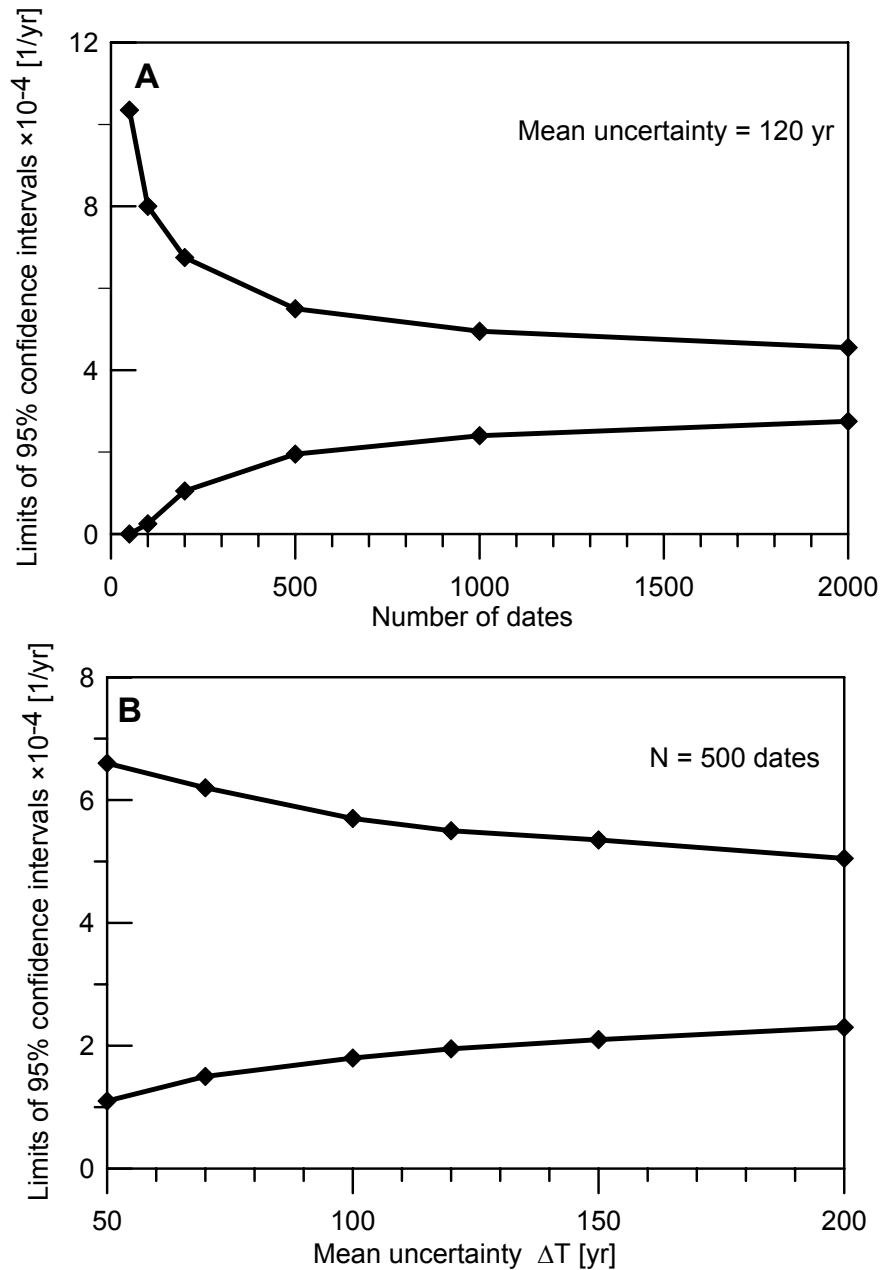


Figure 1 Values of 95% confidence intervals versus number of dates (a) and value of mean uncertainty (b). Part A shows the results for the number of dates $N = 50, 100, 200, 500, 1000,$ and $2000,$ assumed mean uncertainty 120 yr. Part B presents the results for a set of 500 ^{14}C dates and different values of the mean uncertainty $\Delta T = 50, 70, 100, 120, 150,$ and 200 yr.

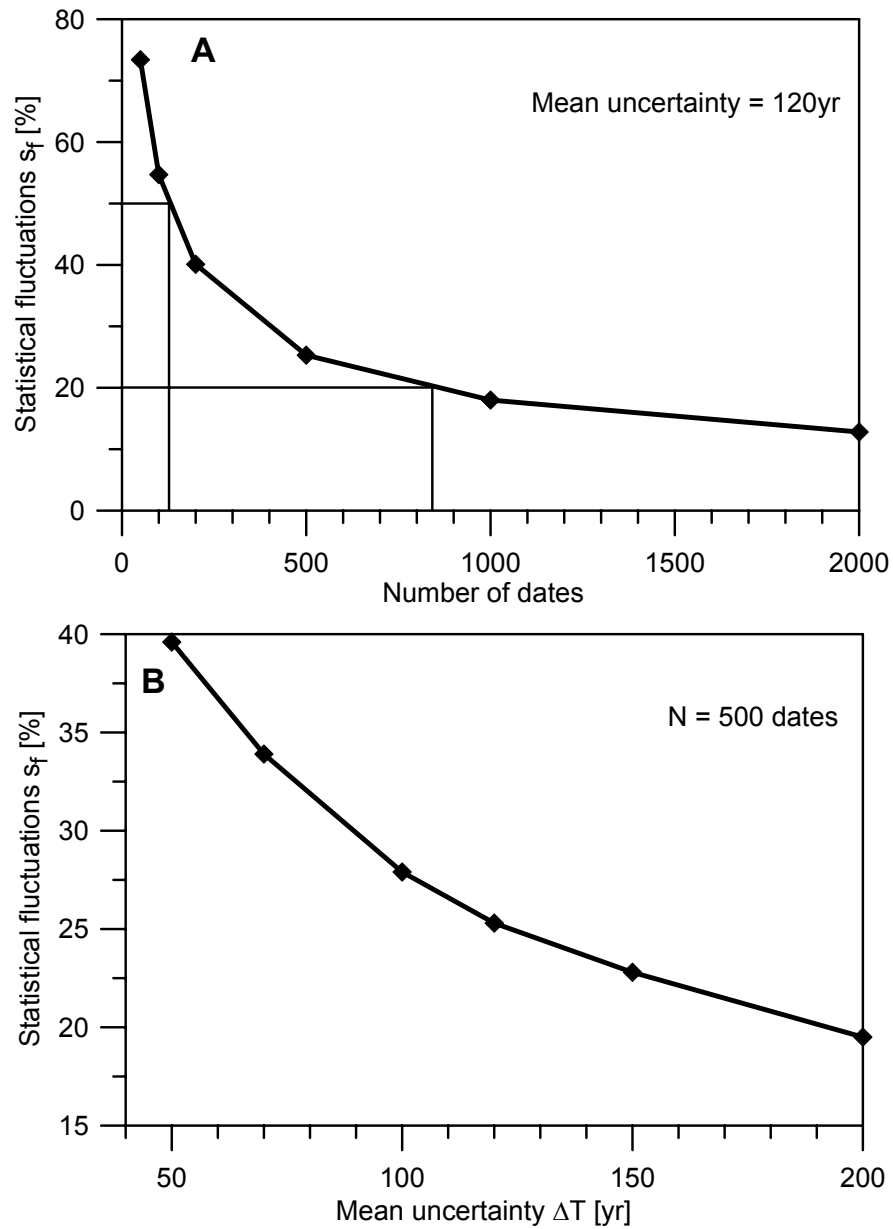


Figure 2 Statistical fluctuations s_f value versus number of dates (a) and mean uncertainty value (b)

In order to estimate the minimum number of dates needed for construction of a reliable CPDF, we did the following:

1. Created a set of 1000 ^{14}C dates (using a random number generator) and calculated the appropriate CPDF;
2. Randomly sampled N_i dates from the set of 1000 dates;
3. Calculated $CPDF_i$ for the selected N_i dates;

4. Calculated the sum of squared deviation between the original (constructed for 1000 dates) CPDF and the secondary (constructed for N_i dates) $CPDF_i$;
5. Repeated steps 2–4 one hundred times and calculated the mean sum of squared deviations MSSD;
6. Repeated steps 2–6 for $N_i = 50, 100, 150, \dots, 950$ dates.

The relationship between the mean sum of squared differences and number of dates is shown in Figure 3. We carried out the experiment for the case mean $\Delta T = 115$ yr. Faster changes of MSSD are characteristic for lower N_i values. The larger the number of dates, the smaller the MSSD value. On the basis of this simulation, we chose $N_i = 200$ as the minimum number of dates needed for the construction of a reliable CPDF. Hercman (2000) described a similar experiment for the set of $^{230}\text{Th}/^{234}\text{U}$ dates. She proposed 150 as the minimum number of $^{230}\text{Th}/^{234}\text{U}$ dates for the analyzed time range 0–200 kyr.

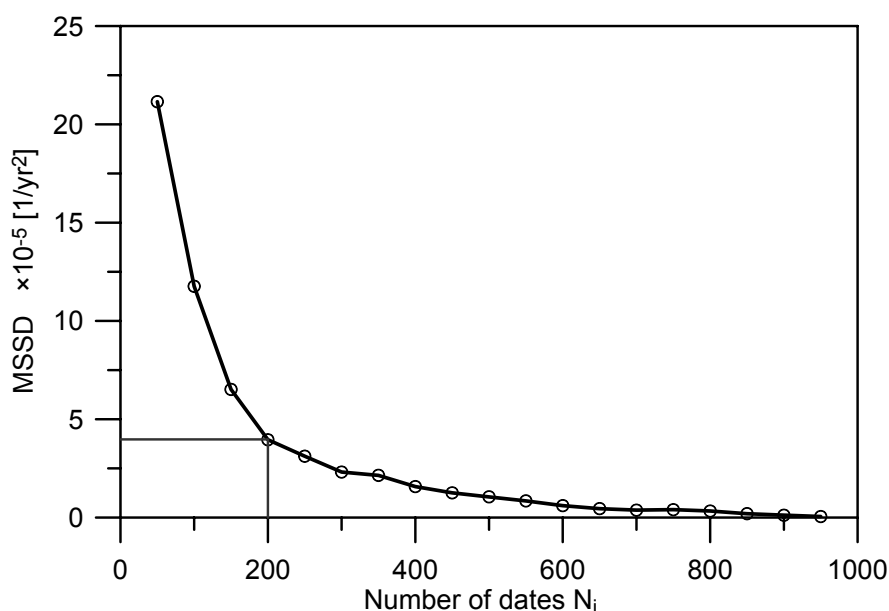


Figure 3 Results of the shape experiment e ; Mean sum of squared deviations MSSD between the original (constructed for 1000 dates) CPDF and secondary (constructed for N_i dates) $CPDF_i$.

The Monte Carlo experiment provides evidence about how the CPDF constructed for a certain set of ^{14}C dates may differ considerably from the CPDF constructed for the same number of dates but uniformly distributed on a ^{14}C timescale. The experiment gives no information about the significance of particular maxima and minima. This significance could be established by a Monte Carlo experiment using a random number generator with the same distribution as the real distribution of sedimentation of the investigated type of sample. Unfortunately, the real distribution is unknown. To estimate it, the “Bootstrap Method” (Efron and Tibishrani 1993; Hercman 2000) may be used. This method assumes only that the chosen set of dates is representative of the sediment type over the investigated time period. The scheme of the Bootstrap Method algorithm is shown in Figure 4, and illustrative 95% confidence intervals calculated for a set of 785 dates of peat from the territory of Poland (see “Analyzed Material”) are shown in Figure 5.

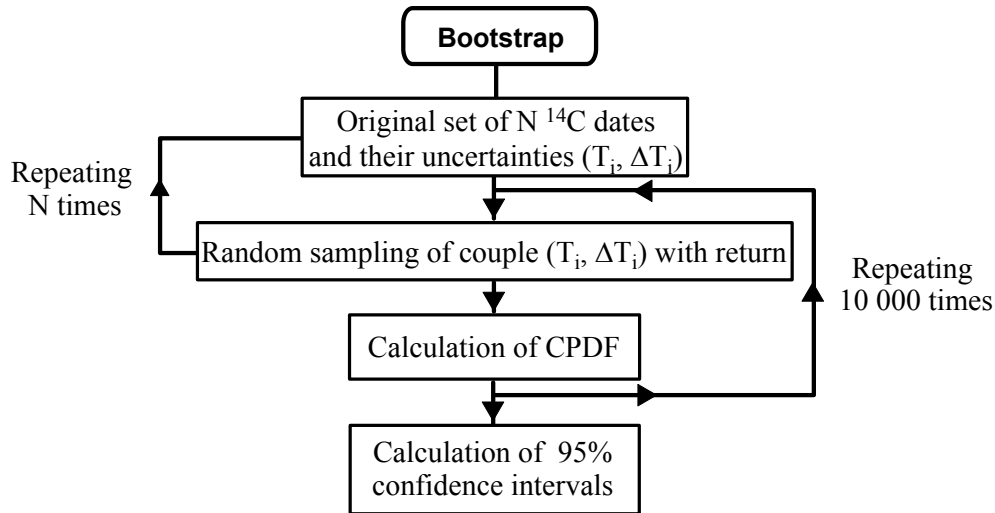


Figure 4 Scheme of the Bootstrap experiment

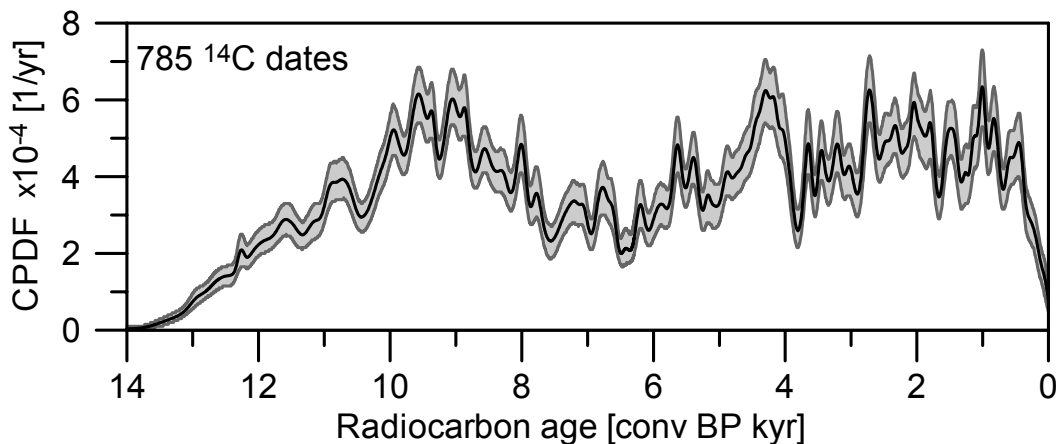


Figure 5 An example of 95% confidence intervals calculated for a set of 785 dates of peat (see “Analyzed Material”) on the basis of the Bootstrap Method.

The correct interpretation of the CPDFs depends on the calendar timescale. It is especially important when comparisons with other paleoenvironmental records (e.g. varves) are made (Bartlein et al. 1995). Differences between the ¹⁴C and calendar timescale can be the source of misleading impressions of synchronicity of some events or incorrect estimation of the duration of episodes if ¹⁴C ages are not calibrated. In order to overcome these difficulties, the method of probabilistic calibration of ¹⁴C dates was applied. We used an updated version of the Gliwice Radiocarbon Laboratory Calibration Programme GdCALIB (Pazdur and Michczyńska 1989; Michczyńska et al. 1990). The method of constructing CPDF on the calendar timescale in our program is the same as in OxCal (Bronk Ramsey 1995). We have not used any smoothing. Our earlier study (Michczyńska et al. 2003) shows that the degree of smoothing has no influence on the main peaks and gaps (cf. Figure 6). In the case when only the global changes are the subject of investigation, the degree of smoothing does not play an important role. With the aim of establishing whether the analyzed CPDFs are visibly different to

CPDFs calculated for sets with the same number of dates but for which the dates are uniformly distributed in the calendar timescale, a Monte Carlo experiment (Experiment 2) was performed. Results of the simulations are presented in Figure 7 in the form of 95% confidence intervals for different numbers of dates in the analyzed set ($N = 100, 200, \text{ and } 1000$). The influence of the shape of the calibration curve on the 95% confidence intervals is clearly visible.

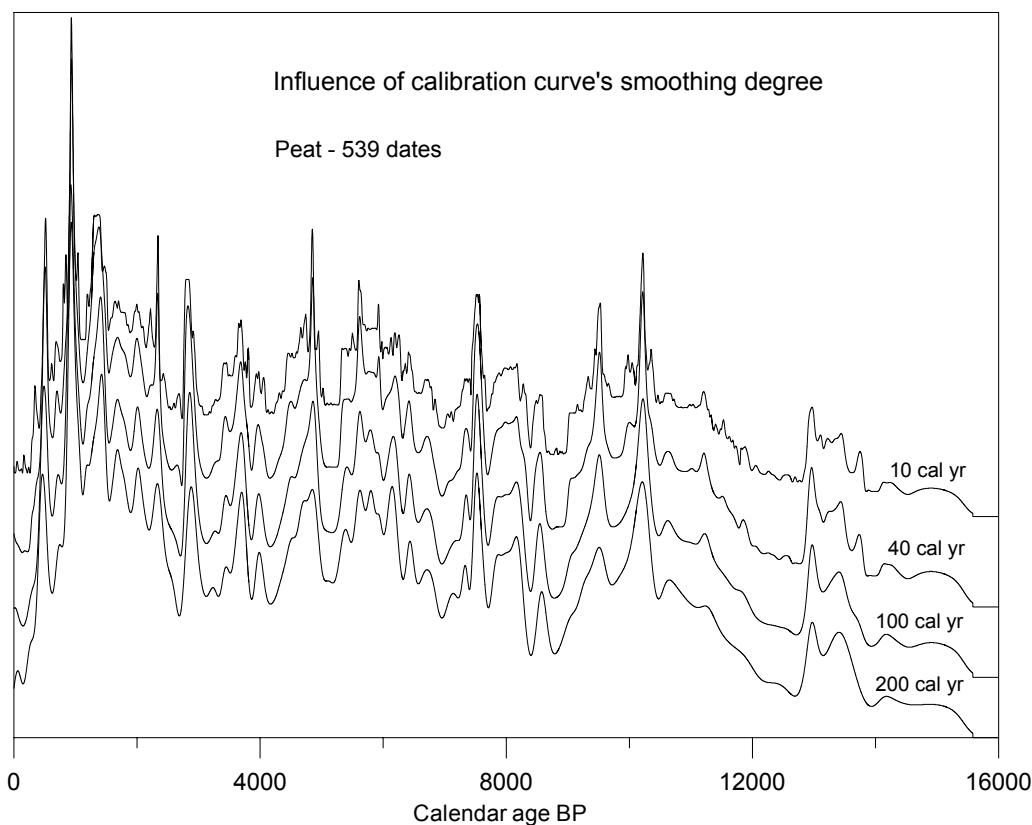


Figure 6 The influence of the calibration curve's smoothing degree on the shape of CPDF. The distributions are constructed for 539 dates of peat samples coming from the whole territory of Poland. Values of the calibration curve's smoothing degree are given in calendar yr; van der Plicht (1993) described details of the smoothing procedure. Particular graphs were vertically separated for higher clarity of the figure (according to Michczyńska et al. 2003).

ANALYZED MATERIAL

A method of statistical analysis for large sets of ^{14}C dates was described with the purpose of identifying environmental changes in the past recorded in the various types of sediment. In this paper, we present the first verification of this method on the basis of ^{14}C dates for peat from Poland. Poland lies in the temperate climate zone of the Northern Hemisphere (latitude $49\text{--}55^\circ\text{N}$, longitude $14\text{--}24^\circ\text{E}$). There are 49,620 peat bogs in Poland (Ilnicki and Żurek 1996). It could be expected that the statistical analysis will show time periods favorable and unfavorable for peat deposition.

For the statistical analysis, 785 dates of peat from Poland were selected. These dates encompassed the Holocene and Late Glacial period (last 14 ^{14}C kyr). The number of ^{14}C dates in particular millennial time periods are shown in Table 1. Dated samples came from Poland, except for those

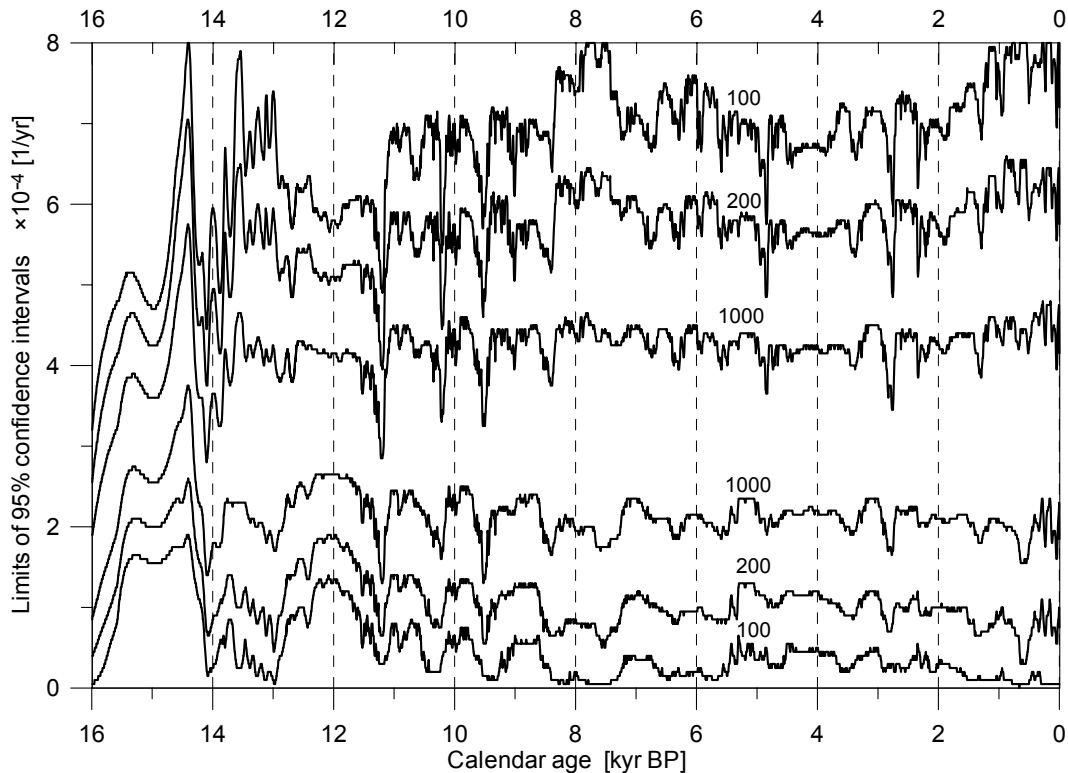


Figure 7 Results of 2nd Monte Carlo experiment. This experiment was executed for $N = 100, 200,$ and 1000 . For all simulations, the mean uncertainty was 115 yr.

from part of the Baltic Coast where changes in the Baltic sink range may influence peat deposition. All dates came from the Gliwice Radiocarbon Laboratory. After pretreatment and carbonization, the samples were combusted, and CO_2 was purified by the standard method used in the Gliwice Radiocarbon Laboratory (Pazdur and Pazdur 1986a). Finally, ^{14}C activity measurements were carried out by gas proportional counting (Pazdur et al. 2000). The result of ^{14}C dating is given as measured ^{14}C age T and its uncertainty ΔT ($T \pm \Delta T$). According to the commonly accepted convention (Stuiver and Polach 1977), the ΔT value is calculated only on the basis of statistical analysis of the measurements and properties of the apparatus without taking into account any extra-laboratory factors. Because peat is a typical organic material and often dated using ^{14}C , this type of deposit was chosen for analysis.

RESULTS AND CONCLUSIONS

We constructed a CPDF for the 785 chosen ^{14}C dates. Results in the calendar timescale are presented in Figure 8. The values of the CPDF exceed the 95% confidence intervals (calculated for 785 ^{14}C dates uniformly distributed on the calendar timescale) for 36.5% of the analyzed interval. This figure indicates that the real distribution of dates on the calendar timescale is not uniform.

For the Late Glacial/Holocene transition, there are many paleoclimatic records. Figure 9 presents an example of the comparison of the CPDF with the isotopic composition of authigenic carbonates in the Younger Dryas section of sediments from Lake Gościąg (Kuc et al. 1998), methane concentra-

Table 1 Number of ^{14}C dates of peat samples versus millennial time periods.

Time range conventional BP	Nr of ^{14}C dates
0–1000	60
1000–2000	72
2000–3000	76
3000–4000	62
4000–5000	80
5000–6000	56
6000–7000	40
7000–8000	49
8000–9000	70
9000–10,000	83
10,000–11,000	58
11,000–12,000	40
12,000–13,000	22
13,000–14,000	5

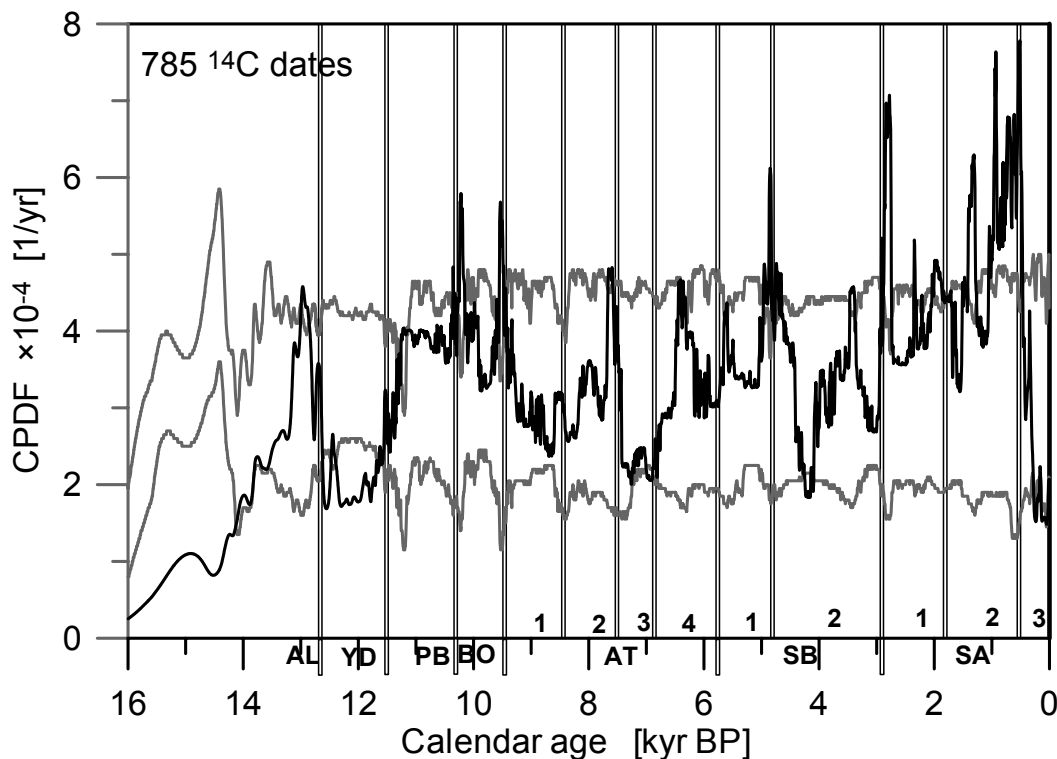


Figure 8 Cumulative probability density function (CPDF) for 785 ^{14}C dates from the interior of Poland is presented as the black curve. The 95% confidence interval is marked in grey based on the uniform distribution on the calendar timescale (cf. experiment Monte Carlo 2). Vertical lines indicate borders of the subdivision of the Late Glacial and Holocene period (Starkel 1999; after calculation on the calendar timescale).

tions in the GRIP ice core (Blunier et al. 1995), and $\delta^{18}\text{O}$ composition in the same ice core (Johnsen et al. 1997). Excellent agreement of the shape of CPDF and other environmental records for Late Glacial/Holocene transition testify the validity of basic assumptions of the statistical analysis. We

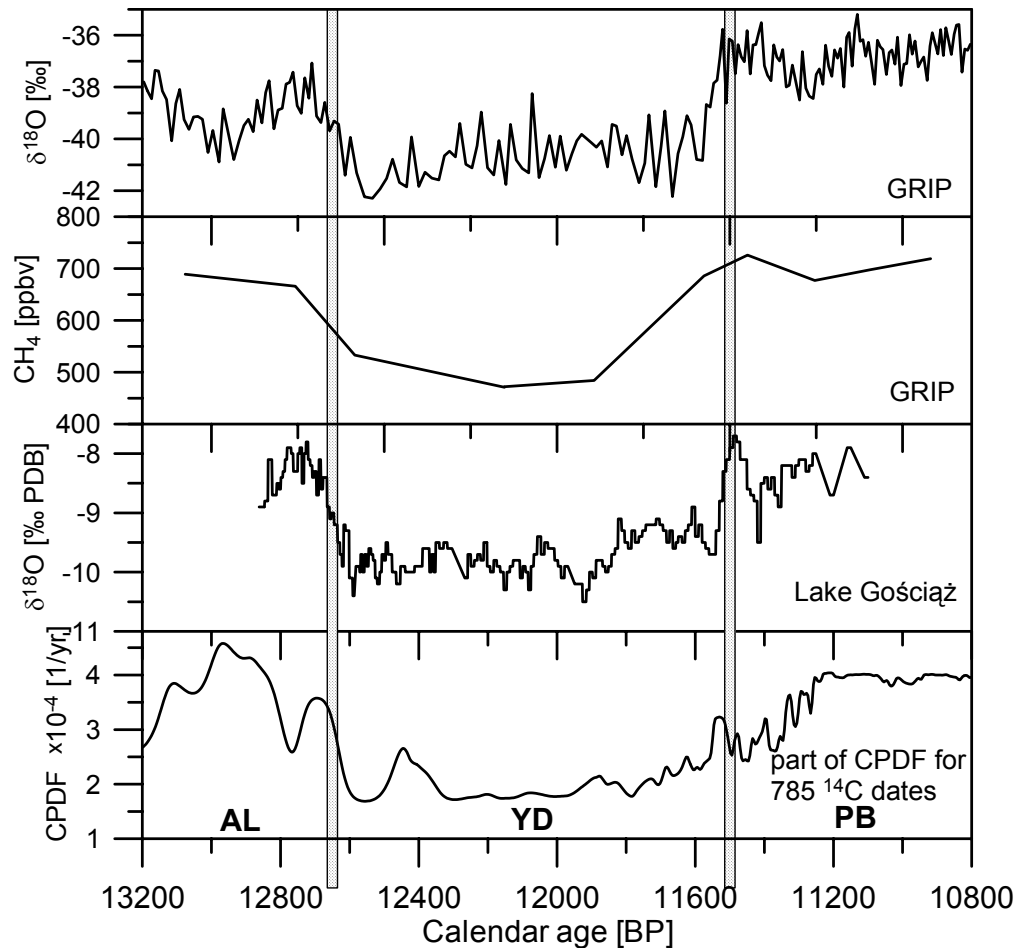


Figure 9 Comparison of part (10,800–13,200 cal BP) of the CPDF constructed for 785 dates and isotopic composition of authigenic carbonates in the Younger Dryas section of the sediments from Lake Gościąg (Kuc et al. 1998), $\delta^{18}\text{O}$ in the Greenland ice core (Johnsen et al. 1997), and methane concentration in the Greenland ice core (Blunier et al. 1995). Vertical grey lines indicate transition AL/YD and YD/PB established in studies of Lake Gościąg sediments (Goslar 1998).

have assumed that the random character of dates is preserved in the case of a large set of ^{14}C dates. Dates came from a large territory, and different investigators interested in various scientific disciplines collected them. However, the shape of the CPDF constructed for the 785 dates is strange. We observed narrow peaks; such narrow peaks are characteristic only for the real CPDF. They are absent for the CPDFs generated in Monte Carlo experiments. We could expect essential changes in the shape of CPDFs at those time periods where changes in environment were present, but the narrow peaks are unexpected. We suppose that their presence near the border of the Holocene subdivisions (cf. Figure 8; Starkel 1999, after calculation on calendar timescale) may be the result of the sampling methodology. Samples for ^{14}C dating are frequently collected only from selected horizons which are of special interest from the point of view of investigator. Because of economic reasons, only a limited number of organic layers can be dated. The general rule of taking samples from places of visible sedimentation changes (e.g. from the top and bottom of the peat layer) may be the reason that samples from the border of the Holocene subdivisions are collected essentially frequently. On

the one hand, preferential sampling hampers analysis, but on other hand, it may be useful to establish the border of the Holocene subdivision on the calendar scale for the analyzed geographical area.

The authors intend to repeat the research, basing it only on ^{14}C dates received for peat samples coming from raised bogs. These type of peat bogs supply all of the moisture from the atmosphere; therefore, the humidity in the upper peat layers depends essentially on precipitation, temperature, and evaporation.

We made the following conclusions from our analysis:

- 200 is the minimum number of dates required for the time interval 0–14 kyr;
- The first Monte Carlo experiment showed that CPDFs have lower statistical fluctuations than histograms;
- The first Monte Carlo experiment showed that the CPDF for 785 dates with a mean uncertainty of 115 yr in the range of 0–14 kyr BP is reliable according to the criteria proposed by Geyh (1980); for histograms, 1530 dates from the same time interval would be required;
- Calculated 95% confidence intervals in Monte Carlo Experiments 1 and 2 allow us to state that the CPDF constructed for the real 785 ^{14}C peat dates from Poland are visibly different than the curve constructed for dates uniformly distributed on the ^{14}C timescale and on the calendar timescale;
- Excellent shape agreement of the CPDF with other environmental records for the Late Glacial/Holocene transition indicate the validity of the basic assumptions of the statistical analysis;
- Along with the assumed proportionality between the number of ^{14}C dates and the amount of deposited organic matter in the studied time intervals, the influence of preferential sampling is visible. The general rule to take samples for ^{14}C dating where changes in sedimentation are observed or from a point in the profile where important changes in pollen are apparent, results in narrow peaks in the CPDF near the climatostratigraphic subdivision.

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