

THE
BULLETIN
OF
SYMBOLIC LOGIC

EDITED BY

RICHARD A. SHORE, Managing Editor

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VOLUME 5 · NUMBER 2 · JUNE 1999
ISSN 1079-8986

PUBLISHED QUARTERLY BY THE ASSOCIATION FOR SYMBOLIC LOGIC, INC.
WITH SUPPORT FROM INSTITUTIONAL AND CORPORATE MEMBERS

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THE BULLETIN OF SYMBOLIC LOGIC (ISSN 1079-8986) is published quarterly, in the months of March, June, September, and December, by the Association for Symbolic Logic, Inc. at 1325 South Oak Street, Champaign, IL 61820-6903, USA. Second class postage is paid at Champaign, IL and additional offices. The BULLETIN is distributed with THE JOURNAL OF SYMBOLIC LOGIC; the 1999 annual subscription price for the two journals is \$340. Postmaster: Send address changes to *The Bulletin of Symbolic Logic, Journals Division UIP, 1325 South Oak Street, Champaign, IL 61820-6903, USA*. Business correspondence should be sent to the Secretary-Treasurer of the Association, C. Ward Henson (address on inside back cover).

The BULLETIN and the JOURNAL are the official organs of the Association for Symbolic Logic, an international organization for furthering research in symbolic logic and the exchange of ideas among mathematicians, philosophers, computer scientists, linguists, and others interested in this field.

The BULLETIN invites submission of *Articles* and *Communications*. *Articles* should be expository or survey papers of broad interest that are accessible to a wide audience of logicians. They may deal with any areas of logic including mathematical or philosophical logic, logic in computer science or linguistics, the history or philosophy of logic, and applications of logic to other fields. *Communications* should be announcements of important new results and ideas in any aspect of logic; they may be short papers in their final form or preliminary announcements (extended abstracts, position papers) of longer, full papers that will be published elsewhere. In any case, they should include, in addition to a description of the new results or ideas, enough history, background, and explanation to make the significance of the work apparent to a wide audience. *Communications* will be quickly refereed and published within six months of the submission of final versions.

Continued on inside back cover

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The four numbers of Volume 5 were issued at the following dates:

Number 1, pages 1–160, April 20, 1999

Number 2, pages 161–288, June 17, 1999

Number 3, pages 289–432, October 14, 1999

Number 4, pages 433–584, December 15, 1999

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ERRATUM

Vol. 4 (1998), No. 4, p. 461, line 11, replace \prod_1^0 by \prod_2^0 , so that the last theorem in the Abstract by Coles, Downey and Khousainov reads as follows:

Theorem: There exists a computable linearly ordered set with a \prod_2^0 -initial segment which does not possess a computable presentation.