

THE
BULLETIN
OF
SYMBOLIC LOGIC

EDITED BY

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Articles should be expository or survey papers of broad interest that are accessible to a wide audience of logicians. They may deal with any areas of logic including mathematical or philosophical logic, logic in computer science or linguistics, the history or philosophy of logic, and applications of logic to other fields.

Communications should be announcements of important new results and ideas in any aspect of logic; they may be short papers in their final form or preliminary announcements (extended abstracts, position papers) of longer, full papers that will be published elsewhere. In any case, they should include, in addition to a description of the new results or ideas, enough history, background, and explanation to make the significance of the work apparent to a wide audience. *Communications* will be quickly refereed and published within six months of the submission of final versions.

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Books for review in the BULLETIN should be sent to **Herbert B. Enderton**, *Association for Symbolic Logic, UCLA, Los Angeles, CA 90095-1555, USA*. The other editors of reviews are **Geoffrey Hellman** (hellm001@umn.edu), **Thomas Jech** (jech@math.psu.edu), **Wolfram Pohlers** (pohlers@escher.uni-muenster.de), and **Philip Scowcroft** (pscowcroft@wesleyan.edu). Submitted manuscripts should be typewritten with wide margins and with double spacing between the lines, or prepared with a word processor, such as L^AT_EX or Microsoft Word. Two copies of the manuscript should be sent to the editor, and the author should also keep a complete copy and the electronic file from which the submitted copy was prepared, if a word processor was used. After the paper is accepted in its final form, an electronic copy will be appreciated and will advance the final publication date of the paper, especially if it is in L^AT_EX or A_MS-L^AT_EX. The JOURNAL and the BULLETIN OF SYMBOLIC LOGIC are typeset in a version of A_MS-L^AT_EX, using a stylefile which is posted on the ASL Website, <http://www.aslonline.org>, along with instructions for its use. Fifty offprints of each article are supplied at no charge, and additional offprints may be purchased if desired.

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