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CORRECTION

FINLAY, R. AND SENETA, E. (2006). Stationary-increment Student and variance-gamma processes. J. Appl. Prob. 43, 441–453.

The process

$$\frac{1}{n^{1-\gamma}}(T_{\lfloor nt \rfloor} - \lfloor nt \rfloor) = \frac{1}{n^{1-\gamma}} \sum_{s=1}^{\lfloor nt \rfloor} (G(\psi_{\nu}(s)) - 1)$$

as $n \to \infty$ was considered by Heyde and Leonenko (2005) and in the above paper, where, respectively, $G(x) = G^{R\Gamma}(x) = (\nu/2 - 1)/x$ and $G(x) = G^{\Gamma}(x) = (2/\nu)x$. In both cases, $2\psi_{\nu}(t) \sim \chi_{\nu}^2$ for each t.

The modified Laguerre expansion of $G^{R\Gamma}(x)$ that is used has the first two terms 1 and $1 - (2/\nu)x$, followed by additional terms, whereas the modified Laguerre expansion of $G^{\Gamma}(x)$ consists of two summands, 1 and $(2/\nu)x - 1$, only. Thus,

$$G^{\mathrm{R}\Gamma}(\psi_{\nu}(t)) - 1 = 1 - \frac{2}{\nu}\psi_{\nu}(t) + E_t,$$

where E_t consists of higher-order terms which, as was shown in Heyde and Leonenko (2005, Section 5.1), become asymptotically negligible, while

$$G^{\Gamma}(\psi_{\nu}(t)) - 1 = \frac{2}{\nu}\psi_{\nu}(t) - 1.$$

Hence, the weak limit as $n \to \infty$ in the R Γ (reciprocal gamma) case is the process $-(1/\nu)\sum_{i=1}^{\nu} R_i(t)$ and the weak limit as $n \to \infty$ in the Γ (gamma) case is the process $(1/\nu)\sum_{i=1}^{\nu} R_i(t)$.

The distribution of the random variate R(t) is not in fact symmetric, as claimed in the last two paragraphs on page 450 of the above paper, so the two limit processes in the R Γ and Γ cases are not in fact distributionally equivalent, as claimed there.

References

HEYDE, C. C. AND LEONENKO, N. N. (2005). Student processes. Adv. Appl. Prob. 37, 342–365.