

## Nonlinear Survey of RRd Models

R. Szabó<sup>1</sup>, Z. Kolláth<sup>1</sup>, Z. Csubry<sup>2</sup>, J. R. Buchler<sup>3</sup>

**Abstract.** We used our nonlinear hydrodynamical code with turbulent convection to model RR Lyrae stars. In some regime this approach produces double-mode solutions. We investigated series of models with different parameters (metallicity, luminosity, etc.). Our goal was to estimate the width of the double-mode region. The resulting tendencies can be directly compared with observational properties.

The aim of this work was to map the topology of the RRd area in the  $T_{\text{eff}} - L - Z - \alpha_\nu$  (turbulent eddy viscosity) parameter-space at a given stellar mass. An implicit, 1-D Lagrangian, nonlinear hydrodynamical code (Buchler, Kolláth, & Marom 1997) was used that includes turbulent convection (Yecko, Kolláth, & Buchler 1998). Sequences of models were computed with different parameters covering a reasonable range of observable and numerical parameters ( $L = 35 - 55 L_\odot$ ,  $Z = 10^{-4} - 4 \times 10^{-3}$ ,  $\alpha_\nu = 0.2 - 1.8$ ). Stellar masses ( $0.77 M_\odot$ ) and hydrogen content ( $X=0.75$ ) were fixed. The following numerical (dimensionless) parameters were used: number of zones: 120,  $\alpha_1 = 0.41$ ,  $\alpha_c = 0.75$ ,  $\alpha_s = 0.75$ ,  $\alpha_{rmt} = 1.0$ ,  $\alpha_d = 4.0$ ,  $\alpha_p = \frac{2}{3}$ . The calibration of the luminosity-metallicity relation is based on the empirical relation of Jurcsik (1998a) and Table 1 in Dorman's (1992) paper was used for the [Fe/H] -  $Z$  conversion for horizontal-branch stars. We list here some apparent *tendencies* from our sequences:

- An increase in *luminosity* yields a narrower double-mode region DMR and shifts it to higher temperatures (Fig. 1). After the vanishing of double-mode pulsation a broad *either-or region* appears.
- Surprisingly the *metallicity* parameter causes only minor differences.
- The shape of the  $\alpha_\nu - T_{\text{eff}}$  diagram is similar to Fig. 1: an increase in *eddy viscosity* pushes the DMR to higher  $T_{\text{eff}}$ . Another interesting feature is again the apparent *either-or region* at the blue edge of the DMR.
- In order to compare the *location of the DMR* with observational results, models of lower masses were built and similar surveys of lower masses (Bono, Castellani, & Stellingwerf 1995; Feuchtinger 1998) were taken into account. This comparison revealed that the DMR of  $0.65 M_\odot$  is shifted by 150 - 200 K to the blue. In this way excellent agreement can be seen with the position of observed RRd stars in M3 (Bakos & Jurcsik 2000).

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<sup>1</sup>Konkoly Observatory, P.O. Box 67, H-1525 Budapest, Hungary

<sup>2</sup>Eötvös Loránd University, Pázmány Péter sétány, H-1117 Budapest, Hungary

<sup>3</sup>Physics Department, University of Florida, Gainesville, FL 32611, USA

- Nevertheless, there is still a discrepancy between the empirical and theoretical slopes and orientations of the *blue edge of the fundamental instability strip* in the  $L = 35 - 55L_{\odot}$  interval (Jurcsik, 1998b).

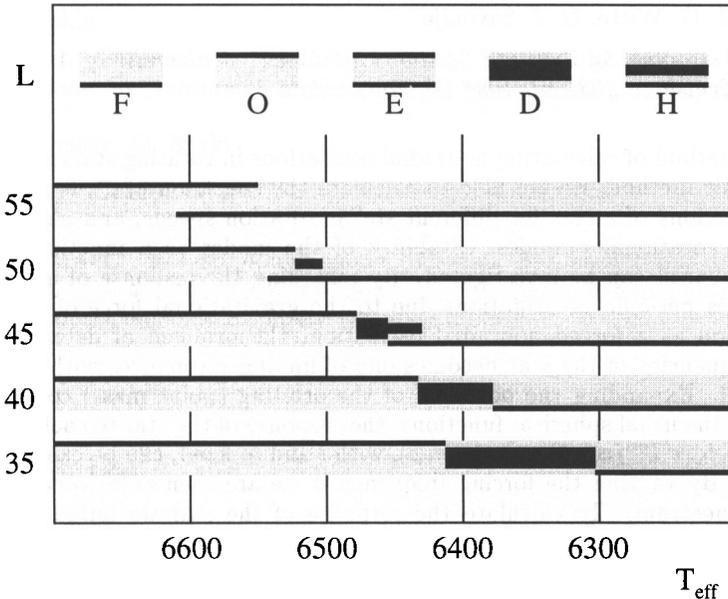


Figure 1. Double-mode (DM) instability region at  $Z=0.0001$ ,  $\alpha_{\nu}=1.0$ . F: fundamental mode only, O: first overtone only, E: either fundamental mode or first overtone, D: DM only, H: either DM or fundamental mode.

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