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*Eighth Meeting, Friday, June 14th, 1895.*

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JOHN M'COWAN, Esq., M.A., D.Sc., President, in the Chair.

A Summary of the Theory of the Refraction of their approximately Axial Pencils through a Series of Media bounded by coaxial Spherical Surfaces, with Applications to a Photographic Triplet, &c.

By PROFESSOR CHRYSAL.

*[The Paper will be published in the next Volume.]*

On a Diophantine Equation.

By R. F. DAVIS, M.A.

In the consideration of Question 12612 appearing in the *Educational Times* for January of this year, proposed by the Rev. Dr. Haughton, F.R.S., of Trinity College, Dublin, the following Diophantine Equation suggests itself:

What values of  $x$  make  $8x^3 - 8x + 16 = \square$  ?

Since it may be written  $8x(x^2 - 1) + 16 = \square$  it is obvious that  $x = 0, \pm 1$  are solutions. Also that  $x = 2$  is a solution. Moreover  $x = -\frac{3}{2}$  when substituted gives  $-27 + 12 + 16 = 1$  and is therefore a solution,—marking approximately a limit to the negative root.

I. Put  $8x^3 - 8x + 16 = (px^2 + x - 4)^2$ ; then after reduction and division by  $x^2$ , we have

$$p^2x^2 - 2x(4 - p) + 1 - 8p = 0 \quad \dots \quad \dots \quad \dots \quad (\text{A})$$